

Colorado Student Assessment Program

Technical Report 2011

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TABLE OF CONTENTS

OVERVIEW	1
PART 1: STANDARDS	2
Reading and Writing.....	2
The Colorado Model Content Standards.....	2
The Colorado Model Subcontent Areas.....	2
Mathematics.....	3
The Colorado Model Content Standards.....	3
The Colorado Model Subcontent Areas.....	4
Science	6
The Colorado Model Content Standards.....	6
The Colorado Model Subcontent Areas.....	6
PART 2: TEST DEVELOPMENT.....	8
Test Development and Content Validity.....	8
Test Configuration.....	9
CSAP Content Validity and Alignment Review.....	9
Universal Design and Plain Language in the Colorado Student Assessment Program	10
Linking Item (Anchor Item) Selection for the 2010 Assessments.....	11
Items Flagged for Fit and DIF in Test Assembly	13
PART 3: ADMINISTRATION	15
Test Administration Training.....	16
Test Sections and Timing	16
PART 4: SCORING AND SCALING DESIGN.....	18
Test Scores for the Total Test and by Content Standard and Subcontent Area	18
Anchor Paper Review of New Constructed-Response Items	19
Rater Reliability and Severity	20
Interrater Reliability.....	20
Rater Severity/Leniency Study	21
Scaling Design	23

PART 5: ITEM ANALYSES24**Third Grade25**

Reading25

Reading – Spanish25

Writing26

Writing – Spanish26

Mathematics26

Fourth Grade27

Reading27

Reading – Spanish27

Writing28

Writing – Spanish28

Mathematics29

Fifth Grade29

Reading29

Writing30

Mathematics30

Science30

Sixth Grade31

Reading31

Writing31

Mathematics32

Seventh Grade32

Reading32

Writing32

Mathematics33

Eighth Grade33

Reading33

Writing34

Mathematics34

Science35

Ninth Grade35

Reading35

Writing35

Mathematics36

Tenth Grade36

Reading36

Writing37

Mathematics37

Science38

PART 6: CALIBRATION AND EQUATING39**Overview of the IRT Models39****Calibration of the Assessment40**

Model Fit Analyses	41
Model Fit Analyses Results	42
Third Grade.....	42
Fourth Grade.....	43
Fifth Grade.....	43
Sixth Grade.....	43
Seventh Grade.....	44
Eighth Grade.....	44
Ninth Grade	44
Tenth Grade	44
Item Local Independence.....	45
Evaluation of Item Analysis and Calibration.....	45
Equating Procedures	46
Anchor Items Evaluation Criteria	47
Anchor Items Evaluation Results	49
p-value Comparisons	49
Item Parameter Comparisons.....	49
Scaling Constants	50
Additional Analyses of Flagged Items.....	50
Effectiveness of the Equating.....	51
PART 7: SCALE SCORE SUMMARY STATISTICS.....	52
Scale Score Distributions: Student Results	53
Third Grade.....	53
Fourth Grade.....	56
Fifth Grade.....	58
Sixth Grade	61
Seventh Grade.....	62
Eighth Grade.....	64
Ninth Grade	66
Tenth Grade	68
Correlations among Content Standards and among Subcontent Areas.....	71
PART 8: RELIABILITY AND VALIDITY EVIDENCE.....	72
Total Test and Subgroup Reliability.....	72
Interrater Reliability, Item-to-Total Score Correlation, and DIF.....	74
Standard Error of Measurement	75
Test Validity	76
Content-Related Validity	76
Construct Validity	77
Minimization of Construct-Irrelevant Variance and Under-Representation.....	77

Minimizing Bias through DIF Analyses	78
Linn–Harnisch DIF Method.....	80
Differential Item Functioning Ratings and Results	81
Internal Factor Structure and Unidimensionality of the CSAP Assessment.....	83
IRT Model to Data Fit as an Evidence of Test Score Validity	83
Divergent (Discriminant) Validity.....	84
Predictive Validity	84
Classification Consistency and Accuracy	85
Classification Consistency and Accuracy When Pattern Scoring Is Used	86
PART 9: SPECIAL STUDY	89
Writing Trend Study	89
REFERENCES	91
TABLES.....	94
FIGURES	504
APPENDIX: Criteria for Item Acceptability	

Overview

This report presents the results of the statewide spring 2011 administration of the Colorado Student Assessment Program (CSAP). In the spring of 2011, students in grades 3 through 10 were assessed in Reading, Writing, and Mathematics, and students in grades 5, 8, and 10 were also assessed in Science. Spanish versions of Reading and Writing tests were also administered in grades 3 and 4. The assessments were developed by CTB/McGraw-Hill, LLC in collaboration with the Colorado Department of Education and were scored and scaled by CTB/McGraw-Hill.

This report is organized in parts. Part 1 provides an overview of the CSAP assessments, including descriptions of content standards and subcontent areas. Part 2 includes descriptions of test development, content validity, test configuration, and differential item functioning (DIF) and fit in test assembly. Part 3 details test administration. Part 4 describes the scoring and scaling design (including descriptions of scoring and scaling procedures for the total test and for individual content standards and subcontent areas), as well as interrater reliability and rater severity/leniency. Part 5 includes detailed item analysis results, including item-to-total score correlations, p -values, and omit rates. Part 6 describes the calibration and equating results, including an overview of the Item Response Theory (IRT) models, model-to-data fit, item independence, and equating procedures. Part 7 presents scale score summary statistics and correlations among content standards and subcontent areas. Part 8 contains reliability and validity evidence, including total and subgroup reliability, test validity, content- and construct-related validity, and minimization of construct irrelevance variance and under-representation. Finally, Part 9 presents the Writing subscale trends for paragraph and extended writing.

Part 1: Standards

The CSAP assessments are developed to measure the Colorado content standards. Note that the terms “content standard” and “standard” are used synonymously throughout the text. Beginning in 2001, subcontent reporting categories were added at the request of the Colorado Department of Education to provide additional diagnostic information. Each subcontent area may cover several content standards. Some items in CSAP are mapped to a subcontent area, whereas all items are mapped to one, and only one, content standard. The various content standards and subcontent areas are listed below for each content area. Table 1 provides an overview of which content standards and subcontent areas are assessed in each of the grades.

Reading and Writing

The Colorado Model Content Standards

- 1) Reading Comprehension – Students read and understand a variety of materials. (Reading)
- 2) Write for a Variety of Purposes – Students write and speak for a variety of purposes and audiences. (Writing)
- 3) Write Using Conventions – Students write and speak using conventional grammar, usage, sentence structure, punctuation, capitalization, and spelling. (Writing)
- 4) Thinking Skills – Students apply thinking skills to reading, writing, speaking, listening, and viewing. (Reading)
- 5) Use of Literary Information – Students read to locate, select, and make use of relevant information from a variety of media, reference, and technology source materials. (Reading)
- 6) Literature – Students read and recognize literature as a record of human experience. (Reading)

The Colorado Model Subcontent Areas

- 1) Fiction – Students read, predict, summarize, comprehend, and analyze fictional texts; determine the main idea and locate relevant information; and respond to literature that represents different points of view. (Reading)

- 2) Nonfiction – Students read, predict, summarize, comprehend, and analyze a variety of nonfiction texts, including newspaper articles, biographies, and technical writings; locate the main idea and select relevant information; and determine the sequence of steps in technical writings. (Reading)
- 3) Vocabulary – Students use word recognition skills and resources such as phonics, context clues, word origins, and word order clues; root prefixes and suffixes of words. (Reading)
- 4) Poetry – Students read, predict, summarize, and comprehend poetry; determine the main idea, make inferences, and draw conclusions; and respond to poetry that represents different points of view. (Reading)
- 5) Paragraph Writing – Students write and edit in a single session. (Writing)
- 6) Extended Writing – Students plan, organize, and revise writing for an extended essay. (Writing)
- 7) Grammar and Usage – Students know and use correct grammar in writing, including parts of speech, pronouns, conventions, modifiers, sentence structure, and agreement. (Writing)
- 8) Mechanics – Students know and use conventions correctly including spelling, capitalization, and punctuation. (Writing)

Mathematics

The Colorado Model Content Standards

- 1) Number Sense – Students develop number sense, use numbers and number relationships in problem-solving situations, and communicate the reasoning used in solving these problems.
- 2) Algebra, Patterns, and Functions – Students use algebraic methods to explore, model, and describe patterns and functions involving numbers, shapes, data, and graphs in problem-solving situations and communicate the reasoning used in solving these problems.
- 3) Statistics and Probability – Students use data collection and analysis, statistics, and probability in problem-solving situations and communicate the reasoning used in solving these problems.
- 4) Geometry – Students use geometric concepts, properties, and relationships in problem-solving situations and communicate the reasoning used in solving these problems.

- 5) Measurement – Students use a variety of tools and techniques to measure, apply the results in problem-solving situations, and communicate the reasoning used in solving these problems.
- 6) Computational Techniques – Students link concepts and procedures as they develop and use computational techniques including estimation, mental arithmetic, paper and pencil, calculators, and computers in problem-solving situations, and communicate the reasoning used in solving these problems.

The Colorado Model Subcontent Areas

1) Subcontent Area 1 (Varies by Grade).

- Number and Operation Sense (Grades 4 and 5) – Students demonstrate meanings for whole numbers, commonly used fractions, decimals, and the four basic arithmetic operations through the use of drawings, and decomposing and composing numbers; and identify factors, multiples, and prime/composite numbers.
- Number and Operation Sense (Grade 6) – Students demonstrate an understanding of relationships among benchmark fractions, decimals, and percents and justify the reasoning used. Students add and subtract fractions and decimals in problem-solving solutions. (SA 1, grade 6)
- Number Sense (Grade 7) – Students demonstrate understanding of the concept of equivalency as related to fractions, decimals, and percents.
- Linear Pattern Representation (Grade 8) – Students represent, describe, and analyze linear patterns using tables, graphs, verbal rules, and standard algebraic notation and solve simple linear equations in problem-solving situations using a variety of methods.
- Multiple Representations of Linear/Nonlinear Functions (Grade 9) – Students represent linear and nonlinear functional relationships modeling real-world phenomena using written explanations, tables, equations, and graphs; describe the connections among these representations; and convert from one representation to another.
- Multiple Representations of Functions (Grade 10) – Students represent functional relationships that model real-world phenomena using written explanations, tables, equations, and graphs; describe the connections among these representations; and convert from one representation to another.

2) Subcontent Area 2 (Varies by Grade).

- Patterns (Grade 4) – Students reproduce, extend, create, and describe geometric and numeric patterns as problem-solving tools.
- Patterns (Grade 5) – Students represent, describe, and analyze geometric and numeric patterns using tables, graphs, and verbal rules as problem-solving tools.
- Patterns (Grade 6) – Students represent, describe, and analyze geometric and numeric patterns using tables, words, concrete objects, and pictures in problem-solving situations.
- Area and Perimeter Relationships (Grade 7) – Students demonstrate an understanding of perimeter, circumference, and area and recognize the relationships between them.
- Proportional Thinking (Grade 8) – Students apply the concepts of ratio, proportion, scale factor, and similarity, including using the relationships among fractions, decimals, and percents in problem-solving situations.
- Proportional Thinking (Grade 9) – Students apply the concepts of ratio and proportion in problem-solving situations.
- Probability and Counting Techniques (Grade 10) – Students apply organized counting techniques to determine a sample space and the theoretical probability of an identified event which includes differentiating between independent and dependent events and using area models to determine probability.

3) Subcontent Area 3 (Varies by Grade).

- Measurement (Grade 4) – Students demonstrate knowledge of time, and understand the structure and use of U.S. customary and metric measurement tools and units.
- Data Display (Grade 5) – Students organize, construct, and interpret displays of data, including tables, charts, pictographs, line plots, bar graphs, and line graphs, and choose the correct graph from possible graph representations of a given scenario.
- Geometry (Grade 6) – Students reason informally about the properties of two-dimensional figures and solve problems involving area and perimeter.

- Geometry (Grade 8) – Students describe, analyze, and reason informally about the properties of two- and three-dimensional figures to solve problems.

Science

The Colorado Model Content Standards

- 1) Scientific Investigation – Students apply the processes of scientific investigation and design, conduct, communicate about, and evaluate such investigations.
- 2) Physical Science – Students know and understand common properties, forms, and changes in matter and energy. (*Focus: Physics and Chemistry*)
- 3) Life Science – Students know and understand the characteristics and structure of living things, the processes of life, and how living things interact with each other and their environment. (*Focus: Biology – Anatomy, Physiology, Botany, Zoology, Ecology*)
- 4) Earth and Space Science – Students know and understand the processes and interactions of Earth's systems and the structure and dynamics of Earth and other objects in space. (*Focus: Geology, Meteorology, Astronomy, Oceanography*)
- 5) The Nature of Science – Students understand that the nature of science involves a particular way of building knowledge and making meaning of the natural world.

The Colorado Model Subcontent Areas

- 1) Experimental Design and Investigations – Students design, plan, and conduct a variety of investigations; understand and apply scientific questions, hypotheses, variables, and experimental design.
- 2) Results and Data Analysis – Students select and use appropriate technology; organize, analyze, interpret, and predict from scientific data in order to communicate the results of investigations.
- 3) Physics Concepts – Students understand physical forces, the motion of objects, and energy transfer or energy transformation.
- 4) Chemistry Concepts – Students understand the properties, composition, structure, and changes of matter.
- 5) Life Process – Students understand levels of organization in organisms, cellular structure and processes, and concepts in heredity.

- 6) Geology and Astronomy – Students understand Earth's composition, energy resources, plate movement, and characteristics of different celestial objects in the universe and how they interact with one another.

Part 2: Test Development

Content-related validity in achievement tests is evidenced by a correspondence between test content and a specification of the content domain. Content-related validity can be demonstrated through consistent adherence to test blueprints and through a high-quality test development process that includes review of items for accessibility by various subgroups, including English Language Learners and students with disabilities. Part 2 provides an overview of the CSAP test design and the development of student assessments that assist stakeholders in making informed educational decisions. Specifically, it describes the CSAP test development activities in terms of content validity; test configuration; content revision in terms of sensitivity, bias, and plain language; selection of linking items for maintaining scales; model-to-data fit; and differential item functioning (DIF) in 2011 assessments.

Test Development and Content Validity

Content-related validity can be defined as the degree to which elements of an assessment instrument are relevant to and representative of the targeted construct for a particular assessment purpose. In order to ensure the content-related validity of the CSAP assessments, the Colorado Model Content Standards and Assessment Frameworks were studied by CTB's content developers, who worked with Colorado content-area specialists, teachers, and assessment experts to develop a pool of items that measured Colorado's Assessment Frameworks in each grade and content area. Several sources contributed to the 2011 CSAP items. CTB/McGraw-Hill's extensive pool of previously field-tested Reading passages, Writing prompts, Mathematics, and Science items provided the initial source. Many of these existing items were revised in order to ensure accessibility by different student groups and better measurement of the relevant Colorado standards and benchmarks. Additional items were developed by CTB and the staff at the Colorado Department of Education as needed to complete the alignment of CSAP to the Assessment Frameworks. These items were carefully reviewed under plain language revision and discussed by Content Validity and Alignment Review committees to ensure not only content validity and alignment to Colorado Standards but also the quality and appropriateness of the items. These committees represented Colorado's diverse population and included Colorado teachers, community members, and State Department of Education staff. The committees' recommendations were used to select and/or revise items from the item pool to construct the final Reading, Writing, Mathematics, and Science assessments.

Each new form also included a subset of multiple-choice items used in the previous administrations of the CSAP assessments as an anchor set. These repeated items were used to equate the forms across years. Equating is

necessary to account for slight year-to-year differences in test difficulty and to maintain scale comparability across years. Details of the equating process are provided later in Part 6 of this report. The assessments that are reported on vertical scales (English Reading, English Writing, and Mathematics) also had items in common between adjacent grades. In grades 3 and 4, the 2011 Spanish Reading and Writing test forms were the same forms that had been administered in previous administrations.

Test Configuration

Tables 2 through 6 provide information regarding the configuration of the CSAP assessments. Table 2 provides the number of multiple-choice (MC) and constructed-response (CR) items on each test, as well as the number of obtainable score points on each CR item. Tables 3 through 6 provide the number of MC and CR items by content standard (CS) and subcontent area (SA). Note that the subcontent areas Fiction (SA 1) and Poetry (SA 4) are combined for grades 3 through 6 Reading. The following content standards are also combined: Algebra, Patterns, and Functions (CS 2) and Statistics and Probability (CS 3) in grade 3 Mathematics; Number Sense (CS 1) and Computational Techniques (CS 6) in grades 7 through 10 Mathematics; Geometry (CS 4) and Measurement (CS 5) in grades 3 through 10 Mathematics; and Scientific Investigation (CS 1) and the Nature of Science (CS 5) in grades 5, 8, and 10 Science.

Every item is associated with a content standard, but not all items are associated with a subcontent area. For this reason, the sum of the subcontent area points is less than the total number of points for the test.

Tables 7 and 8 provide the Depth of Knowledge (DOK) level distribution for the 2011 CSAP assessments. DOK distribution will be articulated in the blueprint for the 2011 CSAP assessments.

CSAP Content Validity and Alignment Review

The items that appeared in 2011 CSAP tests were carefully reviewed and discussed in June 2010 by Content Validity and Alignment Review committees to ensure content validity, accurate alignment to content standards, and the quality and appropriateness of the items. Included was a review for bias and sensitivity issues. These committees represented Colorado's diverse population and included Colorado teachers, community members, and State Department of Education staff.

Specific areas of focus of the content review committees included the following:

- alignment of items to assessment objectives under the Colorado Model Content Standards, the Assessment Frameworks, and Depth of Knowledge
- accuracy and grade-level appropriateness of items
- accessibility of items to all Colorado students, using Universal Design and Plain Language principles
- appropriateness and usability of scoring guides for constructed-response items.

Processes for alignment review were designed to ensure that

- reviews resulted in an independent alignment recommendation by each reviewer
- thorough discussion of appropriate alignment occurred following the independent reviews; and
- thorough documentation of alignment findings was captured.

Processes for bias and sensitivity review were designed to ensure that

- items were neither advantageous nor disadvantageous to a specific group of students
- items did not stereotype specific groups
- items did not promote personal, moral, or religious values or viewpoints; and
- students' achievement on a given test item would be dependent solely on what they know and are able to do.

The committees' feedback was reconciled by CDE and CTB staff and used to select and/or revise items from the item pool to construct the final Reading, Writing, Mathematics, and Science assessments.

