## Curriculum Development Course at a Glance Planning for 3<sup>rd</sup> Grade Mathematics

| Content Area   | Mathematics     Grade Level     3 <sup>rd</sup> Grade                     |  |   |  |                                |
|--|---|--|---|--|--------------------------------|
| Course Name/Course Code  |   |  |   |  |                                |
| Standard   | Grade Level Expectations (GLE)  |  |   |  | GLE Code                       |
| 1. Number Sense, Properties, and<br>Operations   | <ol> <li>The whole number system describes plac<br/>algorithms</li> </ol> | e value relatio  | nships and forms the found  | ation for efficient  | MA10-GR.3-S.1-GLE.1            |
|  | 2. Parts of a whole can be modeled and rep                                | resented in dif  | fferent ways  |  | MA10-GR.3-S.1-GLE.2            |
|  | 3. Multiplication and division are inverse op                             | erations and c   | an be modeled in a variety  | of ways  | MA10-GR.3-S.1-GLE.3            |
| 2. Patterns, Functions, and<br>Algebraic Structures  | Expectations for this standard are integra                                | ited into the o  | ther standards at this grade  | level.   |                                |
| 3. Data Analysis, Statistics, and<br>Probability   | 1. Visual displays are used to describe data                              |  |   |  | MA10-GR.3-S.3-GLE.1            |
| 4. Shape, Dimension, and   | 1. Geometric figures are described by their                               | attributes   |   |  | MA10-GR.3-S.4-GLE.1            |
| Geometric Relationships  | 2. Linear and area measurement are fundar                                 | nentally differ  | ent and require different ur  | nits of measure  | MA10-GR.3-S.4-GLE.2            |
|  | 3. Time and attributes of objects can be me                               | asured with ap   | opropriate tools  |  | MA10-GR.3-S.4-GLE.2            |
| Service       Critical Thinking and Reasoning: Thinking Deeply, Thinking Differently         Information Literacy: Untangling the Web         Collaboration: Working Together, Learning Together         Self-Direction: Own Your Learning         Invention: Creating Solutions |   | Mathem<br>1. Mal<br>2. Rea<br>3. Con<br>4. Mo<br>5. Use<br>6. Atto<br>7. Loo<br>8. Loo | atical Practices:<br>ke sense of problems and p<br>ison abstractly and quantita<br>istruct viable arguments an<br>del with mathematics.<br>e appropriate tools strategic<br>end to precision.<br>k for and make use of struct<br>k for and express regularity | ersevere in solving t<br>tively.<br>d critique the reasor<br>ally.<br>ture.<br>in repeated reasoni | hem.<br>ning of others.<br>ng. |
| Unit Titles  |   |  | Length of Unit/Contact H  | ours Unit Nu   | umber/Sequence                 |
| Multiply, Divide & Conquer   |   |  | 5 weeks   | 1  |                                |
| Everything Has a Place   |   |  | 4 weeks   | 2  |                                |
| Inside, Outside, What's it All About?  |   |  | 4 weeks   | 3  |                                |
| Fun with Fractions   |   |  | 4 weeks   | 4  |                                |
| Collect, Represent, What Does it Mean?   |   |  | 3 weeks   | 5  |                                |
| Time, Volume and Mass, Oh My!  |   |  | 3 weeks   | 6  |                                |
| Shape it Up!   |   |  | 2 weeks   | 7  |                                |

Authors of the Sample: Margaret Brownley (Douglas County RE 1); Paige Wild (Boulder Valley RE 2)

3<sup>rd</sup> Grade, Mathematics

| Unit Title                                     | Multiply, Divide & Conquer   |   | Length of Unit   | 5 weeks   |
|--|--|---|--|---|
| Focusing Lens(es)                              | Interpretation/Relationships   | Standards and Grade<br>Level Expectations<br>Addressed in this Unit                                 | MA10-GR.3-S.1-GLE.3  |   |
| Inquiry Questions<br>(Engaging-<br>Debatable): | • How are multiplication and division related? (MA10-GR.3-S.1-GLE.3-IQ.1)                              |   |  |   |
| Unit Strands                                   | Operations and Algebraic Thinking, Personal Financial Literacy   |   |  |   |
| Concepts                                       | Multiplication, division, equal g<br>many, times fewer, unknown f<br>distributive property, identity p | groups, arrays, combinations, f<br>actor, inverse operations, sub<br>property, zero property), equa | fair share, rate, scaling, area, unit conv<br>stitution, models, properties of operati<br>tions, arithmetic patterns | ersions, addition, subtraction, rows, columns, times as ions (commutative property, associative property, |