Universal Design and Plain Language in the Colorado Student Assessment Program

As indicated in the previous section, one purpose of the CSAP content review was the application of Universal Design in test assembly. The CSAP measures what students know and are able to do as defined in the Colorado Model Content Standards. Assessment must ensure comprehensible access to this content. CDE's and CTB's content experts revised the item pool and removed

unnecessary verbiage from the 2011 CSAP tests so that students could show what they know and are able to do. Areas of focus included directions, writing prompts, test questions, and answer choices. New items developed for 2011 were authored using these principles. Items previously developed and administered prior to 2011 were also modified to conform to these principles.

Aspects of Universal Design

- ☐ Precisely Defined Constructs
 - Direct match to objective being measured
- ☐ Accessible, Nonbiased Items
 - Ensure ability to use accommodations from the start (Braille, oral presentation)
 - Ensure that quality is retained in all items
- ☐ Simple, Clear Directions and Procedures
 - Presented in understandable language
 - Consistency in procedures and format in all content areas
- ☐ Maximum Legibility
 - Simple fonts
 - Use of white space
 - Headings and graphic arrangement
 - Direct attention to relative importance
 - Direct attention to the order in which content should be considered
- ☐ Maximum Readability: Plain Language
 - The use of Plain Language in CSAP
 - Increases validity to the measurement of the construct
 - Increases the accuracy of the inferences made from the resulting data
 - Plain Language in CSAP uses
 - Active instead of passive voice
 - Short sentences
 - Common, everyday words
 - Purposeful graphics to clarify what is being asked

Linking Item (Anchor Item) Selection for the 2010 Assessments

In order to equate current tests to base year scale, a set of previously administered multiple-choice anchor items was selected for each of the 2011 assessments in Reading, Writing, Mathematics, and Science. These items demonstrated good classical and IRT statistics and represented the test blueprint. Equating is necessary to account for slight differences in test difficulty and maintain scale comparability across administrations. Details of the equating process are provided in Part 6.

The following criteria were followed to select anchor items in Reading, Writing, Mathematics, and Science:¹

Content Representation and Item Difficulty – Content representation is one of the two most important criteria for anchor item selection. The items in an anchor set should represent a miniature version of the form. The other critical criterion is the spread of item difficulties across the difficulty range of the test. The item difficulty values for anchor items should cover the item difficulty range in the test but generally should *not* include extremely easy ($p > 0.90$) or extremely difficult ($p < 0.25$) items. However, a recent study by Sinharay and Holland (2007) indicated that the anchor set difficulty range mirroring the complete form is not necessarily optimal. In any case, one way to think of selecting anchor items is to select “the best items” in the pool.

Number of Anchor Items and Item Format Representation – The 2011 CSAP tests included 13 to 25 anchor items for each grade and content area. Only multiple-choice items were selected as anchors.² For anchor items associated with a passage, all items originally included with the passage were readministered. The length of the passage associated with the anchor items was not extreme relative to the length of other passages in the form.

Relative Item Position in a Form – Anchor items were placed in approximately the same relative position in the form as they were previously administered. The position of items can affect their performance. For this reason, the position of each anchor item on the new form was as close as possible to its position on the form in which it appeared previously (in most cases within 6 positions). A minimum requirement was that they be placed in the same third of the form that they appeared in when they were previously administered. Similarly, it was required that the item sets (testlets) with common stimuli be placed on the same side of the two open pages.

It was also required that the anchor items be interspersed throughout the test, not placed at the very beginning or end of a form or session, or in any locations where speededness effects may occur.

Item Characteristics – Content experts *avoided* using items in the anchor sets with

- Point biserials ≤ 0.18 for the correct answer

¹ The 2011 Spanish tests for grades 3 and 4 Reading and Writing were identical to the tests that were administered in previous years. For this reason, and because of the small number of students taking these tests, the Spanish tests were scored using the same item parameters that were used to score the tests in 2010.

² When only MC items are used as anchors, it is assumed that the CR items do not measure a significant performance characteristic unique to that item format. Excluding CR items prevents equating error that could occur if raters varied in severity from year to year.

- Positive point biserials for the distractors
- $p\text{-value} \leq 0.25$ or ≥ 0.90
- Omit rates $\geq 5\%$

For all items, content experts *minimized* the use of items with poor fit statistics (Q1) or significant differential item functioning (DIF) statistics for gender or ethnicity. If it was essential to include an item with DIF, counterbalancing was suggested with an item exhibiting bias in the opposite direction. The number of items flagged for poor fit and DIF in 2011 tests are listed and described later in this section, under the heading “Items Flagged for Fit and DIF in Test Assembly.”

Form Characteristics – The test characteristic curves (TCCs) and standard error (SE) curves of the total test and the anchor set overlaid each other as closely as possible. Since only MC items were used as anchors and the test consisted of both MC and CR items, the alignment of the TCCs was difficult for some grades/content areas. In that situation, content developers attempted to match the anchor item TCC with the TCC for all of the MC items on the test. The maximum expected percent difference between TCCs was expected to be less than 0.05. In case this could not be met, content experts met this criterion at cut points. For tests that were vertically scaled, the TCC was sequentially aligned as the grade level increased.³

Items Flagged for Fit and DIF in Test Assembly

The items flagged for poor fit and DIF were avoided as much as possible when assembling the 2011 assessments. As a guideline, if it was essential to include an item with poor fit in the test in order to meet the test blueprint, it was to be with only marginally poor fit, with $p\text{-value}$ and item-to-total score correlation in a reasonable range. Similarly, if it was essential to include an item with DIF, content experts were instructed to minimize overall bias by counterbalancing with an item exhibiting bias in the opposite direction. Moreover, prior to including the item(s) flagged for DIF in the final forms, items were reviewed and judged to be fair by educational community professionals who represent various ethnic groups.

Table 9 displays the items with DIF and fit flags from previous administrations across all operational items for the 2011 assembled test forms. For the 1,042 operational English items with available statistics on the CSAP Mathematics, Reading, Writing, and Science assessments, 28 (2.7%) were flagged for marginal poor fit and 43 (4.1%) for DIF for gender and ethnic subgroups. Only 2 of these items were used as anchors in 2011.

³ Some overlap at either the top or bottom end of the TCCs may be permissible. However, a significant overlap in the middle portion is not allowed.

Of the 216 previously used Spanish items, 52 (24.1%) were flagged in a previous administration for marginal poor fit and 1 was flagged for gender DIF.⁴

Most of the flagged Spanish items were on the grade 4 Reading and Writing assessments (24 and 18 items, respectively), with very few items flagged in grade 3 (3 Reading items and 3 Writing items). As mentioned above, the poor fit was marginal for most items, and their inclusion in the tests was essential to meet the test blueprint for content standards.

⁴ Because of the very small number of students taking the Spanish assessments each year, the same test forms are readministered each year and it is not feasible to replace items or create new test forms. DIF statistics for the Spanish tests were not computed after 2008 because of the very small case counts.

Part 3: Administration

The Colorado Student Assessment Program (CSAP) is Colorado's large-scale standardized paper-and-pencil achievement test administered every year. In 2011, grade 3 Reading (English and Spanish) assessments were administered between February 7 and March 4. The rest of the English language tests, plus the grade 4 Spanish Reading and grades 3 and 4 Spanish Writing tests, were administered between February 28 and April 15. The purpose of the CSAP is to provide an annual measure of student performance relative to the Colorado Model Content Standards. All CSAP forms are timed, standardized assessments administered under standardized conditions to ensure the reliability and validity of the test results. All students in grades 3 through 10 for Reading/Writing and Mathematics and grades 5, 8, and 10 for Science were tested with a single form for each grade. The following accommodations were allowed to students on the basis of demonstrated need.

- 1 = Braille version
- 2 = Large-print version
- 3 = Teacher-read directions only
- 4 = Use of manipulatives (Not applicable to Reading and Writing)
- 5 = Scribe
- 6 = Signing
- 7 = Assistive communication device
- 8 = Extended timing used
- 9 = Oral script (Not applicable to Reading)
- A = Approved nonstandard accommodation
- B = Translated oral script (Not applicable to Reading)
- C = Word-to-Word dictionary (Not applicable to Reading)

Prior to test administration, accommodation requests were documented in a formal plan created for each individual student by a team of teaching professionals, with input from parents. The accommodations provided students equal opportunity to access information and demonstrate knowledge and skills without affecting the reliability and validity of the assessment. For detailed information regarding the test administration or accommodations, please refer to the 2011 test administration manual and the Colorado accommodations manual (Colorado Department of Education, 2011.)

The following sections briefly describe the training conducted before the test administration to ensure proper handling of test materials, test administration, and the secure return of materials to the scoring center. That information is followed by the number of sessions in each test and the time given to complete the test.

Test Administration Training

Prior to the actual testing window, CDE, with support from CTB, conducted pretest administration training for the 2011 CSAP. The live training consisted of an overview of CDE policies and procedures for the administration of the CSAP tests. Training included proper use of the CSAP Test Proctor's manuals and the District Assessment Coordinator/School Assessment Coordinator (DAC/SAC) manuals.

The Test Proctor's manuals provided specific instruction on proper administration of the CSAP tests. The manuals provided detailed definitions of the CSAP test proctors' responsibilities, the purpose of the test, security before and during the test, and chain-of-custody guidance to ensure that all students took the tests in a standardized manner (same time, same test, with no student interaction). The manuals also provided a list of authorized materials required for testing. Prior to test administration, the CSAP test proctors were responsible for ensuring that an adequate supply of the materials required for testing would be available in testing rooms.

The DAC/SAC manuals provided instruction to the District Assessment Coordinator and the School Assessment Coordinator on how to distribute, safeguard, collect, package, and ship the completed test books to CTB for scoring. Test administrators were instructed to return all test books (both used and unused) to CTB.

CDE scheduled and conducted regional test administration training sessions. The attendees at these sessions were district assessment coordinators and administrators. CDE stressed policy and procedure guidance as well as test administration training during these sessions. District and school assessment coordinators were required to provide training to all test proctors.

The CSAP Test Proctor's manual and the CSAP DAC/SAC manual can be found at www.ctb.com/csap.

Test Sections and Timing

Although the 2011 CSAP tests were administered independently, the CSAP Reading and Writing tests were combined in a single test book for grades 4 through 10 with six sections: three sections for Reading and three for Writing. Grade 3 Reading and Writing tests were not combined into one booklet (for both English and Spanish versions) as they were administered at separate times of the year. In grade 3 there were two sections for Reading and two for Writing. Similarly, there were two sections each for grade 3 Spanish Reading and Writing and three sections each for grade 4 Spanish Reading and Writing. For

Mathematics, there were three sections for grades 4 through 10 tests and two sections for the grade 3 test. For Science, grades 5, 8, and 10 each had three sections.

Test developers also considered speededness in the development of the CSAP assessments. CTB believes that achievement tests should not be speeded; little or no useful instructional information can be obtained from the fact that a student did not finish a test, whereas a great deal can be learned from student responses to questions. In the CSAP tests, students were allowed a maximum of 60 minutes for each session in Reading/Writing and 65 minutes in Mathematics and Science. The analysis of omit rates of the items showed no indication of speededness in the CSAP assessments. See Part 5 for further details on omit ranges.

Part 4: Scoring and Scaling Design

Part 4 describes scoring procedures for the total test, followed by scoring of constructed-response (CR) items. The succeeding sections describe rater reliability and rater severity. Finally, Part 4 wraps up with a detailed description of the scaling design for the 2011 CSAP assessments.

Test Scores for the Total Test and by Content Standard and Subcontent Area

In the CSAP tests, students' total scores are based on their performance on all the scored items on the test. The range of possible scores varies by grade and content area. The lowest obtainable scale score (LOSS) and highest obtainable scale score (HOSS) for each grade and content area is provided in Table 10. CSAP reports item pattern scores and the HOSS increases from grade to grade to allow students' growth to be reflected in the subsequent administrations. The HOSS for grade 3 Reading is markedly different from those for grades 4 through 10 because grade 3 responses were scaled separately when the scale was set, and grade 3 scores were reported earlier than the rest of the grades. The same LOSS and HOSS are maintained over the years in all grades and content areas; however, the Science grades' LOSS/HOSS changed in 2008. Students also receive a score for each content standard (and for each subcontent area) that is based only on the items that contribute to the given content standard (or subcontent area). Note that every item on the test corresponds to a content standard, but not all items contribute to a subcontent area. The scale scores for the content standards and the subcontent areas are calculated using the item parameters that are obtained when the *total* test is calibrated (see Part 6). For each grade and content area, the minimum and maximum possible scale scores for content standards and subcontent areas are set at the same LOSS and HOSS as the total scale score.

Students were scored at the total test, content standard, and subcontent area levels using an item response theory (IRT) item-pattern (IP) scoring procedure. This procedure produces maximum likelihood trait estimates (scale scores) based on students' item response patterns, as described by Lord (1974, 1980, pp. 179–181). Pattern scoring, based on IRT, takes into account which items a student answered correctly and produces better test information, less measurement error, and greater reliability than number-correct scoring. Moreover, pattern scoring produces more accurate scores for individual students. On average, the increase in accuracy is equivalent to approximately a 15% to 20% increase in test length (Yen, 1984; Yen & Candell, 1991). Note that score reliability tends to increase with the number of items, and thus the total score is more reliable than the content standard or subcontent area scores.

Anchor Paper Review of New Constructed-Response Items

CDE and CTB conducted an “anchor paper” (also called “range finding”) review of new constructed-response (CR) items on the 2011 CSAP tests. CTB’s handscoring supervisors reviewed approximately 300 to 1,000 student written responses to each of the CR items, drawn from the entire set of responses that were available at that time.⁵ Using scoring guides and rubrics prepared by CTB’s content developers, CTB’s supervisors selected responses that they determined were representative of students who demonstrated various levels of proficiency and understanding of the concepts being assessed. Supervisors annotated the sample anchor papers with their comments and logic for assigning scores.

The handscoring supervisors also reviewed anchor papers for CR items that were used in previous years’ versions of the tests. If items were revised or if there was reason to believe that a review should be conducted to obtain fresh anchor papers, the supervisors included sample anchor papers in the review package.

CTB’s handscoring supervisors prepared anchor paper review packets for the various grades and contents to be reviewed with Colorado teachers at a live session in Denver, Colorado, in April 2011.

At the 2011 CSAP anchor paper review, CTB’s supervisors distributed numbered packets containing the established scoring guide and the proposed and annotated anchors for all new items in 2011.

CTB’s supervisors led discussion of each proposed, annotated anchor paper for each reviewed CR item, beginning with the top score point and continuing in reverse order to the lowest score point. Annotations were amended when necessary so that they more closely reflected the teacher-informed scoring stance for the item.

The review participants approved the proposed anchors or selected an alternative anchor for all items reviewed. A Colorado participant, appointed by a CDE consultant, verified the approval of the anchor by signing and dating a copy of each anchor. In the event that one or more anchors for that item were deemed ineffective, participants chose from other sample responses for a replacement. CTB’s supervisor, if appropriate, suggested other student responses from additional materials brought to the review.

After the committee of teachers reviewed and approved the scores and annotations of the anchors, members continued to review additional responses that the supervisor deemed questionable. The approved score, as well as a brief

⁵While this process did limit the selection to those districts that delivered their materials in time to be included in the sample, there was no attempt to include, exclude, or weight the participation of any particular districts in the sample.

synopsis of the scoring philosophy behind the decision, was recorded by CTB's supervisor.

The reviewed and annotated anchor papers served as the basis for conducting handscoring training for the 2011 CSAP at a CTB scoring facility.

Rater Reliability and Severity

The CSAP test design framework includes a variety of different item types, including short response and extended constructed-response items. Although constructed-response items greatly enhance the construct and instructional validity of the CSAP, reliability of handscoring items should be closely examined and documented. Through the ongoing process of training and research analyses, evidence of the reliability of handscoring was continuously gathered. Many training and monitoring techniques were used to ensure handscoring reliability and accuracy. Scoring guides were carefully developed and refined; scorers were trained, calibrated, and monitored throughout the scoring process; and rater reliability indices were generated and examined. Reliability for constructed-response items was typically examined by calculating indices of interrater agreement—the reliability with which human raters assign scores to student responses. For this analysis, a certain percentage of student responses are scored by two raters.

Interrater Reliability

To measure interrater reliability *within* the 2011 CSAP administration, approximately 5% of the constructed-response items scored were given a blind double read (i.e., were read by a second reader), and the resulting scores were documented and analyzed. In each case, the response was randomly assigned to a second reader selected at random from among all readers other than the reader who had provided the first score. The second reader was not aware that this was a second read. For Spanish, approximately 15% of the constructed-response items were a blind double read. Evidence supporting interrater reliability of the CSAP assessments is presented in terms of raw score means, raw score standard deviations, and percentages of exact and adjacent agreement between raters. Exact agreement is defined as scores that are exactly the same. Adjacent agreement is defined as scores differing by one point. In addition, Cohen's kappa (Cohen, 1960) is provided as a measure of agreement between the raters and is commonly used to summarize the agreement between raters. It is computed as (Brennan & Prediger, 1981)

$$\kappa = \frac{\sum P_{ii} - \sum P_{i \cdot} P_{\cdot i}}{1 - \sum P_{i \cdot} P_{\cdot i}},$$

where $\sum P_{ii}$ is the observed proportion of agreement and $\sum P_{i \cdot} P_{\cdot i}$ is the chance proportion of agreement.⁶ Tables 11 through 16 show the rater reliability indices for all constructed-response items by content area. The results indicate that the kappa is reasonably high for all grades and content areas.

Rater Severity/Leniency Study

In addition to examining rater reliability measures within a given administration year, CTB conducts a rater severity study *across* years. Rater severity or leniency is defined as the extent to which scores assigned by raters across years are systematically higher or lower than the scores that would be assigned by an ideal group of objective and unbiased raters. The study entails sampling student responses from previous administrations, having a representative group of raters from the current administration score them, and comparing the scores against the scores assigned by the previous raters. Table 17 shows the number of rater severity/leniency items used in the study by content area and grade. The following specifications describe the rater severity study in detail:

- 1) In 2011, a rater severity study was done using constructed-response items that were repeated from 2009 or 2010. Random samples of student responses were selected from the CSAP tests in which these repeated items were present: A random sample of approximately 1,000 students was selected for English Reading, English Writing, Mathematics, and Science assessments.
- 2) The samples of papers were distributed blindly to the 2011 raters during the second half of 2011 operational scoring; that is, the raters scoring the papers from a previous administration ideally knew neither that the papers had been scored before, nor that they came from a previous test administration. The items to be rescored were shown to the 2011 raters under their 2011 item numbers (see Table 17).
- 3) The scores from the rescore were then compared with the original scores given to the papers by the raters in 2009 or 2010.

Table 17 shows results of the rater severity study, including mean scores from the previous administration; mean scores from the 2011 administration; percent of the scores with exact, adjacent, and discrepant agreement; correlation; intraclass correlation; and weighted kappa.

⁶ The observed proportion of agreement is computed by summing the proportion of agreement across cells; the chance agreement proportion is computed by summing the products of the column and row proportions.

Weighted kappa, which may be interpreted as the chance-corrected weighted proportional agreement, is reasonably high for the items in all content areas (0.56 to 0.92 with median of 0.85 for Reading; 0.67 to 0.75 with median of 0.72 for Writing; 0.73 to 0.98 with median of 0.86 for Mathematics; and 0.65 to 0.85 with median of 0.76 for Science).

Scaling Design

Horizontal equating within each grade was used to place the 2011 forms on the scales that were established previously for English Reading, Writing, Mathematics, and Science, using Stocking and Lord's (1983) procedure. The vertical scale for English Reading, spanning grades 4 through 10, was established in 2001. The grade 3 reading assessment is sufficiently different from the reading assessments in the higher grades (it assesses only one content standard, whereas the other assessments assess multiple content standards) to warrant it to be treated separately. The vertical scales for English Writing, spanning grades 3 through 10, and for Mathematics, spanning grades 5 through 10, were established in 2002. Grades 3 and 4 Mathematics were added to the vertical scale in 2005. Grades 5, 8, and 10 Science were placed on scale in 2008. Because of the nonincremental nature of the content standards and the gaps in grade levels, grades 5, 8, and 10 Science were not placed on a vertical scale.

Although the Spanish Reading and Writing tests in grades 3 and 4 are designed to measure a student's development over time, they were built from CTB's Supera assessments and are not on a vertical scale. Note that the customized versions of the grades 3 and 4 Reading and Writing assessments in Spanish were first administered in 1998.⁷ The customized Spanish version that was first created in 1998 was repeated without modification through 2001. From 2002 through 2006, new Spanish forms were created by selecting psychometrically sound items from the existing item pool. The 2007 assessments were reprints of 2006, with the exception of a few select items. Because the numbers of students taking these tests are very small, the same Spanish test forms were readministered in 2008, 2009, 2010 and 2011, and the 2011 tests were scored using the same pre-equated item parameters that were used to score these tests in previous years.

With the exception of the Spanish Reading and Writing tests, each of the new 2011 CSAP tests contained a set of preselected multiple-choice items⁸ from a previous administration for the same grade. These repeated multiple-choice items served as anchors in Stocking and Lord's (1983) equating procedure, which was used to place each test form on the previously established scale. By equating the 2011 CSAP tests across years within each grade, the unique metrics of the CSAP scales were maintained. The scaling and calibration methods are presented in Part 6 of this report.

⁷ In 1997, Supera had been administered to CSAP students who were eligible to take a Spanish language version of the assessment.

⁸ As noted previously in this report, the exclusion of constructed-response items from the anchor set eliminates the possibility of systematic equating error that might otherwise occur if there were shifts in rater severity across administrations.

Part 5: Item Analyses

All students who participated in the operational administration were scored. For the item analyses and calibration samples, however, student responses from the following categories were excluded as a part of the valid attempt rules:

- Students who were absent when any items assessing a scale were administered, and those with multiple marks.
- Students who had invalidation flags.
- Students who had the following special accommodation codes:
 - 1) For Reading no special accommodation codes were excluded
 - 2) For Writing scribed responses (special code = 5)
 - 3) For Mathematics and Science responses where the entire test was presented orally (special code=9) and where students received translated oral script (special code = B)

The descriptive statistics for scale scores were based on all valid cases. The frequency distributions by gender, ethnicity, and other subgroups are shown in Tables 18 through 22.

Tables 23 through 84 display the item analysis results for both multiple-choice (MC) and constructed-response (CR) items for each grade and content area. The product-moment correlation coefficient is used to estimate the item-to-total score correlation for each item. The coefficient for each item is based on the item score and the score computed as the total of all *other* items on the test (hence, the item itself is excluded from the total score). For items having only two levels, the product-moment coefficient is the point-biserial correlation. If an item had to be removed from the calibration and the test because of its aberrant characteristics, the point-biserial correlation was recomputed with the item dropped from the calculation.

The *p*-value for each multiple-choice item is the percent of students who gave a correct response to the item. The *p*-value for each constructed-response item is the mean percent of the maximum possible score. Any omitted responses to individual items or constructed-response items with condition codes were treated as incorrect for the calculation of the *p*-values and the item-to-total score correlations. This is consistent with the treatment of omits in the computation of the operational scale scores. The item-to-total score correlations or point biserials (these terms may be used interchangeably when referring to multiple-choice items), the *p*-values, the percentages of omits, and the percentages at each score level (for the constructed-response items) are based on the analysis of responses of all students with reported total test scores.

As a part of the evaluation of item analysis results, the percent of students obtaining each score point for the constructed-response items across all grades and content areas was examined. The results indicated that a reasonable amount of variability in students' responses to most multiple-choice items and reasonable distribution of score points on most constructed-response items, indicating that these items provided information over the range of student ability. The classical item statistics for all grades and content areas are described briefly in the following sections.

Third Grade

Reading

Table 23 lists the results of the multiple-choice item analyses for the 2011 third-grade Reading assessment. The point biserials for all multiple-choice items ranged from 0.30 to 0.52, with a mean of 0.42. The *p*-values for the multiple-choice items ranged from 0.40 to 0.89, with a mean of 0.67.

Table 24 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.46 to 0.65, with a mean of 0.54. The *p*-values ranged from 0.32 to 0.69, with a mean of 0.43. More than 50% of the students obtained the highest possible score points for one out of the eight constructed-response items. Scores were generally well distributed across the score points of these items.

The omit rates for the third-grade Reading assessment were generally small, ranging from 0.05% to 3.2% for the multiple-choice items (Table 23) and from 0.81% to 2.73% for the constructed-response items (Table 24).

Reading – Spanish

Table 25 lists the results of the multiple-choice item analyses for the Spanish version of the 2011 third-grade Reading assessment. The point biserials for all multiple-choice items ranged from 0.09 to 0.59, with a mean of 0.39. The *p*-values for the multiple-choice items ranged from 0.25 to 0.94, with a mean of 0.60.

Table 26 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.50 to 0.67, with a mean of 0.59. The *p*-values ranged from 0.39 to 0.73, with a mean of 0.56. More than 50% of the students obtained the highest possible score points for two out of the eight constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for all but one of the multiple-choice items on the Spanish version of the third-grade Reading assessment were small. Omit rates for the multiple-

choice items ranged from 0% to 7.30%, with only one item having an omit rate greater than 5% (Table 25). The omit rates for the constructed-response items were small, ranging from 0.17% to 2.27% (Table 26).

Writing

Table 27 lists the results of the multiple-choice item analyses for the 2011 third-grade Writing assessment. The point biserials for all multiple-choice items ranged from 0.31 to 0.55, with a mean of 0.45. The p -values for the multiple-choice items ranged from 0.39 to 0.96, with a mean of 0.79.

Table 28 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.34 to 0.62, with a mean of 0.49. The p -values ranged from 0.64 to 0.97, with a mean of 0.79. More than 50% of the students obtained the highest possible score points for 15 of the 18 constructed-response items.

The omit rates for the third-grade Writing assessment were generally small, ranging from 0.02% to 6.11% for the multiple-choice items (Table 27) with only one item having an omit rate greater than 5%. Omit rates for the constructed-response items were small, ranging from 0.06% to 0.49% (Table 28).

Writing – Spanish

Table 29 lists the results of the multiple-choice item analyses for the Spanish version of the 2011 third-grade Writing assessment. The point biserials for all multiple-choice items ranged from 0.20 to 0.51, with a mean of 0.41. The p -values for the multiple-choice items ranged from 0.24 to 0.95, with a mean of 0.73.

Table 30 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.37 to 0.63, with a mean of 0.51. The p -values ranged from 0.22 to 0.91, with a mean of 0.70. More than 50% of the students obtained the highest possible score points for 14 of the 18 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the Spanish version of the third-grade Writing assessment were small, ranging from 0% to 1.55% for the multiple-choice items (Table 29) and from 0.57% to 1.39% for the constructed-response items (Table 30).

Mathematics

Table 31 lists the results of the multiple-choice item analyses for the 2011 third-grade Mathematics assessment. The point biserials for all multiple-choice items ranged from 0.00 to 0.59, with a mean of 0.43. The p -values for the multiple-choice items ranged from 0.14 to 0.91, with a mean of 0.68.

Table 32 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.52 to 0.67, with a mean of 0.62. The p -values ranged from 0.37 to 0.77, with a mean of 0.59. More than 50% of the students obtained the highest possible score points for three of the eight constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the third-grade Mathematics assessment were generally small, ranging from 0.10% to 5.80% for the multiple-choice items (Table 31) and from 0.04% to 5.44% for the constructed-response items (Table 32). There was one multiple-choice item and one-constructed response item with an omit rate greater than 5%.

Fourth Grade

Reading

Table 33 lists the results of the multiple-choice item analyses for the 2011 fourth-grade Reading assessment. The point biserials for all multiple-choice items ranged from 0.18 to 0.56, with a mean of 0.43. The p -values for the multiple-choice items ranged from 0.15 to 0.93, with a mean of 0.70.

Table 34 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.46 to 0.60, with a mean of 0.53. The p -values ranged from 0.27 to 0.83, with a mean of 0.49. More than 50% of the students obtained the highest possible score points for three of the 14 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the fourth-grade Reading assessment were small, ranging from 0.02% to 1.98% for the multiple-choice items (Table 33) and from 0.40% to 3.35% for the constructed-response items (Table 34).

Reading – Spanish

Table 35 lists the results of the multiple-choice item analyses for the Spanish version of the 2011 fourth-grade Reading assessment. The point biserials for all multiple-choice items ranged from 0.06 to 0.54, with a mean of 0.31. The p -values for the multiple-choice items ranged from 0.29 to 0.95, with a mean of 0.64.

Table 36 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.28 to 0.68, with a mean of 0.48. The p -values ranged from 0.22 to 0.73, with a mean of 0.42. More than 50% of the students obtained the highest possible score

points for two of the 14 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the Spanish version of the fourth-grade Reading assessment were generally small, ranging from 0% to 3.20% for the multiple-choice items (Table 35) and from 0.00% to 4.00% for the constructed-response items (Table 36).

Writing

Table 37 lists the results of the multiple-choice item analyses for the 2011 fourth-grade Writing assessment. The point biserials for all multiple-choice items ranged from 0.24 to 0.54, with a mean of 0.40. The *p*-values for the multiple-choice items ranged from 0.38 to 0.94, with a mean of 0.77.

Table 38 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.14 to 0.66, with a mean of 0.46. The *p*-values ranged from 0.57 to 0.98, with a mean of 0.76. More than 50% of the students obtained the highest possible score points for eight of the 13 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the fourth-grade Writing assessment were small, ranging from 0.03% to 3.02% for the multiple-choice items (Table 37) and from 0.0% to 3.36% for the constructed-response items (Table 38).

Writing – Spanish

Table 39 lists the results of the multiple-choice item analyses for the Spanish version of the 2011 fourth-grade Writing assessment. The point biserials for all multiple-choice items ranged from 0.00 to 0.51, with a mean of 0.30. The *p*-values for the multiple-choice items ranged from 0.23 to 0.98, with a mean of 0.56.

Table 40 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from -0.09 to 0.69, with a mean of 0.41. The *p*-values ranged from 0.11 to 0.91, with a mean of 0.55. More than 50% of the students obtained the highest possible score points for five of the seven one-point constructed-response items and for the only two-point item. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the Spanish version of the fourth-grade Writing assessment were generally small, ranging from 0% to 4.92% for the multiple-choice items (Table 39) and ranging from 0% to 3.28% for the constructed-response items (Table 40).

Mathematics

Table 41 lists the results of the multiple-choice item analyses for the 2011 fourth-grade Mathematics assessment. The point biserials for all multiple-choice items ranged from 0.17 to 0.60, with a mean of 0.44. The p -values for the multiple-choice items ranged from 0.37 to 0.94, with a mean of 0.73.

Table 42 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.40 to 0.68, with a mean of 0.59. The p -values ranged from 0.35 to 0.88, with a mean of 0.64. More than 50% of the students obtained the highest possible score points for six of the 15 constructed response items. The scores on the remaining constructed-response items were well distributed across the score points in those items.

The omit rates for the fourth-grade Mathematics assessment were generally small, ranging from 0.05% to 3.62% for the multiple-choice items (Table 41) and from 0.04% to 1.13% for the constructed-response items (Table 42).

Fifth Grade

Reading

Table 43 lists the results of the multiple-choice item analyses for the 2011 fifth-grade Reading assessment. The point biserials for all multiple-choice items ranged from 0.19 to 0.53, with a mean of 0.39. The p -values for the multiple-choice items ranged from 0.38 to 0.91, with a mean of 0.68.

Table 44 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.32 to 0.67, with a mean of 0.55. The p -values ranged from 0.26 to 0.68, with a mean of 0.49. More than 50% of the students obtained the highest possible score points for two of the 14 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the fifth-grade Reading assessment ranged from 0.06% to 5.16% for the multiple-choice items (Table 43) and from 0.42% to 5.63% for the constructed-response items (Table 44). One multiple-choice item and two constructed-response items had omit rates greater than 5%.

Writing

Table 45 lists the results of the multiple-choice item analyses for the 2011 fifth-grade Writing assessment. The point biserials for all multiple-choice items ranged from 0.14 to 0.52, with a mean of 0.41. The p -values for the multiple-choice items ranged from 0.46 to 0.94, with a mean of 0.76.

Table 46 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.11 to 0.66, with a mean of 0.47. The p -values ranged from 0.40 to 0.99, with a mean of 0.73. More than 50% of the students obtained the highest possible score points for seven of the 13 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the fifth-grade Writing assessment were small, ranging from 0.08% to 1.52% for the multiple-choice items (Table 45) and from 0% to 2.11% for the constructed-response items (Table 46).

Mathematics

Table 47 lists the results of the multiple-choice item analyses for the 2011 fifth-grade Mathematics assessment. The point biserials for all multiple-choice items ranged from 0.10 to 0.56, with a mean of 0.42. The p -values for the multiple-choice items ranged from 0.31 to 0.95, with a mean of 0.68.

Table 48 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.46 to 0.67, with a mean of 0.59. The p -values ranged from 0.44 to 0.76, with a mean of 0.61. More than 50% of the students obtained the highest possible score points for four of the 15 constructed-response items. Scores were generally well distributed across the score points of the remaining scored items.

The omit rates for the fifth-grade Mathematics assessment were small, ranging from 0.05% to 1.12% for the multiple-choice items (Table 47) and from 0.07% to 0.56% for the constructed-response items (Table 48).

Science

Table 49 lists the results of the multiple-choice item analyses for the 2011 fifth-grade Science assessment. The point biserials for all multiple-choice items ranged from 0.16 to 0.54, with a mean of 0.37. The p -values for the multiple-choice items ranged from 0.16 to 0.92, with a mean of 0.63.

Table 50 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.36 to 0.54, with a mean of 0.47. The p -values ranged from 0.22 to 0.77, with a mean

of 0.47. More than 50% of the students obtained the highest possible score points for 6 of the 18 constructed-response items. Scores were generally well distributed across the score points of the remaining scored items.

The omit rates for the fifth-grade Science assessment were small, ranging from 0.01% to 0.61% for the multiple-choice items (Table 49) and from 0.19% to 1.08% for the constructed-response items (Table 50).

Sixth Grade

Reading

Table 51 lists the results of the multiple-choice item analyses for the 2011 sixth-grade Reading assessment. The point biserials for all multiple-choice items ranged from 0.08 to 0.57, with a mean of 0.40. The *p*-values for the multiple-choice items ranged from 0.28 to 0.93, with a mean of 0.70.

Table 52 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.40 to 0.63, with a mean of 0.53. The *p*-values ranged from 0.20 to 0.73, with a mean of 0.49. More than 50% of the students obtained the highest possible score points for two of the 14 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the sixth-grade Reading assessment ranged from 0.05% to 5.26% for the multiple-choice items (Table 51) and from 0.79% to 7.17% for the constructed-response items (Table 52). There were three multiple-choice items and two constructed-response items with omit rates greater than 5%.

Writing

Table 53 lists the results of the multiple-choice item analyses for the 2011 sixth-grade Writing assessment. The point biserials for all multiple-choice items ranged from 0.18 to 0.56, with a mean of 0.42. The *p*-values for the multiple-choice items ranged from 0.40 to 0.90, with a mean of 0.71.

Table 54 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.11 to 0.66, with a mean of 0.46. The *p*-values ranged from 0.43 to 0.99, with a mean of 0.74. More than 50% of the students obtained the highest possible score points for seven of the 13 constructed-response items (six of the seven one-point items and the only two-point item). Scores were generally well distributed across the score points of the remaining items.

The omit rates for the sixth-grade Writing assessment ranged from 0.04% to 1.45% for the multiple-choice items (Table 53) and from 0% to 2.36% for the constructed-response items (Table 54).

Mathematics

Table 55 lists the results of the multiple-choice item analyses for the 2011 sixth-grade Mathematics assessment. The point biserials ranged from 0.27 to 0.63, with a mean of 0.43. The p -values for the multiple-choice items ranged from 0.28 to 0.89, with a mean of 0.61.

Table 56 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.38 to 0.78, with a mean of 0.58. The p -values ranged from 0.28 to 0.87, with a mean of 0.56. More than 50% of the students obtained the highest possible score points for three of the 15 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the sixth-grade Mathematics assessment ranged from 0.05% to 0.81% for the multiple-choice items (Table 55) and from 0.13% to 1.64% for the constructed-response items (Table 56).

Seventh Grade

Reading

Table 57 lists the results of the multiple-choice item analyses for the 2011 seventh-grade Reading assessment. The point biserials ranged from 0.13 to 0.56, with a mean of 0.41. The p -values for the multiple-choice items ranged from 0.33 to 0.92, with a mean of 0.69.

Table 58 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.39 to 0.67, with a mean of 0.53. The p -values for the constructed-response items ranged from 0.29 to 0.76, with a mean of 0.54. More than 50% of the students obtained the highest possible score points for four of the 14 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the seventh-grade Reading assessment ranged from 0.08% to 4.40% for the multiple-choice items (Table 57) and from 0.91% to 2.95% for the constructed-response items (Table 58).

Writing

Table 59 lists the results of the multiple-choice item analyses for the 2011 seventh-grade Writing assessment. The point biserials for all multiple-choice

items ranged from 0.16 to 0.60, with a mean of 0.41. The p -values for the multiple-choice items ranged from 0.28 to 0.95, with a mean of 0.68.

Table 60 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.11 to 0.65, with a mean of 0.44. The p -values ranged from 0.18 to 0.99, with a mean of 0.67. More than 50% of the students obtained the highest possible score points for five of the 13 constructed-response items (four of the 7 one-point items and the only two-point item). Scores were generally well distributed across the score points of the remaining items.