| Generalizations<br>My students will Understand that   | Guiding   | Questions<br>Conceptual   |
|---|---|---|
| Multiplication and division word problems can involve<br>situations of equal groups, arrays, combinations, fair<br>sharing, rate, scaling, area, and unit conversions (MA10-<br>GR.3-S.1-GLE.3-EO.a.i, a.ii, a.iii) | What does the product (quotient) represent in a context?  | How can you determine if a story problem represents a multiplication/division problem?  |
| Compared with addition/subtraction, multiplication<br>and/or division provide highly efficient means to solve<br>equal-group story problems (MA10-GR.3-S.1-GLE.3-EO.c.i)  | What does it mean to be efficient?<br>Why was multiplication invented? Why not just add?<br>(MA10-GR.3-S.1-GLE.3-IQ.3)<br>Why was division invented? Why not just subtract?<br>(MA10-GR.3-S.1-GLE.3-IQ.4) | Why is (insert a contextual problem with unequal groups)<br>a multiplication or addition problem?   |
| Division enables decision-making determinations<br>regarding the size of groups or the number of groups in a<br>given context (MA10-GR.3-S.1-GLE.3-EO.a.ii)   | What does it mean to count how many are in a group<br>versus the number of groups?<br>What are two types of equal group division problems?  | How do equal problems lead to types of answers to division problems?  |
| Arrays such that an array of m rows and n columns has n x<br>m items can model multiplication and division word<br>problems (MA10-GR.3-S.1-GLE.3-EO.a.iii)  | What is an array?<br>What are rows and columns?<br>How can an array model be used to help solve a<br>combination problem such as 3 pants and 2 shirts?  | How is an array a model for multiplication?<br>How can an array model show the commutative<br>property?<br>How are arrays connected to the concept of area? |

| The comparison of the size of a collection against the size<br>of a group reflects multiplication and division problems<br>related to the concept of "times as many" or "times<br>fewer" (MA10-GR.3-S.1-GLE.3-EO.a)  | What is the difference between comparing one group as<br>n "times as many" than another group and<br>comparing by stating how many more are in one<br>group?  | How can comparing groups lead to multiplication and division problems?   |
|--|---|--|
| Because multiplication and division are inverse<br>operations, multiplication provides and effective means<br>to solve division problems as unknown factor problems<br>(MA10-GR.3-S.1-GLE.3-EO.b.ii)   | How can you use a multiplication or division fact to find a related fact?   | How are multiplication and division related? (MA10-<br>GR.3-S.1-GLE.3-IQ.1)<br>Why is division by zero undefined?  |
| Arithmetic patterns, justified by properties of operation,<br>constitute strategies that can be used to multiply and<br>divide (MA10-GR.3-S.1-GLE.3-EO.d.iv)   | <ul> <li>What patterns do you notice in a multiplication table?<br/>Addition table?</li> <li>How can three numbers be multiplied in any order to<br/>solve a multiplication problem (e.g., 2 x 7 x 5 or 14 x<br/>5?)</li> <li>How do arithmetic patterns help to build fluency with<br/>basic facts?</li> </ul> | Why are zero and one special in multiplication?<br>Why do odd numbers times odd numbers result in odd<br>numbers? Is there another way to get an odd number<br>when multiplying? |
| Fluency with multiplication and division facts results from<br>multiple experiences with different models,<br>representations, problem types, properties of operations<br>and interrelationships among multiplication and division<br>facts (MA10-GR.3-S.1-GLE.3-EO.c.i, c.ii) | How can you use a multiplication or division fact to find<br>a related fact? (MA10-GR.3-S.1-GLE.3-IQ.2)<br>How can strategies such as doubling, halving, skip<br>counting, partitioning and reassembling help to<br>develop fluency with basic multiplication facts?  | Why is relying solely on rote memorization of facts limiting when learning more advanced mathematics?  |

| Key Knowledge and Skills: | What students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics |
|---------------------------|---|
| My students will          | samples what students should know and do are combined.  |

- Solve word problems involving equal groups, measurement quantities, and arrays by using multiplication and division (MA10-GR.3-S.1-GLE.3-EO.a.iii)
- Represent multiplication and division story problems by using drawings and equations with a symbol for the unknown number (MA10-GR.3-S.1-GLE.3-EO.a.iii)
- Understand division as an unknown-factor problem (MA10-GR.3-S.1-GLE.3-EO.b.ii)
- Model strategies to achieve a personal financial goal using arithmetic operations (MA10-GR.3-S.1-GLE.3-EO.a.v)\*
- Interpret whole-number products and quotients (MA10-GR.3-S.1-GLE.3-EO.a.i, a.ii)
- Determine the unknown whole number in a multiplication or division equation relating three whole numbers (MA10-GR.3-S.1-GLE.3-EO.a.iv, b.ii)
- Apply properties of operations as strategies to multiply and divide (MA10-GR.3-S.1-GLE.3-EO.d)
- Identify and explain patterns in arithmetic (including patterns in addition and multiplication tables) using properties of operations (MA10-GR.3-S.1-GLE.3-EO.d)
- Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (MA10-GR.3-S.1-GLE.3-EO.c)