The omit rates for the seventh-grade Writing assessment ranged from 0.05% to 1.72% for the multiple-choice items (Table 59) and from 0% to 2.50% for the constructed-response items (Table 60).

Mathematics

Table 61 lists the results of the multiple-choice item analyses for the 2011 seventh-grade Mathematics assessment. The point biserials for all multiple-choice items ranged from 0.19 to 0.62, with a mean of 0.41. The p -values for the multiple-choice items ranged from 0.20 to 0.92, with a mean of 0.54.

Table 62 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.11 to 0.75, with a mean of 0.59. The p -values ranged from 0.17 to 0.75, with a mean of 0.41. Scores were generally well distributed across the score points of the items.

The omit rates for the seventh-grade Mathematics assessment ranged from 0.06% to 1.61% for the multiple-choice items (Table 61) and from 0.21% to 2.09% for the constructed-response items (Table 62).

Eighth Grade

Reading

Table 63 lists the results of the multiple-choice item analyses for the 2011 eighth-grade Reading assessment. The point biserials for the multiple-choice items ranged from 0.12 to 0.53, with a mean of 0.38. The p -values for the scored multiple-choice items ranged from 0.27 to 0.91, with a mean of 0.68.

Table 64 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.50 to 0.67, with a mean of 0.59. The p -values ranged from 0.42 to 0.68, with a mean of 0.54. More than 50% of the students obtained the highest possible score

points for two of the 14 constructed-response items. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the eighth-grade Reading assessment ranged from 0.03% to 1.10% for multiple-choice items (Table 63) and from 0.84% to 5.54% for constructed-response items (Table 64). There was one constructed-response item with an omit rate greater than 5%.

Writing

Table 65 lists the results of the multiple-choice item analyses for the 2011 eighth-grade Writing assessment. The point biserials for all multiple-choice items ranged from 0.03 to 0.55, with a mean of 0.38. The p -values for the multiple-choice items ranged from 0.28 to 0.94, with a mean of 0.68.

Table 66 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.11 to 0.64, with a mean of 0.43. The p -values ranged from 0.61 to 0.99, with a mean of 0.77. More than 50% of the students obtained the highest possible score points on all of the 7 one-point items and on the only two-point item in the test. Scores were generally well distributed across the score points of the remaining items.

The omit rates for the eighth-grade Writing assessment ranged from 0.10% to 0.94% for multiple-choice items (Table 65), and from 0% to 3.07% for constructed-response items (Table 66).

Mathematics

Table 67 lists the results of the multiple-choice item analyses for the 2011 eighth-grade Mathematics assessment. The point biserials for all multiple-choice items ranged from 0.05 to 0.59, with a mean of 0.41. The p -values for the multiple-choice items ranged from 0.13 to 0.84, with a mean of 0.53.

Table 68 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.13 to 0.77, with a mean of 0.59. The p -values ranged from 0.19 to 0.69, with a mean of 0.40. Scores were generally well distributed across the score points of all of the constructed-response items.

The omit rates for the eighth-grade Mathematics ranged from 0.06% to 2.56% for the multiple-choice items (Table 67) and from 0.18% to 2.79% for the constructed-response items (Table 68).

Science

Table 69 lists the results of the multiple-choice item analyses for the 2011 eighth-grade Science assessment. The point biserials for all multiple-choice items ranged from 0.07 to 0.56, with a mean of 0.35. The p -values for the multiple-choice items ranged from 0.22 to 0.88, with a mean of 0.54.

Table 70 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.13 to 0.70, with a mean of 0.44. The p -values ranged from 0.01 to 0.81, with a mean of 0.44. More than 50% of the students obtained the highest possible score points for six of the 23 constructed-response items. Scores were generally well distributed across the score points of the remaining constructed-response items.

The omit rates for the eighth-grade Science assessment ranged from 0.03% to 0.61% for the multiple-choice items (Table 69) and from 0.36% to 8.75% for the constructed-response items (Table 70). There were two constructed-response items with omit rates greater than 5%.

Ninth Grade

Reading

Table 71 lists the results of the multiple-choice item analyses for the 2011 ninth-grade Reading assessment. The point biserials ranged from 0.12 to 0.56, with a mean of 0.38. The p -values for these multiple-choice items ranged from 0.31 to 0.98, with a mean of 0.68.

Table 72 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.49 to 0.67, with a mean of 0.58. The p -values ranged from 0.26 to 0.69, with a mean of 0.50. Scores were generally well distributed across the score points of the constructed-response items.

The omit rates for the ninth-grade Reading assessment ranged from 0.04% to 3.73% for the multiple-choice items (Table 71). The omit rates for the constructed-response items ranged from 1.33% to 11.4%, with four of the 14 items having an omit rate greater than 5% (Table 72).

Writing

Table 73 lists the results of the multiple-choice item analyses for the 2011 ninth-grade Writing assessment. The point biserials for all multiple-choice items ranged from -0.04 to 0.62, with a mean of 0.44. The p -values for the multiple-choice items ranged from 0.26 to 0.89, with a mean of 0.70.

Table 74 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.16 to 0.66, with a mean of 0.47. The p -values ranged from 0.23 to 0.98, with a mean of 0.63. More than 50% of the students obtained the highest possible score points for five of the 13 constructed-response items. Scores were generally well distributed across the score points of the remaining constructed-response items.

The omit rates for the ninth-grade Writing assessment ranged from 0.10% to 0.91% for the multiple-choice items (Table 73). The omit rates for the constructed-response items ranged from 0% to 4.45% (Table 74).

Mathematics

Table 75 lists the results of the multiple-choice item analyses for the 2011 ninth-grade Mathematics assessment. The point biserials for all multiple-choice items ranged from -0.01 to 0.55, with a mean of 0.35. The p -values for the multiple-choice items ranged from 0.03 to 0.87, with a mean of 0.47.

Table 76 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.41 to 0.76, with a mean of 0.63. The p -values ranged from 0.18 to 0.74, with a mean of 0.40. Scores were generally well distributed across the score points of the 15 constructed-response items.

The omit rates for the ninth-grade Mathematics assessment were ranged from 0.10% to 0.86% for the multiple-choice items (Table 75). The omit rates for the constructed-response items ranged from 0.57% to 5.40%, with only one item greater than 5% (Table 76).

Tenth Grade

Reading

Table 77 lists the results of the multiple-choice item analyses for the 2011 tenth-grade Reading assessment. The point biserials for all multiple-choice items ranged from 0.11 to 0.53, with a mean of 0.39. The p -values for the multiple-choice items ranged from 0.34 to 0.95, with a mean of 0.67.

Table 78 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.48 to 0.70, with a mean of 0.62. The p -values ranged from 0.27 to 0.69, with a mean of 0.49. More than 50% of the students obtained the highest possible score points for one of the 14 constructed-response items. Scores were generally well distributed across the score points of the remaining constructed-response items.

The omit rates for the tenth-grade Reading assessment were small for the multiple-choice items but large for the constructed-response items. The omit rates for multiple-choice items ranged from 0.06% to 1.18% (Table 77). The omit rates for the constructed-response items ranged from 3.15% to 8.50%, with eight out of the 14 items having an omit rate greater than 5% (Table 78).

Writing

Table 79 lists the results of the multiple-choice item analyses for the 2011 tenth-grade Writing assessment. The point biserials for all multiple-choice items ranged from 0.26 to 0.58, with a mean of 0.45. The *p*-values for the multiple-choice items ranged from 0.33 to 0.95, with a mean of 0.74.

Table 80 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from -0.01 to 0.68, with a mean of 0.43. The *p*-values ranged from 0.39 to 0.98, with a mean of 0.71. More than 50% of the students obtained the highest possible score points for six of the seven one-point items and for the only two-point item. Scores were generally well distributed across the score points of the remaining constructed-response items.

The omit rates for the tenth-grade Writing assessment ranged from 0.10% to 0.88% for the multiple-choice items (Table 79). The omit rates for the constructed-response items ranged from 0% to 3.37% (Table 80).

Mathematics

Table 81 lists the results of the multiple-choice item analyses for the 2011 tenth-grade Mathematics assessment. The point biserials for the multiple-choice items ranged from 0.14 to 0.58, with a mean of 0.37. The *p*-values for the multiple-choice items ranged from 0.05 to 0.79, with a mean of 0.47.

Table 82 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.23 to 0.74, with a mean of 0.62. The *p*-values for the constructed-response items ranged from 0.03 to 0.61, with a mean of 0.35. More than 50% of the students obtained the highest possible score points for none of the 15 constructed-response items. Scores were generally well distributed across the score points of the constructed-response items.

The omit rates for the tenth-grade Mathematics assessment ranged from 0.05% to 0.99% for the multiple-choice items (Table 81) and from 0.60% to 5.05% for the constructed-response items (Table 82). There was one constructed-response item with an omit rate greater than 5%.

Science

Table 83 lists the results of the multiple-choice item analyses for the 2011 tenth-grade Science assessment. The point biserials for the multiple-choice items ranged from -0.04 to 0.53, with a mean of 0.33. The p -values for these items ranged from 0.23 to 0.87, with a mean of 0.54.

Table 84 lists the results of the constructed-response item analyses. The item-to-total score correlations for the constructed-response items ranged from 0.27 to 0.58, with a mean of 0.44. The p -values for the constructed-response items ranged from 0.09 to 0.56, with a mean of 0.33. More than 50% of the students obtained the highest possible score points for two of the 23 constructed-response items. Scores were generally well distributed across the score points of the remaining constructed-response items.

The omit rates for the tenth-grade Science assessment ranged from 0.02% to 0.65% for the multiple-choice items (Table 83). The omit rates for the constructed-response items ranged from 1.63% to 23.43%, with seven out of the 23 items having an omit rate greater than 5% (Table 84).

Part 6: Calibration and Equating

Part 6 describes item response theory (IRT) models used for calibration and equating, fit criterion for model-to-data fit, and items flagged for poor model fit for all grades and content areas. It also briefly presents the number of item pairs correlated within each grade and content area measured by Yen's Q3 statistic (Yen, 1984), followed by equating design and methods for evaluating anchor items. The test characteristic curves for the total test and anchor set are presented as evidence that the anchor set was representative of the total test and linking was reasonable. Finally, the scaling constants resulting from the linking are presented.

Overview of the IRT Models

CTB uses IRT to place multiple-choice and constructed-response items on the same scale. Because the characteristics of selected-response (multiple-choice) and constructed-response (open-ended) items are different, two-item response theory models are used in the analysis of test forms containing both item types. The three-parameter logistic (3PL) model (Lord, 1980; Lord & Novick, 1968) is used for the analysis of selected-response items. In this model, the probability that a student with scale score θ responds correctly to item i is

$$P_i(\theta) = c_i + \frac{1 - c_i}{1 + \exp[-1.7a_i(\theta - b_i)]},$$

where a_i is the item discrimination, b_i is the item difficulty, and c_i is the probability of a correct response by a very low scoring student. These three parameters are estimated from the item response data.

For analysis of constructed-response items, the two-parameter partial credit model (2PPC) (Muraki, 1992; Yen, 1993) is used. The 2PPC model is a special case of Bock's (1972) nominal model. Bock's model states that the probability of an examinee with ability θ having a score at the k th level of the j th item is

$$P_{jk}(\theta) = P(x_j = k - 1 | \theta) = \frac{\exp Z_{jk}}{\sum_{i=1}^{m_j} \exp Z_{ji}}, \quad k = 1, K, m_j,$$

where m_j is the number of score levels and

$$Z_{jk} = A_{jk}\theta + C_{jk}.$$

For the special case of the 2PPC model used here, the following constraints are used:

$$A_{jk} = \alpha_j(k-1), \quad k = 1, 2, \dots, K, m_j,$$

and

$$C_{jk} = -\sum_{i=0}^{k-1} \gamma_{ji}, \quad \text{where } \gamma_{j0} = 0,$$

and where α_j and γ_{ji} are the parameters to be estimated from the data. The first constraint implies that higher item scores reflect higher ability levels and that the items can vary in their discriminations. For the 2PPC model, for each item there are $m_j - 1$ independent γ_{ji} parameters and one α_j parameter; a total of m_j independent item parameters are estimated.

The IRT models are implemented using CTB's PARDUX computer program (Burket, 1993). PARDUX estimates parameters simultaneously for dichotomous (multiple-choice) and polytomous (constructed-response) items using marginal maximum likelihood procedures implemented via the EM algorithm (Bock & Aitkin, 1981; Thissen, 1982).

Calibration of the Assessment

The items within a grade in each content area were calibrated using CTB's computer program PARDUX (Burket, 1993), and all items were evaluated for model fit and local independence. The calibration sample ranged from 88% to 100% of the total tested population for all grades and content areas.

The parameters estimated by PARDUX are in two different parameterizations, corresponding to the two item response theory models (3PL and 2PPC). The location (difficulty) and discrimination (characteristics of an item to differentiate students with different abilities) parameters for the multiple-choice items are in the traditional 3PL metric and are designated as b and a , respectively. The location and discrimination parameters for the constructed-response items are in the 2PPC metric, designated g (gamma) and f (alpha), respectively. Because of the different metrics used, the 3PL (multiple-choice) parameters (a and b) are not directly comparable to the 2PPC (constructed-response) parameters (f and g). However, they can be converted to a common metric. The two metrics are related by $b = g/f$ and $a = f/1.7$ (see Burket, 1993). As a result of this procedure, the multiple-choice and constructed-response items are placed on the same scale. Note that for the 2PPC model there are $m_j - 1$ (where m_j is the number of score levels for item j) independent g 's and one f , for a total of m_j independent parameters estimated for each item. For the 3PL model, there is one "a"

parameter, one “ b ” parameter, and one pseudo-guessing parameter, “ c ,” for each item.

Model Fit Analyses

During the calibration process, each item is reviewed for how well the item parameters in the model fit the observed data. Item fit was assessed using the Q_1 statistic described by Yen (1981) for the dichotomously (multiple-choice) scored items and using a generalization of this statistic for the multilevel (constructed-response) items. As described by Yen, Q_1 is a Pearson chi-square of the form in each cell

$$Q_{1j} = \sum_{i=1}^I \frac{N_{ji} (O_{ji} - E_{ji})^2}{E_{ji}} + \sum_{i=1}^I \frac{N_{ji} [1 - O_{ji} - 1 - E_{ji}]^2}{1 - E_{ji}},$$

where N_{ji} is the number of examinees in cell i for item j . O_{ji} and E_{ji} are the observed and predicted proportions of examinees in cell i that attain the maximum possible score on item j , where

$$E_{ji} = \frac{1}{N_{ji}} \sum_{a \in cell i}^{N_{ji}} P_j(\hat{\theta}_a).$$

The generalization of Q_1 for multilevel (constructed-response) items in each cell can be stated as

$$Q_{1j} = \sum_{i=1}^I \sum_{k=1}^{m_j} \frac{N_{jki} (O_{jki} - E_{jki})^2}{E_{jki}},$$

where

$$E_{jki} = \frac{1}{N_{ji}} \sum_{a \in cell i}^{N_{ji}} P_{jk}(\hat{\theta}_a).$$

O_{jki} and E_{jki} are the observed and expected proportion of examinees in cell i who performed at the k th score level.

Chi-square statistics are affected by sample size and extreme expectations (Stone, Ankenmann, Lane, & Liu, 1993), and their degrees of freedom are a function of the number of independent observations entering into the calculation minus the number of parameters estimated. Items with more score levels have more degrees of freedom, making it awkward to compare fit for items that differ in the number of

score levels. To facilitate this comparison, the following standardization of the Q_i statistic was used:

$$Z_{Q_i} \equiv \frac{Q_{1j} - df}{\sqrt{2df}}.$$

The value of Z still will increase with sample size, all else being equal. To use this standardized statistic to flag items for potential misfit, it has been CTB's practice to vary the critical value for Z as a function of sample size. When piloting multiple-choice items for new tests, CTB typically has used the flagging criterion $Z \geq 4.00$ with sample sizes of approximately 1,000 students. For the operational tests, which have larger calibration sample sizes, the criterion Z_c used to flag items was calculated using the expression

$$Z_c = \left(\frac{\text{Calibration Sample Size}}{1,500} \right) * 4.00.$$

This criterion was used to flag operational CSAP items for potential misfit. Item characteristic curves (ICCs) of all flagged items were visually inspected in order to decide whether their high Z 's resulted from poor model-data fit or from irrelevant variables such as extreme expectations that often accompany unusually easy or hard items. Only those items judged to be poorly fit by the model were defined as misfitting items.

Model Fit Analyses Results

The model fit statistics and item parameter results are based on the analysis of a sample data set used for item calibration and scaling⁹. The summary fit statistics for the multiple-choice and constructed-response items for different grades and content areas are shown in Tables 85 through 146.

Detailed summaries of the model fit results are presented below.

Third Grade

The third-grade item parameters and fit statistics are shown in Tables 85 through 94. The critical Z -values for these tables are 153.46 for Reading, 3.60 for Spanish Reading, 162.12 for Writing, 3.92 for Spanish Writing, and 147.16 for Mathematics.

⁹ Results for the Spanish tests are based on previous years' data because these four tests were not recalibrated in 2011. The grade 4 Spanish tests were pre-equated using item parameters from several different prior administrations.

Across all content areas, three items exceeded these critical Z-values and exhibited less than optimal fit: one Spanish Reading item (CR item 1), one Spanish Writing item (MC item 6), and one Mathematics item (CR item 37).

Fourth Grade

The fourth-grade item parameters and fit statistics are shown in Tables 95 through 104. The critical Z-values for these tables are 162.82 for Reading, 162.32 for Writing, and 148.40 for Mathematics. The pre-equated Spanish Reading test had a critical Z-value of 1.39 for items that originated in the 2004 administration, 1.30 for items that originated in the 2005 administration, and 0.70 for items that originated in the 2007 administration. The pre-equated Spanish Writing test had a critical Z-value of 1.40 for items that originated in the 2004 administration and 1.31 for items that originated in the 2005 administration. Spanish Writing grade 4 had a critical Z-value of 2.67 for constructed-response items that originated in 2002, 1.31 for items that originated in the 2005 administration, and 0.70 for items that originated in the 2007 administration.

Across all English content areas, five items exceeded the critical Z-values and exhibited less than optimal fit: two Reading items (CR items 108 and 109), two Writing items (CR items 3A and 93), and one Mathematics item (CR item 15).

Fifth Grade

The fifth-grade item parameters and fit statistics are shown in Tables 105 through 112. The critical Z-values for these tables are 160.41 for Reading, 159.79 for Writing, 149.25 for Mathematics, and 149.50 for Science.

Across all content areas, five items exceeded these critical Z-values and exhibited less than optimal fit: one Reading item (CR item 27), two Writing items (CR items 3A and 96), and two Science items (MC item 26 and CR item 73).

Sixth Grade

The sixth-grade item parameters and fit statistics are shown in Tables 113 through 118. The critical Z-values for these tables are 153.40 for Reading, 153.00 for Writing, and 151.27 for Mathematics.

Across all content areas, four items exceeded these critical Z-values and exhibited less than optimal fit: two Writing items (CR items 3A and 98), and two Mathematics items (CR items 15 and 40).

Seventh Grade

The seventh-grade item parameters and fit statistics are shown in Tables 119 through 124. The critical Z -values for these tables are 150.47 for Reading, 150.16 for Writing, and 151.24 for Mathematics.

Across all content areas, seven items exceeded these critical Z -values and exhibited less than optimal fit: one Reading item (CR item 99), two Writing items (CR items 3A and 95), and four Mathematics items (MC items 5 and 36 and CR items 12 and 26).

Eighth Grade

The eighth-grade item parameters and fit statistics are shown in Tables 125 through 132. The critical Z -values for these tables are 146.96 for Reading, 146.58 for Writing, 149.17 for Mathematics, and 148.90 for Science.

Across all content areas, eight items exceeded these critical Z -values and exhibited less than optimal fit: one Reading item (MC item 28), three Writing items (CR items 3A, 94, and 116), three Mathematics items (CR items 48, 54, and 60), and one Science item (CR item 51).

Ninth Grade

The ninth-grade item parameters and fit statistics are shown in Tables 133 through 138. The critical Z -values for these tables are 147.53 for Reading, 147.29 for Writing, and 154.55 for Mathematics.

Across all content areas, four items exceeded these critical Z -values and exhibited less than optimal fit: one Reading item (MC item 92), two Writing items (MC item 63 and CR item 116), and one Mathematics item (CR item 60).

Tenth Grade

The tenth-grade item parameters and fit statistics are shown in Tables 139 through 146. The critical Z -values for these tables are 141.97 for Reading, 141.60 for Writing, 149.02 for Mathematics, and 148.77 for Science.

Across all content areas, 11 items exceeded these critical Z -values and exhibited less than optimal fit: two Reading items (MC items 21 and 104), four Writing items (MC item 56 and CR items 3A, 3B, and 116), four Mathematics items (MC items 51 and 56 and CR items 8 and 60), and one Science item (CR item 24).

Item Local Independence

In using IRT models, one of the assumptions made is that the items are locally independent. That is, a student's response to one item is not dependent on the response to another item. Statistically speaking, when a student's ability is accounted for, the response to each item is statistically independent.

One way to measure the statistical local independence of items within a test is via the Q3 statistic (Yen, 1984). This statistic was obtained by correlating differences between students' observed and expected responses for pairs of items after taking into account overall test performance. If a substantial number of items within a test form demonstrate local dependence, these items may need to be calibrated separately. Pairs of items with Q3 values greater than 0.30 were classified as locally dependent. The maximum value for this index is 1.00.

The number of item pairs flagged for each test form was quite small, ranging from zero to four pairs across grades and content areas. For Reading, three item pairs were flagged across all grades (grade 4 items 8 and 26; grade 9 items 97 and 98; and grade 9 items 98 and 99). For Writing, 16 pairs were flagged (grade 4 items 3A and 3B; grade 4 items 3B and 3C; grade 5 items 3A and 3B; grade 6 items 3A and 3B; grade 7 items 3A and 3B; grade 7 items 72 and 116; grade 7 items 78 and 79; grade 7 items 95 and 116; grade 8 items 3A and 3B; grade 8 items 94 and 116; grade 9 items 3A and 3B; grade 9 items 65 and 91; grade 9 items 91 and 116; grade 10 items 3A and 3B; grade 10 items 69 and 90; and grade 10 items 90 and 116). For Mathematics, four pairs were flagged (grade 5 items 37 and 41; grade 6 items 27 and 51; grade 9 items 10 and 46; and grade 10 items 1 and 19). For Science, no item pairs were flagged. When compared to grades 3 and 4 English Writing items, a relatively larger number of items in the Spanish tests were flagged¹⁰ but for lower Q3 values ranging from 0.33 to 0.56 (12 pairs in all of the Spanish assessments – grade 3 items 2 and 21; grade 3 items 2 and 37; grade 3 items 2 and 50; grade 3 items 2 and 52; grade 3 items 3 and 28; grade 3 items 3 and 35; grade 3 items 3 and 50; grade 3 items 4 and 21; grade 3 items 4 and 35; grade 3 items 4 and 50; grade 4 items 2 and 8; and grade 4 items 2 and 9).

Evaluation of Item Analysis and Calibration

After the evaluation of item analyses and calibration outputs across all grades and content areas, 11 multiple-choice items and one constructed-response item exhibited aberrant characteristics (non-convergence where the item parameters could not be estimated, poor model fit, negative point biserials for the correct

¹⁰ Note that the item dependency statistics for the Spanish assessments are based upon results from a previous administration because these tests were not recalibrated in 2011.

choice, or positive point biserials for distractor(s)). After consulting with CTB content experts and CDE, the following items were removed from the final calibration (all items are MC items except for Writing, grade 10 item 2D, which is a CR item):

- Reading, grade 4 – Item 17
- Reading, grade 6 – Item 108
- Reading, grade 9 – Item 30
- Writing, grade 8 – Items 62 and 80
- Writing, grade 9 – Item 70
- Writing, grade 10 – Item 2D
- Mathematics, grade 8 – Item 49
- Mathematics, grade 9 – Item 57
- Science, grade 10 – Items 46, 68, and 69

Tables 2 through 6 indicate the number of items and score points for each test form after suppressed items were removed.

Equating Procedures

Through a common item equating design, the calibrated/scaled item parameters for each test were placed onto a vertical (cross-grade) or grade-specific scale. A set of previously selected common or anchor multiple-choice items that had been used in previous operational tests were among the items administered in each grade and content area. Three statistical methods were in place to evaluate the differential performance of these anchor items. The methods are described in the next section. These items were given in approximately the same location or in the same third of the test as their original administration location. The items were operational in previous administrations and maintained original starting parameter values. These multiple-choice items were used as anchors in the spring 2011 CSAP to link the tests across years. The anchor parameters were not fixed during calibration and were used in the equating procedures defined by Stocking and Lord (1983). The anchor parameters were used to place the estimated parameters for the spring 2011 CSAP items on the original scales.

As mentioned previously, equating is a statistical procedure that allows adjusting scores on test forms so that the scores are comparable. The Stocking and Lord procedure (1983), also called the test characteristic curve (TCC) method, was used to place each grade on the vertical scale that had been developed previously for each content area. It minimizes the mean squared difference between the two characteristics curves, one based on estimates from the previous calibration and the other on transformed estimates from the current calibration. Let $\hat{\psi}_j$ be a true score for an examinee, j , with ability θ_j based on item parameter estimates (a_j, b_j, c_j) from the previous calibration and $\hat{\psi}_j^*$ be the estimated true score obtained after the re-estimation of item parameters using current data and transformed to the previous scale.

$$\hat{\psi}_j = \hat{\psi}(\theta_j) = \sum_{i=1}^n P_i(\theta_j; a_i, b_i, c_i) \quad \hat{\psi}_j^* = \hat{\psi}(\theta_j) = \sum_{i=1}^n P_i(\theta_j; \frac{a_i}{M_1}, M_1 b_i + M_2, c_i)$$

The TCC method determines the scaling constants (multiplicative--M1 and additive--M2) by minimizing the following quadratic loss function (F):

$$F = \frac{1}{N} \sum_{j=1}^N (\hat{\psi}_j - \hat{\psi}_j^*)^2$$

where N is the number of examinees in the arbitrary group.

Anchor Items Evaluation Criteria

The multiple-choice anchor items were carefully reviewed to ensure they were performing very similarly in both current and reference years. Three statistical methods—the TCC method (Stocking & Lord, 1983), the Delta Plot method (Angoff, 1972; Dorans & Holland, 1993), and the Chi-Square method (Lord, 1980)—were applied to evaluate the anchor items. A description of the TCC method can be seen in the previous section (Equating Procedures). The Delta Plot and Lord's Chi-Square methods are described briefly below.

The Delta Plot method relies only on the differences in the probability of responding to the item correctly (p -value). For example, p -values of the anchor items based on the previous and current year's population will be calculated. The p -values then will be converted to standard normal distribution, Z -scores, that correspond to the $(100 \cdot (1 - p))$ th percentiles. For example, for a p -value of 0.90, the corresponding Z -score will be at the 10th percentile $(100 \cdot (1 - 0.90))$, which is -1.2816 . A simple rule to identify outlier items that are functioning differentially between the two groups with respect to the level of difficulty is to draw perpendicular distance to the line of best fit. The fitted line is chosen so as to minimize the sum of squared perpendicular distances of the points to the line. The perpendicular distance is given by

$$D = \frac{AZ_{old} - Z_{new} + B}{\sqrt{A^2 + 1}},$$

where

$$A = \frac{(SD_{Z_{new}}^2 - SD_{Z_{old}}^2) + \sqrt{(SD_{Z_{new}}^2 - SD_{Z_{old}}^2)^2 + 4r_{(Z_{old})(Z_{new})}^2 SD_{Z_{old}}^2 SD_{Z_{new}}^2}}{2r_{(Z_{new})(Z_{old})} SD_{Z_{old}} SD_{Z_{new}}}$$

and

$$B = \text{Mean}(Z_{new}) - A \cdot \text{Mean}(Z_{old}).$$

The standard deviation (SD) of the perpendicular distance is given by

$$SD_D = [(SD_{Z_{new}} + SD_{Z_{old}}) / 2] * \sqrt{1 - r_{(Z_{old})(Z_{new})}}.$$

As a rule of thumb, any items lying more than three standard deviations of the distances away from the fitted line are flagged as outliers.

Lord's Chi-Square criterion involves significance testing of both item difficulty and discrimination parameters simultaneously for each item and evaluating the result based on the chi-square distribution table (see Divgi, 1985, and Lord, 1980, for details). If the null hypotheses that the item difficulty and discrimination parameters are equal are true, the χ^2 follows chi-square distribution with 2 degrees of freedom.

The following verifications were performed to ensure the quality and accuracy of the equating:

- 1) The IRT item parameters (a , b , and c), and p -values between reference and current anchor sets were plotted for preliminary screening.
- 2) The p -values of the anchor items were compared to make sure that the anchor items were similar in difficulty in both new and reference administrations. A regression line was drawn for the p -values between the estimated new form and the reference form. If the samples are similar in ability, this regression line will be the identity line. The Delta Plot method (Angoff, 1972; Dorans & Holland, 1993) was used to evaluate the significant p -value differences.
- 3) The IRT item parameters for each anchor item were compared. Lord's Chi-Square (Lord, 1980) method was used for flagging items with significantly differential item characteristic curves.
- 4) The reference and equated anchor item set TCCs were compared to make sure that they were closely overlapping. Similarly, the correlation coefficients between the reference and equated item parameters were compared.
- 5) The linear transformation parameters (also known as scaling constants) were compared to make sure that they were fairly stable across administrations.

Additional analyses of the equating results included the following:

- 6) The p -values of the common anchor items between the two administrations were compared to show that changes in the p -values were consistent with changes in the scale scores.
- 7) The full distribution of scale scores was compared for reasonableness across administrations and results verified to ensure that any observed differences were consistent with the differences in ability that were indicated by the anchor items.

- 8) The pass rates were compared for reasonableness across administrations, given any noted ability changes.

These routine CTB quality-check steps were followed during equating for all grades and content areas.

Anchor Items Evaluation Results

The Colorado Department of Education had the final responsibility for determining which items would or would not be removed from the anchor sets. The primary criteria for removing an anchor item from the anchor set were as follows: If an anchor item was flagged by both Delta Plot and Lord's Chi-Square methods *and* had a p -value difference of greater than 0.10, it would be dropped from the anchor set. Items that did not meet these criteria but exhibited other serious statistical problems or content-related issues also were carefully reviewed in making this determination.

After a careful review of the 31 grade/content areas in the 2011 CSAP administration, two items met the criteria for removal from the anchor sets (grade 5 Writing item 90, grade 6 Writing item 77). The p -values and item parameter comparison results for the final anchor sets are presented below. Figures 1 and 2 show the item characteristic curves for the anchor items removed from the equating of the 2011 CSAP operational tests.

p -value Comparisons

The analysis of p -values across administrations indicated that the values were aligned closely, with correlations at or above 0.97 for all grades and content areas (Table 147). This indicates that the estimated p -values for the reference and estimated new form item parameters are very similar, suggesting that the anchor items performed similarly across years.

Item Parameter Comparisons

The differential anchor item functioning between the two administrations was evaluated by comparing the correlations between the reference and estimated new form items for difficulty (b) and discrimination (a) values as well as their plots. Guessing (c) parameters exhibit the greatest fluctuation and were not considered in the evaluation criteria.

Results indicate that the parameter correlations for item difficulty (b) and discrimination (a) are high (see Table 147). This indicates that the items were performing similarly in the two administrations and provides further evidence that the equating results are reasonable and accurate. The b -parameter correlations ranged from, 0.88 to 0.99. The a -parameter correlations for the Reading,

Mathematics, and Science tests ranged from 0.92 to 0.98. For the Writing tests, the a -parameter correlations ranged from 0.87 to 0.97 for all grades except grade 8 which had a correlation of 0.61.

Anchor item functioning in terms of item characteristic curves from the two administrations was also evaluated using Lord's Chi-Square method. In addition to the two items that were removed from the anchor sets, five other items were flagged using Lord's Chi Square and Delta Plot methods but were not removed because they failed to meet the other removal criteria. This group was made up of one item in grade 10 Reading, one in grade 4 Writing, one in Grade 7 Writing, one in Grade 9 Writing, and one in Grade 10 Writing.

Scaling Constants

The scaling constants (linear transformation parameters that were used to place scores onto the equated scale score metric) were examined to determine whether the ability levels of students in the calibration and equating samples varied over time or were similar across years. Since the calibration "centers" the raw IRT scale close to the average ability of the sample, differences in these scaling constants would indicate differences in the ability distributions of the calibration samples from reference to new form administrations. The scaling constants for the CSAP grades and content areas are displayed in Table 148 for the 2010 and 2011 administrations.

Table 148 indicates that for most grades and content areas the scaling constants are fairly similar across the two administrations.

Additional Analyses of Flagged Items

Review of the content balance for the final anchor sets after removing the flagged items indicated that these anchors were reasonably representative of the blueprint for the total tests. Tables 149 through 153 indicate number and percentage of items by content standard for total test and anchor set.

Effectiveness of the Equating

Figures 3 through 29 show the TCC and SEM plots for the spring 2011 operational tests in grades 3 through 10 Reading (Figures 3 through 10), Writing (Figures 11 through 18), Mathematics (Figures 19 through 26), and grades 5, 8, and 10 Science (Figures 27 through 29) compared to the previous year's plots based on census data. Each figure included in this section displays four comparison curves: (a) test characteristic curves, (b) standard errors of measurement, (c) test information curves, and (d) cumulative frequency distributions. These plots illustrate the effectiveness of the equating. The similarity of the plots of the TCCs (the S-shaped curves) and the SEM curves (the U-shaped curves) for each subject area and grade indicates that the test forms administered in 2010 and 2011 strongly resembled each other in terms of item difficulty, discrimination, and accuracy. Note that because the Spanish Reading and Writing tests were not post-equated this year, the plots for these tests are not included.

After the tests were equated, the final scaled parameters were used to derive each student's scale score. The CSAP uses item-pattern scoring for all tests. During item-pattern scoring, the pattern of student responses and the attributes of each item contribute to the student's final scale score. For example, two students who respond correctly to a total of 20 questions obtain the same scale score in number-correct scoring. Depending upon the difficulty and discrimination of the items the students answered correctly, they may receive different scale scores in item-pattern scoring. The item-pattern scoring is able to take those responses and item attributes into account and provide a scale score that better represents the students' abilities. This enhances the comparability of scores across years.

Part 7: Scale Score Summary Statistics

Student results are reported statewide in terms of scale scores and performance levels. All valid cases were used for the computation. The scale score ranges (LOSS and HOSS) for each grade and content area are listed in Table 10.

The performance level cut scores were adopted by the Colorado State Board of Education on the basis of the recommendations of standard setting committees composed of qualified Colorado educators, using a variation of the Bookmark standard setting procedure (Lewis, Mitzel, & Green, 1996). As mentioned previously, the performance standards for Reading were adopted from the 2001 standard setting. The performance standards for Writing and Mathematics were adopted from 2002 standard setting, except for grades 3 and 4 Mathematics. The grades 3 and 4 Mathematics assessments were introduced in 2005, and standards were set in the same year. Similarly, performance standards for grades 5, 8, and 10 Science were reviewed and set in 2008.

Summary statistics are based on the total Colorado student population tested by the CSAP. Table 154 presents the mean, median, and standard deviation of the scale scores for the total population and for each gender in each grade/content area. Note that the male and female students do not necessarily equal the total population because some students may not identify their gender.

On average, female students scored higher than male students at all grade levels on the Reading and Writing tests, while male students scored slightly higher than female students at grades 5 and 8 on the Science assessments. For Mathematics, male students scored slightly higher than females in grades 3, 5, and 10, and female students scored slightly higher than males in grades 6, 7, and 8.

Tables 155 and 156 contain scale score descriptive statistics for each content standard and subcontent area, respectively. Since the scale scores for content standards and subcontent areas are computed on the basis of fewer items, students more easily get the highest obtainable score or the lowest obtainable score on these than on the total test, causing the scale score distributions to be skewed in some cases. For that reason, both means and medians are reported. Tables 157 and 158 contain number-correct descriptive statistics for the total population, and the mean percent of the maximum points obtained for each content standard and subcontent area, respectively.

Note the following particulars for reporting purposes: Grade 3 Reading measures only one content standard; content standards 2 and 3 are combined for grade 3 Mathematics; content standards 1 and 6 are combined in grades 7 through 10 Mathematics; content standards 4 and 5 are combined in grades 3 through 10 Mathematics; and content standards 1 and 5 are combined for grades 5, 8, and

10 Science. Similarly, subcontent areas 1 and 4 are combined for grades 3 through 6 Reading. In Tables 155 through 158, where content standards or subcontent areas are combined (e.g., CS 2/3 for grade 3 Mathematics) the scores are reported under the first content standard or subcontent area (e.g., CS 2 for grade 3 Mathematics).

Scale Score Distributions: Student Results

Third Grade

Reading

The mean and median scale scores for the total population of students taking the 2011 third-grade Reading assessment are 559 and 569, respectively, with a standard deviation of 77.7. The mean scale score for female students is 568, with a standard deviation of 73.1, and the mean scale score for male students is 551, with a standard deviation of 81.0.