\*Denotes connection to Personal Financial Literacy (PFL)

| A student in<br>ability to apply and comp<br>through the following sta | can demonstrate the<br>rehend critical language<br>tement(s):      | If 24 apples are arranged into 4 equal rows, I know that 6 apples will be in each row because 6x4 equals 24, and 24/4<br>equals 6.                                |
|--|--|---|
| Academic Vocabulary: Fair share, represent, equal, gro                 |  | ups, model, solve, interpret, rows, columns, times as many, times fewer, unknown  |
|  |  |   |
| Technical Vocabulary:  | Product, quotient, whole numbe<br>combinations, area, addition, su | er, operation, multiplication, division, pattern, equation, strategy, relationship, unknown factor, properties, array,<br>Ibtraction, factor, inverse operations, |

| Unit Title                                     | Everything Has a Place   |   | Length of Unit      | 4 weeks |
|--|--|---|---------------------|---------|
| Focusing Lens(es)                              | Efficiency   | Standards and Grade<br>Level Expectations<br>Addressed in this Unit | MA10-GR.3-S.1-GLE.1 |         |
| Inquiry Questions<br>(Engaging-<br>Debatable): | • How might our number system be different if humans had twenty figures instead of ten? (MA10-GR.3-S.1-GLE.1-IQ.2)   |   |                     |         |
| Unit Strands                                   | Operations and Algebraic Thinking, Number and Operations in Base Ten   |   |                     |         |
| Concepts                                       | Reasonableness, rounding, number properties, mental computation, common sense, estimation, sums, differences, place value, variables, unknown quantities, properties of operations, addition, subtraction, fluency, flexibility, standard algorithm, multiples of ten, multiplication, decomposing |   |                     |         |

| Generalizations<br>My students will <b>Understand</b> that   | Guiding (<br>Factual  | Questions<br>Conceptual  |
|--|---|--|
| Multiple methods of assessing the reasonableness of an<br>answer (e.g., rounding, context clues, number properties,<br>mental computation) provide opportunities to<br>(re)evaluate the interpretation of a problem (MA10-GR.3-<br>S.1-GLE.1-EO.d.i, d.iii)      | What is mental computation?<br>What strategies do we use to check or evaluate our<br>mental calculations?   | Why is it important to assess the reasonableness of an answer?   |
| Successful estimation of sums and differences by<br>rounding to the nearest 10 or 100 depends on a thorough<br>understanding of place value within a base-ten system<br>(MA10-GR.3-S.1-GLE.1-EO.a.i)   | What does it mean to round?<br>How do we use rounding in our everyday use of<br>mathematics?  | How does rounding make mental computation easier?  |
| Letters (called variables) often represent unknown quantities in equations (MA10-GR.3-S.1-GLE.1-EO.d.ii)   | When might we use a variable and why?   | Why are letters used to represent unknown quantities?  |
| Facility with place value, properties of operations and<br>number relationships increases flexibility with addition<br>and subtraction of multi-digit numbers and leads to<br>conceptual understanding of (standard) algorithms<br>(MA10-GR.3-S.1-GLE.1-EO.a.ii) | <ul> <li>What is a place value strategy that is useful in problem solving?</li> <li>How is knowledge of properties of operations useful in problem solving?</li> <li>How does the relationship between addition and subtraction strategy help us problem solve</li> </ul> | How is place value important in addition and subtraction<br>of multi-digit numbers?<br>Why does the standard algorithm work? |

| The continued practice of decomposing multiples of ten<br>into ten times a number increases multiplication abilities<br>(MA10-GR.3-S.1-GLE.1-EO.a.iii) | <ul><li>What does it mean to decompose through<br/>multiplication?</li><li>How does previous experience with counting forwards<br/>and backwards by decades help when multiplying a<br/>number by a multiple of ten?</li></ul> | Why is ten so important when multiplying larger numbers? |
|--|--|--|
|--|--|--|

| Key Knowledge and Skills:<br>My students will | What students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics samples what students should know and do are combined. |
|---|--|
|   |  |

- Use place value understanding to round whole numbers to the nearest 10 or 100. (MA10-GR.3-S.1-GLE.1-EO.a.ii)
- Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction (MA10-GR.3-S.1-GLE.1-EO.a.iii)
- Multiply one-digit whole numbers by multiples of 10 in the range 10-90 using strategies based on place value and properties of operations (MA10-GR.3-S.1-GLE.1-EO.a.iii)
- Solve two-step word problems using the four operations and asses the reasonableness of answers using mental computation and estimation strategies (MA10-GR.3-S.1-GLE.1-EO.d.i, d.iii)
- Represent word problems using equations with a letter standing for the unknown quantity (MA10-GR.3-S.1-GLE.1-EO.d.ii)