The scale score frequency distribution of the third-grade Reading assessment for the total population is shown in Table 159. Figure 30 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the distributions of scale scores for the total population and for each gender are slightly negatively skewed.

The mean scale score for the single content standard is 559, and the median is 569 (Table 155). The mean scale scores for the subcontent areas ranged from 550 to 586, and the median scale scores ranged from 568 to 569 (Table 156).

The mean percentages of the maximum obtainable raw score for the subcontent areas ranged from 51.4% to 74.9% (Table 158). The mean percentage of the maximum obtainable raw score for the total test was 57.5%.

Reading – Spanish

The mean scale score for the total population of students taking the 2011 third-grade Spanish Reading assessment is 522, with a standard deviation of 50.4. The mean scale score for female students is 530, with a standard deviation of 45.8, and the mean scale score for male students is 513, with a standard deviation of 53.6.

The scale score frequency distribution of the third-grade Spanish Reading assessment for the total population is shown in Table 160. Figure 31 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the

distributions of scale scores for the total population and for each gender are essentially normal, but with some floor effects.¹¹

The mean scale score for the single content standard is 522, and the median is 525. The mean scale scores for all the subcontent areas ranged from 520 to 522; the median scale scores for the subcontent areas ranged from 525 to 526, close to the median scale score of 525 for the total test.

The mean percentages of the maximum obtainable raw score for the subcontent areas ranged from 55.0% to 61.4%. The mean percentage of the maximum obtainable raw score for the total test was 58.6%.

Writing

The mean and median scale scores for the total population of students taking the 2011 third-grade Writing assessment are 467 and 466 respectively, with a standard deviation of 53.9. The mean scale score for female students is 475, with a standard deviation of 53.7, and the mean scale score for male students is 459, with a standard deviation of 53.1.

The scale score frequency distribution for the total population is shown in Table 161. Figure 32 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the distributions of scale scores for the total population and for each gender are approximately normal, but with some ceiling effects.¹²

The mean scale scores for the two content standards are 469 and 480. The mean scale scores for the subcontent areas ranged from 470 to 505. The median scale score ranged from 466 to 467 for the content standards, and from 466 to 470 for the subcontent areas.

The mean percentages of the maximum obtainable score for the content standards ranged from 75.0% to 81.4%. The mean percentages of the maximum obtainable raw score for the subcontent areas ranged from 76.0% to 81.2%. The mean percentage of the maximum obtainable raw score for the total test was 78.6%.

¹¹ Floor effects are indicated by a pileup of scores at the bottom of the scale, and suggest that the true ability of some of the tested students was lower than the lowest obtainable scale score.

¹² Ceiling effects are indicated by a pileup of scores at the top of the scale, and suggest that the true ability of some of the tested students was higher than the highest obtainable scale score.

Writing – Spanish

The mean and median scale scores for the total population of students taking the 2011 third-grade Spanish Writing assessment are 517 and 521, respectively, with a standard deviation of 74.4. The mean scale score for female students is 533, with a standard deviation of 70.3, and the mean scale score for male students is 500, with a standard deviation of 74.8.

The scale score frequency distribution of the third-grade Spanish Writing assessment for the total population is shown in Table 162. Figure 33 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are approximately normal.

The mean scale scores for the two content standards are 525 and 515, respectively, with median scale scores of 532 and 510. The mean scale scores for the subcontent areas ranged from 515 to 541, and the median scale scores for the subcontent areas varied between 511 and 556.

The mean percentages of the maximum obtainable raw scores ranged from 68.0% to 73.7% for the content standards, and from 69.1% to 74.3% for the subcontent areas. The mean percentage of the maximum obtainable raw score for the total test was 71.2%.

Mathematics

The mean and median scale scores for the total population of students taking the 2011 third-grade Mathematics assessment are 460 and 463, respectively, with a standard deviation of 88.8. The mean scale score for female students is 458, with a standard deviation of 86.7, and the mean scale score for male students is 462, with a standard deviation of 90.6.

The scale score frequency distribution for the total population is shown in Table 163. Figure 34 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are approximately normal.

The mean scale scores for the content standards ranged from 454 to 468, and the medians ranged from 453 to 466. Subcontent area scores are not computed for the grade 3 Mathematics test.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 54.9% to 69.7%. The mean percentage of the maximum obtainable raw score for the total test was 65.1%.

Fourth Grade

Reading

The mean and median scale scores for the total population of students taking the 2011 fourth-grade Reading assessment are 585 and 593, respectively, with a standard deviation of 63.4. The mean scale score for female students is 592, with a standard deviation of 58.5, and the mean scale score for male students is 579, with a standard deviation of 67.2.

The scale score frequency distribution for the total population is shown in Table 164. Figure 35 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the distributions of scale scores for the total population and for each gender are slightly negatively skewed.

The mean scale scores for the content standards ranged from 583 to 591. The mean scale scores for the subcontent areas ranged from 583 to 612. The median scale scores ranged from 593 to 594 for the content standards and for the subcontent areas.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 57.8% to 64.4%. The mean percentage of the maximum obtainable raw score for the total test was 61.6%. The mean percentages of the maximum raw score for the subcontent areas ranged from 57.0% to 71.8%.

Reading – Spanish

The mean and median scale scores for the total population of students taking the 2011 fourth-grade Spanish Reading assessment are 532 and 534, respectively, with a standard deviation of 32.7. The mean scale score for female students is 535, with a standard deviation of 35.8, and the mean scale score for male students is 528, with a standard deviation of 29.0.

The scale score frequency distribution for the total population is shown in Table 165. Figure 36 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the distributions of scale scores for the total population and for each gender are approximately normal.

The mean scale scores for the content standards ranged from 524 to 534. The mean scale scores for the subcontent areas ranged from 524 to 557. The median scale scores varied between 530 and 536 for the content standards and between 525 and 548 for the subcontent areas. The median for the total test scale score is 534.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 49.2% to 63.1%. The mean percentage of the maximum obtainable score for the total test was 55.4%. The mean percentages of the maximum raw score for the subcontent areas ranged from 49.4% to 72.1%.

Writing

The mean and median scale scores for the total population of students taking the 2011 fourth-grade Writing assessment are 491 and 492 respectively, with a standard deviation of 52.4. The mean scale score for female students is 500, with a standard deviation of 51.8, and the mean scale score for male students is 483, with a standard deviation of 51.6.

The scale score frequency distribution for the total population is shown in Table 166. Figure 37 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are approximately normal.

The mean scale scores for the content standards varied between 491 and 501. The mean scale scores for the subcontent areas ranged from 492 to 534. The median scale score ranged from 492 to 493 for content standards, and from 471 to 507 for the subcontent areas.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 65.4% to 81.3%. The mean percentage of the maximum obtainable raw score for the total test was 73.0%. The mean percentages of the maximum raw score for the subcontent areas ranged from 61.0% to 82.1%.

Writing – Spanish

The mean and median scale scores for the total population of students taking the 2011 fourth-grade Spanish Writing assessment are 508 and 510 respectively, with a standard deviation of 41.2. The mean scale score for female students is 510, with a standard deviation of 45.8, and the mean scale score for male students is 505, with a standard deviation of 35.5.

The scale score frequency distribution for the total population is shown in Table 167. Figure 38 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the distributions of scale scores are slightly negatively skewed.

The mean scale scores for the two content standards are 498 and 515. The mean scale scores for the subcontent areas ranged from 496 to 515. The

median scale scores for the two content standards are 504 and 517. The median scale scores for the subcontent areas varied between 505 and 510.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 51.5% to 55.1%. The mean percentage of the maximum obtainable raw score for the total test was 53.4%. The mean percentages of the maximum raw score for the subcontent areas ranged from 47.2% to 58.7%.

Mathematics

The mean and median scale scores for the total population of students taking the 2011 fourth-grade Mathematics assessment are 492 and 496, respectively, with a standard deviation of 78.8. The mean scale score for female students is 492, with a standard deviation of 77.2, and the mean scale score for male students is 492, with a standard deviation of 80.3.

The scale score frequency distribution for the total population is shown in Table 168. Figure 39 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are approximately normal.

The mean scale scores for the content standards ranged from 496 to 514. The mean scale scores for the subcontent areas ranged from 494 to 521. The median scale scores ranged from 497 to 498 for the content standards and from 492 to 498 for the subcontent areas.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 65.9% to 71.2%. The mean percentage of the maximum obtainable raw score for the total test was 69.2%. The mean percentages of the maximum raw score for the subcontent areas ranged from 64.7% to 74.3%.

Fifth Grade

Reading

The mean and median scale scores for the total population of students taking the 2011 fifth-grade Reading assessment are 610 and 618, respectively, with a standard deviation of 67.7. The mean scale score for female students is 616, with a standard deviation of 62.7, and the mean scale score for male students is 604, with a standard deviation of 71.7.

The scale score frequency distribution for the total population is shown in Table 169. Figure 40 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The

figure shows that the scale score distributions for the total population and for each gender are slightly negatively skewed.

The mean scale scores for the content standards ranged from 605 to 614. The mean scale scores for the subcontent areas ranged from 610 to 642. The median scale scores vary from 618 to 619 for the content standards and from 618 to 623 for the subcontent areas, with a median of 618 for the total test.

The mean percentages of the maximum obtainable raw score for content standards ranged from 49.4% to 67.7%. The mean percentage of the maximum obtainable raw score for the total test was 60.8%. The mean percentages of the maximum raw score for the subcontent areas ranged from 58.3% to 73.0%.

Writing

The mean and median scale scores for the total population of students taking the 2011 fifth-grade Writing assessment are both 511, with a standard deviation of 55.6. The mean scale score for female students is 522, with a standard deviation of 54.9, and the mean scale score for male students is 501, with a standard deviation of 54.3.

The scale score frequency distribution for the total population is shown in Table 170. Figure 41 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are approximately normal.

The mean scale scores for the content standards varied between 512 and 520. The mean scale scores for the subcontent areas ranged from 513 to 542. The median scale scores ranged from 510 to 512 for the content standards and from 510 to 542 for the subcontent areas. Most of the median scale scores for the content standards and subcontent areas are at or near the median of 511 for the total test.

The mean percentages of the maximum obtainable raw score for content standards ranged from 68.3% to 79.2%. The mean percentage of the maximum obtainable raw score for the total test was 73.5%. The mean percentages of the maximum raw score for the subcontent areas ranged from 65.0% to 78.8%.

Mathematics

The mean and median scale scores for the total population of students taking the 2011 fifth-grade Mathematics assessment are 521 and 525, respectively, with a standard deviation of 79.5. The mean scale score for female students is 521, with a standard deviation of 75.6, and the mean scale score for male students is 522, with a standard deviation of 83.0.

The scale score frequency distribution for the total population is shown in Table 171. Figure 42 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are approximately normal.

The mean scale scores for the content standards ranged from 522 to 540. The mean scale scores for the subcontent areas ranged from 531 to 543. The median scale scores vary from 525 to 527 for the content standards and from 524 to 533 for the subcontent areas.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 54.9% to 75.7%. The mean percentage of the maximum obtainable raw score for the total test was 65.1%. The mean percentages of the maximum raw score for the subcontent areas ranged from 64.4% to 71.4%.

Science

The mean and median scale scores for the total population of students taking the 2011 fifth-grade Science assessment are 496 and 502, respectively, with a standard deviation of 67.2. The mean scale score for female students is 494, with a standard deviation of 64.6, and the mean scale score for male students is 498, with a standard deviation of 69.5.

The scale score frequency distribution for the total population is shown in Table 172. Figure 43 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The distributions of the scale scores are approximately normal for the total population and for each gender.

The mean scale scores for the content standards ranged from 496 to 498. The mean scale scores for the subcontent areas ranged from 497 to 505. The median scale scores vary from 502 to 503 for the content standards and from 501 to 503 for the subcontent areas, and all are very close to the median scale score of 502 for the total test.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 53.5% to 59.4%. The mean percentage of the maximum obtainable raw score for the total test was 56.8%. The mean percentages of the maximum raw score for the subcontent areas ranged from 55.0% to 61.2%.

Sixth Grade

Reading

The mean and median scale scores for the total population of students taking the 2011 sixth-grade Reading assessment are 626 and 634, respectively, with a standard deviation of 65.2. The mean scale score for female students is 634, with a standard deviation of 60.8, and the mean scale score for male students is 618, with a standard deviation of 68.2.

The scale score frequency distribution for the total population is shown in Table 173. Figure 44 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are slightly negatively skewed.

The mean scale scores for the content standards ranged from 625 to 634. The mean scale scores for the subcontent areas ranged from 626 to 663. The median scale scores vary from 633 to 635 for the content standards, from 634 to 635 for the subcontent areas, and all are close to the median scale score of 634 for the total test.

The mean percentages of the maximum obtainable raw score for content standards ranged from 54.1% to 68.6%. The mean percentage of the maximum obtainable raw score for the total test was 62.0%. The mean percentages of the maximum raw score for the subcontent areas ranged from 57.8% to 71.8%.

Writing

The mean and median scale scores for the total population of students taking the 2011 sixth-grade Writing assessment are 529 and 530, respectively, with a standard deviation of 61.1. The mean scale score for female students is 542, with a standard deviation of 59.4, and the mean scale score for male students is 517, with a standard deviation of 60.2.

The scale score frequency distribution for the total population is shown in Table 174. Figure 45 graphically represents the scale score frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are approximately normal.

The mean scale scores for the content standards varied between 531 and 534. The mean scale scores for the subcontent areas ranged from 532 to 554. The median scale scores ranged from 529 to 530 for the content standards and from 530 to 566 for the subcontent areas.

The mean percentages of the maximum obtainable raw score for content standards ranged from 69.7% to 72.9%. The mean percentage of the maximum obtainable raw score for the total test was 71.2%. The mean percentages of the maximum raw score for the subcontent areas ranged from 67.2% to 74.5%.

Mathematics

The mean and median scale scores for the total population of students taking the 2011 sixth-grade Mathematics assessment are 539 and 544, respectively, with a standard deviation of 77.4. The mean scale score for female students is 540, with a standard deviation of 73.5, and the mean scale score for male students is 538, with a standard deviation of 80.9.

The scale score frequency distribution for the total population is shown in Table 175. Figure 46 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the distributions of scale scores for the total population and for each gender are approximately normal.

The mean scale scores for the content standards ranged from 536 to 550. The mean scale scores for subcontent areas ranged from 528 to 544. The median scale scores varied between 543 and 547 for the content standards and between 544 and 547 for the subcontent areas, and all are close to the median total test scale score of 544.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 52.8% to 66.3%. The mean percentage of the maximum obtainable raw score for the total test was 57.6%. The mean percentages of the maximum raw score for the subcontent areas ranged from 46.8% to 62.4%.

Seventh Grade

Reading

The mean and median scale scores for the total population of students taking the 2011 seventh-grade Reading assessment are 640 and 647, respectively, with a standard deviation of 65.3. The mean scale score for female students is 649,

with a standard deviation of 62.1, and the mean scale score for male students is 631, with a standard deviation of 67.1.

The scale score frequency distribution for the total population is shown in Table 176. Figure 47 graphically represents the frequency distributions for total population and for the groups of female and male students separately. The figure indicates that the distribution of the scale scores for the total population and for each gender is slightly negatively skewed.

The mean scale scores for the content standards ranged from 640 to 647. The mean scale scores for the subcontent areas ranged from 636 to 669. The median scale scores vary from 646 to 647 for the content standards and from 647 to 649 for the subcontent areas, and all are close to the median total test scale score of 647.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 57.0% to 70.6%. The mean percentage of the maximum obtainable raw score for the total test was 63.1%. The mean percentages of the maximum raw score for the subcontent areas ranged from 57.4% to 69.3%.

Writing

The mean and median scale scores for the total population of students taking the 2011 seventh-grade Writing assessment are both 553, with a standard deviation of 67.2. The mean scale score for female students is 569, with a standard deviation of 66.3, and the mean scale score for male students is 539, with a standard deviation of 64.8.

The scale score frequency distribution for the total population is shown in Table 177. Figure 48 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure indicates that the scale score distributions are approximately normal for the total population and for each gender.

The mean scale scores for the content standards ranged from 555 to 557. The mean scale scores for the subcontent areas ranged from 554 to 573. The median scale scores ranged from 552 to 554 for the content standards and from 500 to 554 for the subcontent areas. Most of the median scale scores for content standards and subcontent areas are close to the median total test scale score of 553.

The mean percentages of the maximum obtainable raw score for content standards ranged from 66.1% to 67.9%. The mean percentage of the maximum obtainable raw score for the total test was 66.9%. The mean percentages of the maximum raw score for the subcontent areas ranged from 58.9% to 72.3%.

Mathematics

The mean and median scale scores for the total population of students taking the 2011 seventh-grade Mathematics assessment are 559 and 564, respectively, with a standard deviation of 75.5. The mean scale score for female students is 560, with a standard deviation of 72.0, and the mean scale score for male students is 559, with a standard deviation of 78.7.

The scale score frequency distribution for the total population is shown in Table 178. Figure 49 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure indicates that the scale score distributions are approximately normal for the total population and for each gender.

The mean scale scores for the content standards ranged from 549 to 560. The mean scale scores for the subcontent areas ranged from 552 to 564. The median scale scores vary from 564 to 565 for the content standards and vary from 562 to 567 for the subcontent areas. All are close to the median total test scale score of 564.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 41.1% to 54.2%. The mean percentage of the maximum obtainable raw score for the total test was 48.0%. The mean percentages of the maximum raw score for the subcontent areas ranged from 38.0% to 50.1%.

Eighth Grade

Reading

The mean and median scale scores for the total population of students taking the 2011 eighth-grade Reading assessment are 652 and 657, respectively, with a standard deviation of 58.7. The mean scale score for female students is 663, with a standard deviation of 55.8, and the mean scale score for male students is 642, with a standard deviation of 59.7.

The scale score frequency distribution for the total population is shown in Table 179. Figure 50 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions are very slightly negatively skewed.

The mean scale scores for the content standards ranged from 653 to 655. The mean scale scores for the subcontent areas ranged from 654 to 663. The median scale scores vary from 654 to 658 for the content standards and from

655 to 657 for the subcontent areas. Most of the median scale scores for content standards and subcontent areas are close to the median total test scale score of 657.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 54.6% to 66.4%. The mean percentage of the maximum obtainable raw score for the total test was 62.8%. The mean percentages of the maximum raw score for the subcontent areas ranged from 60.1% to 69.2%.

Writing

The mean and median scale scores for the total population of students taking the 2011 eighth-grade Writing assessment are 564 and 563 respectively, with a standard deviation of 72.3. The mean scale score for female students is 579, with a standard deviation of 71.3, and the mean scale score for male students is 549, with a standard deviation of 70.3.

The scale score frequency distribution for the total population is shown in Table 180. Figure 51 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure indicates that the scale score distributions are approximately normal for the total population and for each gender.

The mean scale scores for the content standards ranged from 565 to 571. The mean scale scores for the subcontent areas ranged from 565 to 588. The median scale scores vary from 562 to 564 for the content standards and from 565 to 613 for the subcontent areas, and most are close to the median total test scale score of 563.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 66.1% to 75.3%. The mean percentage of the maximum obtainable raw score for the total test was 70.6%. The mean percentages of the maximum raw score for the subcontent areas ranged from 60.1% to 75.9%.

Mathematics

The mean and median scale scores for the total population of students taking the 2011 eighth-grade Mathematics assessment are 576 and 579, respectively, with a standard deviation of 67.3. The mean scale score for female students is 576, with a standard deviation of 63.8, and the mean scale score for male students is 575, with a standard deviation of 70.6.

The scale score frequency distribution for the total population is shown in Table 181. Figure 52 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The

scale score distributions are very slightly negatively skewed for the total population and for each gender.

The mean scale scores for the content standards ranged from 570 to 577. The mean scale scores for subcontent areas ranged from 562 to 580. The median scale scores varied between 579 and 580 for the content standards and between 578 and 580 for the subcontent areas, and all are close to the median total test scale score of 579.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 42.6% to 54.1%. The mean percentage of the maximum obtainable raw score for the total test was 47.6%. The mean percentages of the maximum raw score for the subcontent areas ranged from 36.7% to 54.4%.

Science

The mean and median scale scores for the total population of students taking the 2011 eighth-grade Science assessment are 500 and 506, respectively, with a standard deviation of 62.6. The mean scale score for female students is 498, with a standard deviation of 59.6, and the mean scale score for male students is 501, with a standard deviation of 65.3.

The scale score frequency distribution for the total population is shown in Table 182. Figure 53 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The distributions of the scale scores are slightly negatively skewed for the total population and for each gender.

The mean scale scores for the content standards ranged from 493 to 500. The mean scale scores for the subcontent areas ranged from 492 to 506. The median scale scores varied between 505 and 507 for the content standards and between 505 and 511 for the subcontent areas, with most very close to the median total test scale score of 506.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 40.0% to 58.1%. The mean percentage of the maximum obtainable raw score for the total test was 50.8%. The mean percentages of the maximum raw score for the subcontent areas ranged from 38.4% to 62.0%.

Ninth Grade

Reading

The mean and median scale scores for the total population of students taking the 2011 ninth-grade Reading assessment are 658 and 662, respectively, with a

standard deviation of 50.2. The mean scale score for female students is 666, with a standard deviation of 48.0, and the mean scale score for male students is 651, with a standard deviation of 51.2.

The scale score frequency distribution for the total population is shown in Table 183. Figure 54 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are slightly negatively skewed.

The mean scale scores for the content standards ranged from 658 to 666. The mean scale scores for the subcontent areas ranged from 655 to 679. The median scale scores varied between 661 and 662 for the content standards, varied between 661 and 669 for the subcontent areas, and almost all are close to the median total test scale score of 662.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 58.0% to 68.9%. The mean percentage of the maximum obtainable raw score for the total test was 60.7%. The mean percentages of the maximum raw score for the subcontent areas ranged from 49.3% to 72.1%.

Writing

The mean and median scale scores for the total population of students taking the 2011 ninth-grade Writing assessment are 568 and 569 respectively, with a standard deviation of 79.4. The mean scale score for female students is 584, with a standard deviation of 77.2, and the mean scale score for male students is 553, with a standard deviation of 78.5.

The scale score frequency distribution for the total population is shown in Table 184. Figure 55 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure indicates that the scale score distributions are approximately normal for the total population and for each gender.

The mean scale scores for the content standards ranged from 570 to 573. The mean scale scores for subcontent areas ranged from 571 to 595. The median scale scores are 569 for all of the content standards and ranged from 568 to 607 for the subcontent areas. Most are close to the median scale score of 569 for the total test. The median scale score for SA 6 (Extended Writing) was somewhat higher than the median for the total test score. It should be noted that the score for this subcontent area is computed on the basis of the four scores a student gets for his or her response to the extended writing prompt. Consequently, the scale score for this subcontent area is rather discrete.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 67.1% to 70.1%. The mean percentage of the maximum obtainable raw score for the total test was 68.5%. The mean percentages of the maximum raw score for the subcontent areas ranged from 63.6% to 76.3%.

Mathematics

The mean and median scale scores for the total population of students taking the 2011 ninth-grade Mathematics assessment are 576 and 581 respectively, with a standard deviation of 71.9. The mean scale score for female students is 576, with a standard deviation of 68.0, and the mean scale score for male students is 576, with a standard deviation of 75.5.

The scale score frequency distribution for the total population is shown in Table 185. Figure 56 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The scale score distributions are very slightly negatively skewed for the total population and for each gender.

The mean scale scores for the content standards ranged from 561 to 577. The mean scale scores for the subcontent areas are 553 to 578. The median scale scores varied between 580 and 583 for the content standards, and are 581 for all of the subcontent areas, with all of the medians identical to or very close to the median total test scale score of 581.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 37.0% to 52.5%. The mean percentage of the maximum obtainable raw score for the total test was 43.7%. The mean percentages of the maximum raw score for the subcontent areas ranged from 33.5% to 52.0%.

Tenth Grade

Reading

The mean and median scale scores for the total population of students taking the 2011 tenth-grade Reading assessment are 679 and 685 respectively, with a standard deviation of 54.3. The mean scale score for female students is 689, with a standard deviation of 50.2, and the mean scale score for male students is 670, with a standard deviation of 56.3.

The scale score frequency distribution for the total population is shown in Table 186. Figure 57 graphically represents the frequency distributions for total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are slightly negatively skewed.

The mean scale scores for the content standards ranged from 679 to 683. The mean scale scores for the subcontent areas ranged from 676 to 693. The median scale scores vary from 683 to 686 for the content standards and from 684 to 687 for the subcontent areas, and all are close to the median total test scale score of 685.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 56.7% to 66.3%. The mean percentage of the maximum obtainable raw score for the total test was 59.1%. The mean percentages of the maximum raw score for the subcontent areas ranged from 50.0% to 67.2%.

Writing

The mean and median scale scores for the total population of students taking the 2011 tenth-grade Writing assessment are both 574, with a standard deviation of 73.7. The mean scale score for female students is 590, with a standard deviation of 71.4, and the mean scale score for male students is 559, with a standard deviation of 72.7.

The scale score frequency distribution for the total population is shown in Table 187. Figure 58 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are approximately normal.

The mean scale scores for the content standards ranged from 574 to 585. The mean scale scores for the subcontent areas ranged from 576 to 603. The median scale scores varied between 573 and 575 for the content standards and between 576 and 589 for the subcontent areas, with most quite close to the median scale score of 574 for the total test.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 64.7% to 77.8%. The mean percentage of the maximum obtainable raw score for the total test was 71.0%. The mean percentages of the maximum raw score for the subcontent areas ranged from 59.1% to 81.2%.

Mathematics

The mean and median scale scores for the total population of students taking the 2011 tenth-grade Mathematics assessment are 592 and 597 respectively, with a standard deviation of 69.8. The mean scale score for female students is 590, with a standard deviation of 65.8, and the mean scale score for male students is 594, with a standard deviation of 73.4.

The scale score frequency distribution for the total population is shown in Table 188. Figure 59 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The figure shows that the scale score distributions for the total population and for each gender are approximately normal.

The mean scale scores for the content standards ranged from 579 to 591. The mean scale scores for the subcontent areas ranged from 564 to 591. The median scale scores varied between 596 and 598 for the content standards and between 576 and 598 for the subcontent areas, and most are close to the median total test scale score of 597.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 35.8% to 46.1%. The mean percentage of the maximum obtainable raw score for the total test was 41.4%. The mean percentages of the maximum raw score for the subcontent areas ranged from 26.0% to 43.0%.

Science

The mean and median scale scores for the total population of students taking the 2011 tenth-grade Science assessment are 496 and 504, respectively, with a standard deviation of 64.5. The mean scale score for female students is 496, with a standard deviation of 60.0, and the mean scale score for male students is 496, with a standard deviation of 68.5.

The scale score frequency distribution for the total population is shown in Table 189. Figure 60 graphically represents the frequency distributions for the total population and for the groups of female and male students separately. The distributions of the scale scores are slightly negatively skewed for the total population and for each gender.

The mean scale scores for the content standards ranged from 488 to 497. The mean scale scores for the subcontent areas ranged from 485 to 501. The median scale scores vary from 502 to 505 for the content standards and from 499 to 506 for the subcontent areas, and all are very close to the median total test scale score of 504.

The mean percentages of the maximum obtainable raw score for the content standards ranged from 37.3% to 54.3%. The mean percentage of the maximum obtainable raw score for the total test was 46.6%. The mean percentages of the maximum raw score for the subcontent areas ranged from 34.9% to 57.3%.

Correlations among Content Standards and among Subcontent Areas

Tables 190 through 220 show the correlations between the scale scores for the total test and for the various content standards and subcontent areas for each grade and content area. All content standards and subcontent areas are moderately to highly correlated, as would be expected.

For the English Reading assessments, the correlations among the various content standards ranged from 0.60 (in grade 4) to 0.77 (in grade 9). The correlations among the various English Reading subcontent areas ranged from 0.47 (in grade 9) to 0.76 (in grade 6).

For the third-grade Spanish Reading assessments, correlations among subcontent areas varied between 0.59 and 0.65. For the fourth-grade Spanish Reading assessments, the correlations among the various content standards varied between 0.46 and 0.66, and the correlations among subcontent areas varied between 0.505 and 0.78.

For the English Writing assessments, the correlation between content standards 2 and 3 ranged from 0.63 (grade 3) to 0.75 (grade 9). The correlations among the various English Writing subcontent areas varied between 0.37 (grade 8) and 0.67 (grade 9).

For the Spanish Writing assessments, the correlation between content standards 2 and 3 is 0.80 in grade 3 and 0.62 in grade 4. The correlations among the various Spanish Writing subcontent areas ranged from 0.20 (grade 4) to 0.63 (grade 3).

For the Mathematics assessments, the correlations among content standards ranged from 0.63 (grade 4) to 0.78 (grade 9). Correlations among the Mathematics subcontent areas ranged from 0.53 (grade 10) to 0.69 (grade 4).

Finally, for the Science assessments, the correlations among content standards ranged from 0.62 (grade 10) to 0.77 (grade 8). Correlations among the Science subcontent areas ranged from 0.52 (grade 8) to 0.71 (grade 10).

Part 8: Reliability and Validity Evidence

Part 8 describes reliability and validity evidence for the 2011 CSAP assessments. First, the total test and subgroup reliability coefficients are presented, measured by Cronbach's alpha, as an index of the internal consistency, followed by interrater reliability of constructed-response items, item-to-total score correlations, and items functioning differentially in the CSAP tests. The section further discusses the reliability in terms of standard error of measurement of scale scores.

Second, the test validity in terms of content-related validity, construct-related validity, factor structures, fit and DIF, divergent or discriminant validity, and predictive validity of the CSAP tests are described. Finally, the section is concluded by presenting results from classification consistency and accuracy analyses.

Total Test and Subgroup Reliability

Reliability is an index of the consistency of test results. A reliable test is one that produces scores that are expected to be relatively stable if the test is administered repeatedly under similar conditions. Cronbach's alpha is a frequently used measure of internal consistency. On the basis of a single administration of a test, Cronbach's alpha provides a reliability estimate that equals the average of all split-half coefficients that would be obtained on all possible divisions of the test into halves. Such a split-half coefficient would be obtained by correlating one half of the test with the other half and then adjusting the correlation with the Spearman–Brown formula so that it applies to the whole test (see Allen & Yen, 1979, pp. 83–88).

Total test reliability coefficients (in this case measured by Cronbach's alpha) may range from 0.00 to 1.00, where 1.00 refers to a perfectly consistent test. The data are based on representative samples from each grade (the calibration samples, which ranged from 88% to 100% of the total tested population for all grades and content areas), and are typical of the results obtained for all CSAP operational tests. The total test reliabilities of the operational forms were evaluated first by Cronbach's alpha (Cronbach, 1951) calculated as

$$\hat{\alpha} = \frac{k}{k-1} \left(1 - \frac{\sum \hat{\sigma}_i^2}{\hat{\sigma}_x^2} \right),$$

where k is the number of items on the test form, $\hat{\sigma}_i^2$ is the variance of item i , and $\hat{\sigma}_x^2$ is the total test variance. Achievement tests are typically considered to be of sound reliability when their reliability coefficients are in the range of 0.80 and

above. Tables 221 and 222 show Cronbach's coefficient alpha for all content standards and subcontent areas. At the state level, the total reliability coefficients for content areas ranged between 0.85 (grade 4 Spanish Writing) and 0.94 (grades 4 and 10 Reading and grades 4–6 and 8 Mathematics) with a median value of 0.93. Such a reliability coefficient range is indicative of high internal consistency and signifies that the CSAP tests produce relatively stable scores. The median coefficients for each content area and the ranges across grade levels are as follows:

Test	Median	Range
Reading (English)	0.93	(0.89–0.94)
Writing (English)	0.91	(0.90–0.93)
Mathematics	0.94	(0.91–0.94)
Science	0.93	(0.92–0.93)
Reading (Spanish)	0.89	(0.88–0.90)
Writing (Spanish)	0.89	(0.85–0.92)

Table 221 also shows the individual reliability coefficients for content standards at each grade level. Table 222 provides similar information for all of the subcontent areas. These coefficients tend to be somewhat lower than the coefficients for the total test scores. These results are consistent with the smaller numbers of items that contribute to each content standard and subcontent area.

As evidence that a test is performing similarly across various subgroups, the reliability values for these subgroups can be compared to those for the total population. The reliability measures are impacted by the population distribution and can be lowered when the subgroup is considerably less variable than the total population. However, one would expect the subgroup reliabilities to be adequately high for all groups. Tables 223 through 228 show the total test reliability estimates for each content area by disability, accommodation, free lunch eligibility, gender, language proficiency, and immigrant status. Even at the subgroup level, the ranges were generally quite similar. Of the 702 reliability coefficients in Tables 223 through 228, only five were lower than 0.80. Two of these were for students of limited English proficiency (LEP) on the grade 7 and grade 8 Writing tests ($\alpha=0.79$ and 0.76 respectively), one was for students of limited English proficiency (LEP) on the grade 8 Science test ($\alpha=0.79$), one was for students who are not English proficient (NEP) on the grade 10 Science test ($\alpha=0.74$), and one was for the small number of non-Hispanic white students ($n=11$) who took the grade 3 Spanish Reading test ($\alpha=0.70$).

The performance of accommodated and non-accommodated students with and without reported disabilities is summarized in Table 229. Overall, non-accommodated students scored higher than accommodated students in every grade and content area except for grade 3 Spanish Reading, where the mean score of students without a disability and without an IEP was slightly higher for

accommodated than for non-accommodated students.¹³ As shown in the table, the mean scores of students with reported disabilities were lower than the scores of students without reported disabilities in every grade and content area.

Among students with reported disabilities, the mean scores of students who did not receive accommodations were higher than the scores of students who received accommodations. However, this should not be interpreted as an indication that the testing accommodations were unhelpful, since it is likely that the disabilities of students receiving accommodations were more severe than those of students who were able to complete the test without accommodations.

It is noteworthy that the difference between the mean scores of students with and without reported disabilities was generally lower in the accommodated groups than in the non-accommodated groups.

Interrater Reliability, Item-to-Total Score Correlation, and DIF

Test scores always contain some amount of measurement error. This kind of error can be random or systematic. Standardization of assessments is meant to minimize random error that occurs because of random factors that affect a student's performance on the test. Systematic errors are inherent to examinees and are typically specific to some subgroup characteristic (e.g., students who need accommodations but are not offered them). Reliability refers to the degree to which students' scores are free from such effects and provides a measure of consistency. In other words, reliability helps to describe how consistent students' performance would be if the assessment were given over multiple occasions.

Item-specific reliability statistics include interrater reliability, item-to-total score correlation, and DIF. As discussed in Part 4, the interrater reliability across CR items in terms of the kappa and intraclass correlations is one way to measure the consistency of the handscoring. Tables 11 through 16 provide the results of rater reliability measures, which assess the agreement rates within a given administration, and Table 17 provides the results of rater severity analyses, which compare the scoring leniency across years. As previously mentioned, these results demonstrate that the CSAP tests have relatively high interrater reliability.

As shown in rater reliability Tables 11 through 16, the kappa for English Reading items range from 0.51 to 0.91 with a median value of 0.68. English Writing kappa values had a wider range, from 0.41 to 0.97, with a median of 0.69. (The lower kappa values for some writing items are associated with lower maximum score points.) The kappa values for Mathematics items range from 0.60 to 0.97 with a median value of 0.86, and Science items range from 0.42 to 0.95 with a median

¹³ It should be noted that the small numbers of students taking the Spanish tests make it difficult to draw any meaningful conclusions about group differences.

value of 0.73. On the Spanish versions, kappa ranged from 0.46 to 0.95 with a median of 0.74 for Reading and from 0.41 to 0.94 with a median of 0.67 for Writing.

Table 17 displays the consistency of the ratings assigned to the same papers in 2011 and when they were previously administered. The values of kappa for Reading items range from 0.56 to 0.92 with a median value of 0.85. For Writing items, the range is from 0.67 to 0.75, with a median value of 0.72. For Mathematics items, the range is from 0.73 to 0.98 with a median value of 0.86. For Science items, the range is from 0.65 to 0.85 with a median value of 0.76. The reasonable range of weighted kappa for rater leniency for most items is an indication that the standards applied in the scoring of the constructed-response items are quite stable within an administration and over time.

The item-to-total score correlation is an indication of the relationship between each item and the overall test. As discussed in Part 5 of this report, Tables 23 through 84 display the item-to-total score correlations (and *p*-values) for each grade and content area. Below each table are displayed the average values for these two statistics. Item-to-total score correlations are limited by the response distributions, and therefore tend to be lower among very easy and very difficult items. Thus, the *p*-values of the items are important to consider when reviewing the item-to-total score correlations. According to a study cited in Crocker and Algina (1986), if the average biserial correlation is in a range of about 0.30–0.40, the average *p*-value should ideally be between 0.40 and 0.60. Given that the mean item-to-total score correlations for test forms range from 0.30 to 0.45 for MC items and from 0.41 to 0.63 for CR items, with average *p*-values from 0.47 to 0.79 and from 0.33 to 0.79, respectively, the item-to-total score correlations and *p*-values are in a reasonable range.

The differential item functioning (DIF) statistic provides a measure of the systematic over- or under-performance of selected subgroups on individual test items. Items exhibiting DIF were avoided as much as possible when operational test forms were created. The CSAP 2011 DIF results are presented in a later section of Part 8.