| A student in<br>ability to apply and comp<br>through the following stat | can demonstrate the<br>rehend critical language<br>rement(s):   | I know that 398 +154 is close to 550, because I rounded to the nearest 100 and the nearest 10, so my estimation is 400 +150, and I added those two numbers. |
|---|---|---|
| Academic Vocabulary:  | Reasonableness, common sense  | 2   |
|   |   |   |
| Technical Vocabulary:   | Round, mental computation, estimation, place value, variable, addition, subtraction, algorithms, multi-digit numbers, digit, fluency, flexibility, standard algorithm, multiples (of ten), multiplication |   |

| Unit Title                                     | Inside, Outside, What's it All A   | bout?   | Length of Unit      | 4 weeks |
|--|--|---|---------------------|---------|
| Focusing Lens(es)                              | Representations  | Standards and Grade<br>Level Expectations<br>Addressed in this Unit | MA10-GR.3-S.4-GLE.2 |         |
| Inquiry Questions<br>(Engaging-<br>Debatable): | <ul> <li>How does what we measure influence how we measure? (MA10-GR.3-S.4-GLE.2-IQ-3)</li> <li>Why do we measure area in square units?</li> </ul>   |   |                     |         |
| Unit Strands                                   | Measurement and Data   |   |                     |         |
| Concepts                                       | Square, unit, unit square, square units, area, rows, columns, gaps, overlaps, rectangle, addition, multiplication, partitioning, rectangular array, length, width, conservation, formula, compose, decompose, distributive property, perimeter |   |                     |         |

| Generalizations<br>My students will <b>Understand</b> that   | Guiding Questions<br>Factual Conceptual   |  |
|--|---|--|
| A square with side lengths 1 unit, called "a unit square"<br>represents "one square unit," a form of measurement<br>that facilitates the computation of area in rectangles<br>(MA10-GR.3-S.4-GLE.2-EO.a.i)   | What is a square unit?  | How are square units used to measure area?<br>How does the size of a unit square impact the number of<br>squares required to cover a shape?  |
| Rectangles decomposed into rows and columns of square<br>units encourages the use of repeated addition or<br>multiplication strategies to solve for area- defined as the<br>interior of a two-dimensional figure covered, without gap<br>or overlap, by n unit squares (MA10-GR.3-S.4-GLE.2-<br>EO.a.ii) | What are rows and columns?<br>What does it mean if a shape can tessellate?<br>Which shapes tessellate? Could you use these shapes to<br>measure area?   | <ul><li>How can rows and columns be used to efficiently solve for area?</li><li>Why is it important to measure area with a shape that tessellates?</li><li>Why were squares chosen as the standard unit for measuring area?</li></ul>  |
| The addition of the number of units in the rows and<br>columns corresponding with the sides of a rectangle<br>determines the rectangle's perimeter (MA10-GR.3-S.4-<br>GLE.2-EO.a.ii)   | <ul> <li>How can you determine the number of rows and columns in rectangle if you know the length and width?</li> <li>If you know the length plus the width of a rectangle, how can you find its perimeter?</li> <li>How can you determine the unknown side length of any polygon whose perimeter is known?</li> <li>What's the difference between perimeter and area?</li> <li>What are ways to describe the size of an object or shape? (MA10-GR.3-S.4-GLE.2-IQ.2)</li> </ul> | <ul> <li>How do length and width measurements, measured in units, help to find an area measurement in square units?</li> <li>Why is addition used to find perimeter?</li> <li>How is it possible to have two rectangles with the same perimeter and different areas?</li> <li>How is it possible to have two rectangles with the same area and different perimeters?</li> <li>Why is perimeter considered additive and area multiplicative?</li> </ul> |

| Partitioned rectangles (into rectangular arrays of squares)<br>provides a visual representation of the formula: area of<br>rectangle = length x width (MA10-GR.3-S.4-GLE.2-EO.a.ii)   |  | What is a rectangular array?<br>How can finding the area of rectangles help build<br>fluency with basic multiplication and division facts? | Why is multiplication used to find the area of a rectangle? |
|---|--|--|---|
| Areas of rectangles, combined, illustrate the distributive<br>property if the lengths of one side of each rectangle are<br>the same (i.e., A rectangle with side lengths "a" and "b"<br>combined with a rectangle with side lengths "a" and "c"<br>creates a rectangle whose area can be represented in the<br>equation (a x b) + (a x c) = a (b + c)) (MA10-GR.3-S.4-<br>GLE.2-EO.a.iii)   |  | How can you show that (a x b) + (a x c) = a (b + c) using<br>area models?  | Why is (a x b) + (a x c) = a (b + c) true?                  |
|   |  | •  | · · · · · · · · · · · · · · · · · · ·                       |
| Key Knowledge and Skills:<br>My students willWhat students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics<br>samples what students should know and do are combined.  |  |  |   |
| <ul> <li>Know that a plane figure, which can be covered without gaps or overlaps by <i>n</i> unit squares is said to have an area of <i>n</i> square units (MA10-GR.3-S.4-GLE.2-EO.a.i)</li> <li>Find the area of a rectangle with whole-number side lengths using a variety of methods, including counting unit squares, tiling using a row and column structure, and multiplying side lengths (MA10-GR.3-S.4-GLE.2-EO.a.ii)</li> <li>Represent whole-number products as rectangular areas (MA10-GR.3-S.4-GLE.2-EO.a.iii)</li> <li>Recognize area as additive (MA10-GR.3-S.4-GLE.2-EO.a.iii)</li> <li>Find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas for the non-overlapping parts (MA10-GR.3-S.4-GLE.2-EO.a.iii)</li> <li>Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths a and b + c is the sum of a x b and b x c (MA10-GR.3-S.4-GLE.2-EO.a.iii)</li> <li>Use area models to represent the distributive property in mathematical reasoning (MA10-GR.3-S.4-GLE.2-EO.a.iii)</li> <li>Find the perimeter given the side lengths of a polygon (MA10-GR.3-S.4-GLE.2-EO.c.i)</li> <li>Find an unknown side length of a polygon given the perimeter (MA10-GR.3-S.4-GLE.2-EO.c.ii)</li> <li>Find rectangles with the same perimeter and different areas or with the same area and different perimeters (MA10-GR.3-S.4-GLE.2-EO.c.iii)</li> <li>Show how area can remain constant when composing and decomposing shapes made up of square units (MA10-GR.3-S.4-GLE.2-EO.c.)</li> </ul> |  |  |   |

| A student in can demonstrate the ability to apply and comprehend critical language through the following statement(s): |   | I multiplied the side lengths of this rectangle to find the area.<br>I know this first column has 7 square units and there are 6 columns, which means my area will be 7+7+7+7+7+7 or 7x6.<br>I found the perimeter of this shape by adding the side lengths together. |  |  |
|--|---|---|--|--|
| Academic Vocabulary:   | mic Vocabulary: Measure, row, column, gaps, overlaps, rectangle, length, width, |   |  |  |
| Technical Vocabulary:  | Unit, unit square, square uni   | t, unit square, square units, array, area, perimeter, multiplication, addition, square unit, unit square, conservation, formula,  |  |  |

| Unit Title                                     | Fun with Fractions   |   | Length of Unit      | 4 weeks |
|--|--|---|---------------------|---------|
| Focusing Lens(es)                              | Part/Whole   | Standards and Grade<br>Level Expectations<br>Addressed in this Unit | MA10-GR.3-S.1-GLE.2 |         |
| Inquiry Questions<br>(Engaging-<br>Debatable): | <ul> <li>Why do fractions have more than one name? (MA10-GR.3-S.1-GLE.2-IQ-2)</li> <li>When are two halves not equal?</li> </ul> |   |                     |         |
| Unit Strands                                   | Number and Operations – Fractions  |   |                     |         |
| Concepts                                       | Fraction, whole, equal part, equivalent fraction, numerator, denominator, represent, partition, quantity                         |   |                     |         |

| Generalizations<br>My students will <b>Understand</b> that   | Guiding  | Questions<br>Conceptual  |
|--|--|--|
| Partitioning a whole into equal parts establishes/results in/creates fractions (MA10-GR.3-S.1-GLE.2-EO.a.i)  | What is partitioning?<br>How does partitioning a whole into equal parts<br>establish/result in/creates fractions? (MA10-GR.3-<br>S.1-GLE.2-IQ-1)   | Why and when do we need to break wholes into parts?  |
| The size of a fractional part (of a fraction) directly relates<br>to the size of the whole (MA10-GR.3-S.1-GLE.2-EO.a.i;<br>IQ.3)   | Why do we distinguish the fractional part of a fraction?<br>How does the size of the fractional part change when<br>the size of the whole changes? | When would we change the size of the "whole" part of a fraction?   |
| Equivalent fractions represent the same quantity (size)<br>and point on number line but can have different<br>numerators and denominators (MA10-GR.3-S.1-GLE.2-<br>EO.a.ii, a.iii.1)                         | What are the numerator and denominator?<br>What is the relationship between the numerator and<br>denominator?                                      | Why would you need to represents two equivalent fractions as having different numerators and denominators? |
| Two fractions with the same numerators and<br>denominators represent the same quantity (size) and can<br>be compared to each other if they refer to the same<br>whole (MA10-GR.3-S.1-GLE.2-EO.a.iii.5; RA.2) | Can you imagine when getting I/2 of a particular<br>"whole" would not be as good as getting 1/8 of<br>another "whole"? (MA10-GR.3-S.1-GLE.2-RA.1)  | How can fractions be used to mislead our thinking about the value of our share?                            |
| Fractions represent numbers equal to, less than, or greater than 1 (MA10-GR.3-S.1-GLE.2-EO.a.ii)   | What does represent mean?<br>How do you know when a fraction represents a number<br>less than one? Equal to one? More than one?                    | Why would you use a fraction to represent a number greater than one?                                       |

| Key Knowledge and Sk<br>My students will  | <b>Nowledge and Skills:</b> What students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics samples what students should know and do are combined.   |  |  |  |  |
|---|--|--|--|--|--|
| <ul> <li>Understand a fraction<br/>(MA10-GR.3-S.1-GLE.2</li> <li>Represent a fraction 1/<br/>1/b and the endpoint of<br/>Represent a fraction a/<br/>number a/b on the num</li> <li>Understand two fraction</li> <li>Recognize and generate</li> <li>Explain why two fractions</li> <li>Express whole number</li> <li>Compare two fractions</li> <li>Explain why comparison</li> <li>Record the results of compare</li> </ul> | <ul> <li>Understand a fraction 1/b as the quantity formed by 1 part when a whole is partitioned into be equal parts and a fraction a/b as the quantity formed by a parts of size 1/b (MA10-GR.3-S.1-GLE.2-EO.a.i)</li> <li>Represent a fraction 1/b on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts and recognize that each part has size 1/b and the endpoint of the part based at 0 locates the number 1/b on the number line (MA10-GR.3-S.1-GLE.2-EO.a.ii)</li> <li>Represent a fraction a/b on number line diagram by marking off a lengths 1/b from 0 and recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line (MA10-GR.3-S.1-GLE.2-EO.a.ii)</li> <li>Understand two fractions are equivalent (equal) if they are the same size, or the same point on a number line (MA10-GR.3-S.1-GLE.2-EO.a.iii.1)</li> <li>Recognize and generate simple equivalent fractions (MA10-GR.3-S.1-GLE.2-EO.a.iii.2)</li> <li>Explain why two fraction are equivalent (MA10-GR.3-S.1-GLE.2-EO.a.iii.2)</li> <li>Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers (MA10-GR.3-S.1-GLE.2-EO.a.iii.3)</li> <li>Compare two fractions with the same numerator or the same denominator by reasoning about their size (MA10-GR.3-S.1-GLE.2-EO.a.iii.4)</li> <li>Explain why comparisons are valid only when the two fractions refer to the same whole (MA10-GR.3-S.1-GLE.2-EO.a.iii.5)</li> </ul> |  |  |  |  |
|   |  |  |  |  |  |
| Critical Language: includes the Academic and Technical vocabulary, semantics, and discourse which are particular to and necessary for accessing a given discipline.<br>EXAMPLE: A student in Language Arts can demonstrate the ability to apply and comprehend critical language through the following statement: "Mark Twain exposes the hypocrisy of slavery through the use of satire."                                    |  |  |  |  |  |
| A student in can demonstrate the ability to apply and comprehend critical language through the following statement(s): Sharing one quarter of my banana is not the same as sharing one quarter of your watermelon, therefore, ¼ = ¼ doe not always tell the complete story. Actual comparison or value judgments depend on the whole!   |  |  |  |  |  |
| Academic Vocabulary: Compare, explain, record, reason   |  |  |  |  |  |

| Technical Vocabulary: | Numerator, denominator, fraction, whole, part, equivalent fraction, number line, partition, equivalence |
|-----------------------|---|
|-----------------------|---|

| Unit Title                                     | Collect, Represent, What Does it Mean?  |   | Length of Unit      | 3 weeks |
|--|---|---|---------------------|---------|
| Focusing Lens(es)                              | Interpretation  | Standards and Grade<br>Level Expectations<br>Addressed in this Unit | MA10-GR.3-S.3-GLE.1 |         |
| Inquiry Questions<br>(Engaging-<br>Debatable): | <ul> <li>Why are data displays important and what data are important to display? (MA10-GR.3-S.3-GLE.1-IQ.2)</li> <li>Do data displays simply help us understand information, or can they (mis)lead us to particular conclusions?</li> </ul> |   |                     |         |
| Unit Strands                                   | Measurement and Data  |   |                     |         |
| Concepts                                       | Data, graph, representation, interpretation, icons, pictographs (scaled picture graph), bar graph, axis, unit, measurement, variation, measurement error, communities   |   |                     |         |

| Generalizations   | Guiding Questions  |   |
|---|--|---|
| My students will <b>Understand</b> that   | Factual  | Conceptual  |
| Data represented visually (e.g., graphs) provide a means<br>to capture, convey, and facilitate greater understanding<br>of information (MA10-GR.3-S.3-GLE.1-EO.a)   | What is data?<br>What does it mean to interpret a graph?   | Why do we use graphs to represent data?<br>How does interpreting a graph help you learn more<br>about the data collected? |
| The creators of graphs often use icons, pictographs<br>(scaled picture graph) and tick marks on the axis of a bar<br>graph to denote more than one unit when trying to<br>concisely represent a large amount of data (MA10-GR.3-<br>S.3-GLE.1-EO.a.i, a.ii) | How can you a pictograph or bar graph to answer<br>questions such as, "how many more" or "how many<br>less"?                       | How can you represent large numbers on a pictograph?<br>Bar graph?  |
| Visual data representations of people's experiences,<br>beliefs, preferences, and attitudes increase<br>understandings of given communities (MA10-GR.3-S.3-<br>GLE.1-RA.1)  | What can data tell us about our school or class?<br>What kinds of information could we collect and display<br>about our community? | What can we do with the data we collect and display?  |

| Key Knowledge and Skills: | What students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics |
|---------------------------|---|
| My students will          | samples what students should know and do are combined.  |

- Draw scaled picture graphs and scaled bar graphs to represent a data set with several categories (MA10-GR.3-S.3-GLE.1-EO.a.i)
- Solve one- and two-step "how many more" and "how many less" problems using information presented in scaled bar graphs (MA10-GR.3-S.3-GLE.1-EO.a.ii)
- Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch then show the data by making a line plot, where the horizontal scale is marked off in appropriate units (e.g. whole numbers, halves, or quarters) (MA10-GR.3-S.3-GLE.1-EO.a.iii)

| A student in<br>ability to apply and comp<br>through the following sta | can demonstrate the<br>rehend critical language<br>tement(s): | This graph shows me that 5 more kids in our class have dogs than have cats.  |
|--|---|--|
| Academic Vocabulary:   | Generate, draw, represent, inte                               | erpret, collect, icon  |
| Technical Vocabulary:  | Graph, line plot, scaled picture                              | graph (pictograph), scaled bar graph, data set, data, categories, axis, unit |

| Unit Title                                     | Time, Volume and Mass, Oh My!   |   | Length of Unit      | 3 weeks |
|--|---|---|---------------------|---------|
| Focusing Lens(es)                              | Reliability   | Standards and Grade<br>Level Expectations<br>Addressed in this Unit | MA10-GR.3-S.4-GLE.3 |         |
| Inquiry Questions<br>(Engaging-<br>Debatable): | <ul> <li>What would happen if we did not have standard units of measure for time or volume or mass? (MA10-GR.3-S.4-GLE.3-IQ-1)</li> <li>What is the best way to measure the passage of time?</li> </ul> |   |                     |         |
| Unit Strands                                   | Measurement and Data  |   |                     |         |
| Concepts                                       | Hours, seconds, minutes, elapsed time, time, standard units, measurement, revolution, regrouping, base number systems, units, number line diagram, liquid volume, capacity, masses, height, base        |   |                     |         |

| Generalizations<br>My students will <b>Understand</b> that  | Guiding Guiding   | Questions<br>Conceptual   |
|---|---|---|
| Standardized forms of measurement (e.g., for time, liquid<br>volume and mass) provide common terms/connotations<br>that facilitate mathematical communication and problem<br>solving (MA10-GR.3-S.4-GLE.3-EO.a)   | What are the differences between time, liquid volume<br>and mass?<br>What is a standard unit?   | Why do they need different types of measurement?<br>How do having standard units of measure help us?                                    |
| Although clocks (analog and digital) may have different<br>ways of representing and denoting the passage of time<br>they share a language of time increments (i.e., hours,<br>minutes and seconds) which facilitates their universality<br>(MA10-GR.3-S.4-GLE.3-EO.a.i, a.ii) | How do you read an analog clock to the nearest minute?<br>What do the revolutions of the second and minute<br>hands communicate?<br>How many minutes in an hour?<br>How many seconds in a minute? | Why are there five tick marks between each number on<br>an analog clock?<br>Why do we measure time? (MA10-GR.3-S.4-GLE.3-IQ.2)          |
| Solving elapsed time problems involves composing and decomposing units of hours, minutes and seconds and provides experience with a real-world number base system other than base-ten (MA10-GR.3-S.4-GLE.3-EO.a.iii)  | When do you regroup in problems involving time?<br>How can a number line diagram be used to solve<br>elapsed time problems?   | How are addition and subtraction problems about time<br>similar/different from addition and subtraction<br>problems not involving time? |

| Key Knowledge and S<br>My students will  | <b>kills:</b> What students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics samples what students should know and do are combined. |  |  |
|--|--|--|--|
| <ul> <li>Tell and write time to the nearest minute (MA10-GR.3-S.4-GLE.3-EO.a.i)</li> <li>Measure time intervals in minutes (MA10-GR.3-S.4-GLE.3-EO.a.ii)</li> <li>Solve word problems including elapsed time problems using addition and subtraction of time intervals in minutes using a number line diagram (MA10-GR.3-S.4-GLE.3-EO.a.iii)</li> <li>Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (I) (MA10-GR.3-S.4-GLE.3-EO.a.iv)</li> <li>Use models to add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units (MA10-GR.3-S.4-GLE.3-EO.a.v)</li> </ul> |  |  |  |
| Critical Language: includes the Academic and Technical vocabulary, semantics, and discourse which are particular to and necessary for accessing a given discipline.<br>EXAMPLE: A student in Language Arts can demonstrate the ability to apply and comprehend critical language through the following statement: "Mark Twain exposes the hypocrisy of slavery through the use of satire."   |  |  |  |
| A student in<br>ability to apply and comp<br>through the following sta   | can demonstrate the<br>rehend critical language<br>tement(s):  | I eat breakfast at 6:15 in the morning and I leave for school at 8:00 the amount of elapsed time from 6:15 to 8:00 is 1 hour and 45 minutes. I used an open number line diagram to solve this problem. |  |
| Academic Vocabulary:   | Veasure, estimate, model, hours, seconds, minutes, time  |  |  |
| Technical Vocabulary:  | Gram, kilogram, liter, liquid volume, mass, number line diagram, standard unit, elapsed time, units  |  |  |

| Unit Title                                     | Shape it Up! 2 weeks  |   | 2 weeks             |  |
|--|---|---|---------------------|--|
| Focusing Lens(es)                              | Relationship  | Standards and Grade<br>Level Expectations<br>Addressed in this Unit | MA10-GR.3-S.4-GLE.1 |  |
| Inquiry Questions<br>(Engaging-<br>Debatable): | Why do mathematicians use different terms to describe the same shape? (MA10-GR.3-S.4-GLE.1-IQ.2)  |   |                     |  |
| Unit Strands                                   | Geometry  |   |                     |  |
| Concepts                                       | Equipartitioning, partitioning, attributes, properties, unit fraction, quadrilaterals, categorization, shapes, sides, vertices, relationships, equivalent, length, parallel, perpendicular, angle, right angle, area, whole |   |                     |  |

| Generalizations   | Guiding Questions<br>Factual Conceptual   |  |
|---|---|--|
|   |   |  |
| Shapes in different categories typically share attributes that allow the creation and definition of larger categories (MA10-GR.3-S.4-GLE.1-EO.a.i)  | What attributes are typically used to categorize shapes?  | Why do we categorize shapes by their attributes?                 |
| Attributes (properties) of shapes include sides and vertices and the relationships among sides and vertices (MA10-GR.3-S.4-GLE.1-EO.a.i, a.i.1)   | What is a quadrilateral?<br>Which quadrilaterals have multiple names? How do you<br>know if a shape is a quadrilateral? | Why might a shape have multiple names?                           |
| Relationships between the sides and vertices of a shape typically highlight lengths (equivalent and non-equivalent) and lines (parallel or perpendicular) (MA10-GR.3-S.4-GLE.1-EO.a.i, a.i.1) | Which shapes have parallel sides?<br>Which shapes have square corners?  | How do parallel and perpendicular sides help to classify shapes? |
| Equipartitioning a shape creates equal areas which can<br>each be represented as a unit fraction (MA10-GR.3-S.4-<br>GLE.1-EO.a.ii)  | What is a unit fraction?<br>How do you represent an equal part of a shape using a<br>unit fraction?                     | Into how many parts can a shape be partitioned into evenly?      |

| Key Knowledge and Skills: | What students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics |
|---------------------------|---|
| My students will          | samples what students should know and do are combined.  |

- Understand shapes in different categories may share attributes and that shared attributes can define a larger category (MA10-GR.3-S.4-GLE.1-EO.a.i)
- Recognize rhombuses, rectangles, and squares as examples of quadrilaterals (MA10-GR.3-S.4-GLE.1-EO.a.i.1)
- Draw examples of quadrilaterals that do not belong to any of the subcategories of rhombuses, rectangles, and squares (MA10-GR.3-S.4-GLE.1-EO.a.i.1)
- Partition shapes into equal parts with equal areas and express the area of each part as a unit fraction of the whole (MA10-GR.3-S.4-GLE.1-EO.a.iii)

| A student in<br>ability to apply and comp<br>through the following sta | can demonstrate the<br>rehend critical language<br>tement(s):   | I partitioned this rectangle into four equal parts, and I know that each part is ¼ of the whole.<br>This rhombus is a quadrilateral because it is a shape with four sides.<br>I know this shape I drew is a quadrilateral because it has four sides. I know it's not a rhombus, rectangle or square,<br>because it doesn't share the attributes of those shapes. |
|--|---|--|
| Academic Vocabulary:   | Partition, identify, category, example, non-example, corner, length   |  |
| Technical Vocabulary:  | Quadrilateral (e.g., rhombuses, rectangles, and squares), attributes, unit fractions, area, angle, side, vertices, equal, parallel, perpendicular, right angle, whole |  |