Standard Error of Measurement

Another measure of reliability is the standard error of measurement (SEM). This statistic is a direct estimate of the degree of measurement error in a student's total score on a test. The SEM represents the number of score points about which a given score can vary, similar to the standard deviation of a score. The smaller the SEM, the smaller the variability and the higher the reliability. The SEMs are computed with the following formula:

$$SEM = SD_{SS}(\sqrt{1 - \hat{\alpha}}),$$

where SD_{SS} is the standard deviation of the scale score, and $\hat{\alpha}$ is the result of the calculation of Cronbach's alpha. The SEMs represent the total standard error of measurement in the scale score metric. The overall estimates of SEM are shown in Table 230. The scale scores and associated SEMs by content area and grade are shown in Tables 231 through 235. Tables 223 through 228 provide the SEM values for various subgroups by content area and grade. All SEMs are within reasonable limits.

It is most important to note the specific scale score SEM for each cut score. Table 236 shows the cut scores used for the proficiency levels at each grade and content area. Comparison of the SEMs at the proficient cut to the SEMs associated with other CSAP scale scores for each test reveal that these values near the cut score are among the lowest for most grades and content areas, meaning that the CSAP tests tend to measure most accurately near the cut score. This is a desirable quality when cut scores are used to classify examinees.

Test Validity

Validity refers to the degree to which evidence and theory support the interpretations of test scores entailed by proposed uses of tests. Validity is, therefore, the most fundamental consideration in developing and evaluating tests. The process of validation involves accumulating evidence to provide a sound scientific basis for the proposed score interpretations (AERA, APA, and NCME, 1999)

The purpose of test validation is not to validate the test itself but to validate interpretations of the test scores for particular purposes or uses. Test validation is not a quantifiable property but an ongoing process, beginning at initial conceptualization and continuing throughout the lifetime of an assessment. Every aspect of an assessment provides evidence in support of its validity (or evidence to the contrary), including design, content specifications, item development, and psychometric quality.

Content-Related Validity

Content-related validity in achievement tests is evidenced by a correspondence between test content and a specification of the content domain. To ensure such correspondence, the Colorado Department of Education conducted a comprehensive curriculum review. They met with educational experts to determine common educational goals and the knowledge and skills emphasized in curricula. The Colorado Model Content Standards and Assessment Frameworks are the outcomes of the process.

The Colorado Model Content Standards and Assessment Frameworks are the foundation for the CSAP assessments. All CSAP items are developed to

measure the content standards and are subject to numerous levels of scrutiny, both internal and external, before their operational use. All items are closely examined according to the “Criteria for Item Acceptability”¹⁴ to ensure the adequacy and relevancy of each item with respect to content, theme, wording, format, and style prior to formal review by Content and Bias Review panels. Through this process, all efforts are made to ensure test items are tightly aligned with the Colorado Model Content Standards. Tables 237 through 240 show for each content area test the number of score reporting categories (SRCs)¹⁵, the number of performance indicators (PIs) in each SRC, the number of items measuring each SRC, the number of PIs assessed by the current test, and, finally, the percentage of all PIs assessed. It may not be feasible to assess all PIs in a single test; however, as appropriate, efforts are made to assess all measurable PIs across years.

Construct Validity

Construct validity—the meaning of test scores and the inferences they support—is the central concept underlying the CSAP validation process. Evidence for construct validity is comprehensive and integrates evidence from both content- and criterion-related validity. For example, to demonstrate comprehensiveness, CSAP tests must contain items that represent essential instructional objectives. The following sections present evidence supporting content- and criterion-related validity.

Minimization of Construct-Irrelevant Variance and Under-Representation

Minimization of construct-irrelevant variance and construct under-representation is addressed in the following steps of the test development process: (1) specification, (2) item writing, (3) review, (4) field testing, (5) test construction, and (6) calibration. While the CSAP does not field test, the quality of the item pool used in the construction of the CSAP assessments is evidenced by the item analysis results and the low number of items suppressed during calibration.

Construct-irrelevant variance refers to error variance that is caused by factors unrelated to the constructs measured by the test. For example, when tests are not administered under standardized conditions (e.g., one administration may be timed, while another administration may be untimed), differences in student performance related to different administration conditions may result. Careful specification of content and review of the items under Plain Language

¹⁴ The *Criteria for Item Acceptability* is a checklist that is used to train item writers and to guide the development and review of items during test construction. A copy of the checklist is provided as an appendix to this report.

¹⁵ These score reporting categories correspond to the Colorado model content standards and subcontent areas listed in Table 1.

representing that content are first steps in minimizing construct-irrelevant variance. Then empirical evidence, especially item-level data, is used to infer construct irrelevance.

Construct under-representation occurs when the content of the assessment does not reflect the full range of content that the assessment is expected to cover. The CSAP is designed to represent the Colorado Model Content Standards. Specification and review, in which test blueprints are developed and reviewed, are primary steps in the development process designed to ensure that content is equitably represented.

Minimizing Bias through DIF Analyses

The position of CTB/McGraw-Hill concerning test bias is based on two general propositions. First, students may differ in their background knowledge, cognitive and academic skills, language, attitudes, and values. To the degree that these differences are large, no one curriculum and no one set of instructional materials will be equally suitable for all. Therefore, no one test will be equally appropriate for all. Furthermore, it is difficult to specify what amount of difference can be called large and to determine how these differences will affect the outcome of a particular test.

Second, schools have been assigned the tasks of developing certain basic cognitive skills and supporting development of these skills equitably among all students. Therefore, there is a need for tests that measure the common skills and bodies of knowledge that are common to all learners. The test publisher's task is to develop assessments that measure these key cognitive skills without introducing extraneous or construct-irrelevant elements into the performances on which the measurement is based. If these tests require that students have culture-specific knowledge and skills not taught in school, differences in performance among students can occur because of differences in student background and out-of-school learning. Such tests are measuring different things for different groups and can be called biased (Camilli & Shepard, 1994; Green, 1975). In order to lessen this bias, CTB/McGraw-Hill strives to minimize the role of the extraneous elements, thereby increasing the number of students for whom the test is appropriate. Careful attention is taken in the test construction process to lessen the influence of these elements for large numbers of students. Unfortunately, in some cases these elements may continue to play a substantial role.

Four measures were taken to minimize bias in the CSAP assessments. The first was based on the premise that careful editorial attention to validity is an essential step in keeping bias to a minimum. Bias can occur only if the test is measuring different things for different groups. If the test entails irrelevant skills or knowledge, however common, the possibility of bias is increased. Thus, careful attention was paid to content validity during the item-writing and item-selection process.

The second way bias was minimized was by following specific McGraw-Hill guidelines designed to reduce or eliminate bias. Item writers were directed to the following published guidelines: *Guidelines for bias-free publishing* (McGraw-Hill, 1983) and *Reflecting diversity: Multicultural guidelines for educational publishing professionals* (MacMillan/McGraw-Hill, 1993). Developers reviewed the CSAP assessment materials with these considerations in mind. Such internal editorial reviews were conducted by at least three different people or groups of people: a content editor, who directly supervised the item writers; a style editor; and a content supervisor. The final test was again reviewed by at least these same people as well as independently reviewed by a quality assurance editor.

As part of the standard CSAP test assembly process, items with poor statistical fit or distractors with positive item-to-total score correlations are avoided insofar as practicable since these item characteristics may indicate that an item is tapping ability irrelevant to the construct being measured. DIF with respect to subgroups might also indicate construct irrelevance. Items with these attributes are not selected or are given a lower priority for selection during the test construction stage. For the CSAP, particular scrutiny is given to the equating (or “anchor”) sets in each form, since these items impact the resulting scale scores developed for the entire test. Including DIF items in this equating set could have a greater impact on the overall fairness of the reported scores. The number of fit and DIF flagged items, including anchor items, included in the 2011 test assembly is presented in Table 9.

The third strategy for minimizing bias is to involve educational community professionals who represent various ethnic groups in the review of all new materials. These reviewers are asked to consider and comment on the appropriateness of language, subject matter, and representation of groups of people.

The fourth procedure for minimizing bias involves statistical procedures referred to as DIF analyses to evaluate differential item functioning in all of the CSAP tests. DIF studies include a systematic item analysis to determine if examinees with the same underlying level of ability have the same probability of getting the item correct. The use of items that have been flagged for DIF is minimized in the test development process. DIF studies have been done routinely for all major test batteries published by CTB/McGraw-Hill after 1970. All CSAP test items are analyzed for DIF in subgroups identified by gender, ethnicity, and disabilities.

Because the CSAP tests were built using IRT, DIF analyses that capitalized on the information and item statistics provided by this theory were implemented. There are several IRT-based DIF procedures, including those that assess the equality of item parameters across groups (Lord, 1980) and those that assess area differences between item characteristic curves (Camilli & Shepard, 1994; Linn, Levine, Hastings, & Wardrop, 1981). However, these procedures require a

minimum of 800–1,000 cases in each group of comparison to produce reliable and consistent results. In contrast, the Linn–Harnisch procedure (Linn & Harnisch, 1981) utilizes the information provided by the three-parameter IRT model but requires fewer cases. This procedure was used to complete the DIF studies for the 2011 CSAP tests.

After the administration of new forms, all items were evaluated for poor item statistics, fit, and DIF. The items flagged for fit and DIF were noted in the item analyses report and item pool to enable content experts to reevaluate the items for future selection.

Linn–Harnisch DIF Method

An example of Linn–Harnisch procedure for gender DIF analyses for multiple-choice items is described below.

The parameters for each item (a_i , b_i , and c_i) and the trait or scale score (θ) for each examinee are estimated for the three-parameter logistic model:

$$P_{ij}(\theta) = c_i + \frac{1 - c_i}{1 + \exp[-1.7a_i(\theta_j - b_i)]},$$

where $P_{ij}(\theta)$ is the probability that examinee j , with a given value of θ , will obtain a correct score on item i . Note that the item parameter estimates are based on data from the total sample of valid examinees. The sample is then divided into gender groups, and the members in each group are sorted into 10 equal score categories (deciles) based on their location on the score scale (θ). The expected proportion correct for each group based on the model prediction is compared to the observed (actual) proportion correct obtained by the group.

The proportion of people in decile g who are expected to answer item i correctly is

$$P_{ij} = P_{ig}(\theta) = \frac{1}{n_g} \sum_{j \in g} P_{ij}(\theta),$$

where n_g is the number of examinees in decile g . The formula to compute the proportion of students expected to answer item i correctly (over all deciles) for a group (e.g., female) is given by

$$P_i = P_i(\theta) = \frac{\sum_{g=1}^{10} n_g P_{ig}(\theta)}{\sum_{g=1}^{10} n_g}.$$

The corresponding observed proportion correct for examinees in a decile (O_{ig}) is the number of examinees in decile g who answered item i correctly divided by the number of people in the decile (n_g). That is,

$$O_{ig} = \frac{\sum_{j \in g} u_{ij}}{n_g},$$

where u_{ij} is the dichotomous score for item i for examinee j .

The corresponding formula to compute the observed proportion answering each item correctly (over all deciles) for a complete gender group is given by

$$O_{i.} = \frac{\sum_{g=1}^{10} n_g O_{ig}}{\sum_{g=1}^{10} n_g}.$$

After the values are calculated for these variables, the difference between the observed proportion correct (for gender) and expected proportion correct can be computed. The decile group difference (D_{ig}) for observed and expected proportion correctly answering item i in decile g is

$$D_{ig} = O_{ig} - P_{ig},$$

and the overall group difference (D_i) between observed and expected proportion correct for item i in the complete group (over all deciles) is

$$D_{i.} = O_{i.} - P_{i.}.$$

These indices are indicators of the degree to which members of gender groups perform better or worse than expected on each item, based on the parameter estimates from all subsamples. Differences for decile groups provide an index for each of the ten regions on the score (θ) scale. The decile group difference (D_{ig}) can be either positive or negative. Use of the decile group differences as well as the overall group difference allows one to detect items that give a large positive difference in one range of θ and a large negative difference in another range of θ , yet have a small overall difference.

A generalization of the Linn and Harnisch's (1981) procedure was used to measure DIF for constructed-response items.

Differential Item Functioning Ratings and Results

DIF is defined in terms of the decile group and total target subsample differences, the D_{i-} (sum of the negative group differences) and D_{i+} (sum of the

positive group differences) values, and the corresponding standardized difference (Z_i) for the subsample (see Linn & Harnisch, 1981, p. 112). Items for which $|D_i| \geq 0.10$ and $|Z_i| \geq 2.58$ are identified as possibly biased. If D_i is positive, the item is functioning differentially in favor of the target subsample. If D_i is negative, the item is functioning differentially against the target subsample.

The DIF analyses¹⁶ were conducted for African Americans, Hispanics, Asians, Native Americans, males, and females. Table 241 provides an overview of items flagged for ethnicity DIF in the various assessments based on the entire student population, and Table 242 presents an overview of items flagged for gender DIF. The results for each assessment are briefly described below.

On the Reading assessments, DIF was observed in every grade. Across all grades, two items favored Indian/Alaska Native students; 31 items favored Asian students; eight items favored African American students; three items favored and one disfavored Hispanic students; five favored and five disfavored Hawaiian/Pacific Islander students; eight items favored female students; and six items disfavored male students.

On the Writing assessments, DIF was observed in grades 4 through 10. Across all grades, five items favored and seven disfavored Asian students; two items favored Hispanic students; four items favored and four disfavored Hawaiian/Pacific Islander students; eight items favored female students; and eight items disfavored male students.

On the Mathematics assessments, DIF was observed in every grade except grade 7. Across the grades showing DIF, one item disfavored American Indian/Alaska Native students; two items favored and three disfavored Asian students; three items favored and four disfavored African American students; and two items favored and three disfavored Hawaiian/Pacific Islander students. None of the Mathematics assessments were flagged for gender DIF.

On the Science assessments, items exhibited DIF in all three grades. Four items favored and one disfavored Asian students; one item favored African American students; two items favored Hispanic students; one item favored and three disfavored Hawaiian/Pacific Islander students; three items favored female students; and one item disfavored male students.

Additional DIF analyses are presented in Tables 243 (Accommodations), 244 (Primary Disability State), 245 (Enrollment), 246 (Language Proficiency), 247 (Education Plan), and 248 (Homeless, Immigrant, Migrant, and Free Lunch Eligible).

¹⁶ DIF analyses are not reported for the Spanish Reading and Writing assessments because of small case counts and relative homogeneity of the examinees for these tests.

Internal Factor Structure and Unidimensionality of the CSAP Assessment

Analyses of the internal structure of a test can indicate the extent to which the relationships among test items and components conform to the construct the test purports to measure. Educational assessments are usually designed to measure a single overall construct or domain (e.g., Reading achievement). CSAP test items are calibrated using a unidimensional IRT model, which posits the presence of an essentially unidimensional construct underlying a group of test items and components. Unless tests are designed to have a complex internal structure, a measure of item homogeneity is relevant to validity. The internal consistency coefficient is a measure of item homogeneity. In order for a group of items to be homogeneous, they must measure the same construct (construct validity) or represent the same content domain (content validity).

To assess the overall factor structure of the CSAP assessments, exploratory factor analyses were conducted for each content and grade. Polychoric correlations were obtained, and a principal components analysis was conducted. The resulting eigenvalues for each factor are an indication of the relative proportion of variance accounted for by each successive factor. Figures 61 through 91 contain plots of the eigenvalues (part a) and proportions of variance (part b) for each factor identified in these analyses. These figures show that each of the CSAP tests (English versions) demonstrated a strong single factor, accounting for approximately 26% to 50% of the overall variance, providing evidence that the items in each test are measuring a single construct. The variance accounted for by the single factor for grades 3 and 4 Spanish Reading and Writing tests was slightly lower, ranging from 19% to 33%. However, the number of examinees taking the Spanish tests was so small that the factor analyses should be interpreted with extreme caution.

IRT Model to Data Fit as an Evidence of Test Score Validity

When IRT models are used to calibrate test items and to report student scores, demonstrating item fit is also relevant to construct validity. That is, the extent to which test items function as the IRT model prescribes is relevant to the validation of test scores. As part of the scaling process, all CSAP items were examined closely with respect to classical (i.e., p -value and item-to-total score correlation) and IRT (Q1) fit indices. Items judged to be poorly fit by the model were visually inspected to decide whether the misfit was substantive in origin or from irrelevant sources such as extreme expectations that often accompany extremely easy or hard items. Very few items (fewer than 4%) on the 2011 assessments were flagged for poor model fit, indicating that the test items were adequately scaled by the unidimensional IRT models, and the resulting scores are interpretable and valid. IRT fit statistics are discussed in greater detail in Part 6 of this Technical Report. Summaries of the IRT fit statistics are presented in Tables 85 through 146.

Divergent (Discriminant) Validity

Measures of different constructs should not be highly correlated with each other. Divergent validity is a subtype of construct validity that can be estimated by the extent to which measures of constructs that theoretically should not be related to each other are, in fact, observed as not related to each other. Typically, correlation coefficients among measures are examined in support of divergent validity.

To assess the divergent validity of the CSAP tests, scale scores were obtained and correlated for students who took various CSAP content area tests in 2011. Tables 249 and 250 show the intercorrelations among content areas (scale scores and percentile ranks) by grade level. The correlation coefficients among scale scores ranged from 0.72 (between Reading and Mathematics in grade 3) to 0.87 (between Reading and Writing in grade 9). The correlation coefficients suggest that individual student scores for Reading, Mathematics, Writing, and Science are moderately to highly related. These coefficients are not so low as to call into question whether these tests are tapping into achievement constructs and not so high as to arouse suspicion that the intended constructs are not distinct.

It is worth noting that the correlation coefficients between Reading and Writing were consistently higher than those between Mathematics and Reading and between Mathematics and Writing. It is also interesting to note that Science was correlated with Reading and Mathematics to a similar degree; however, the correlation between Science and Writing was relatively lower. A similar pattern of correlations has been observed in *TerraNova* (CTB/McGraw-Hill, 2001).

Additional evidence of divergent validity can be obtained by evaluating the correlations of test scores with extraneous demographic variables. Correlations were computed between total scale scores and age, gender, and ethnic group. Overall, these correlations were found to be somewhat small, ranging from nearly -0.36 to 0.09 (Table 251). The fact that these correlations are generally greater than zero in absolute terms can be attributed to differences in the overall ability of the various groups.

Predictive Validity

Predictive validity is a type of criterion-related validity that refers to the degree to which test scores predict criterion measurements that will be made at some point in the future (Crocker & Algina, 1986). In the context of annual assessment of student proficiency in a content area, the extent to which test scores in a year are predictive of those in the subsequent year can provide evidence for predictive validity. Colorado Model Content Standards in Mathematics, Reading, and Writing are designed to be incremental and progressive from lower to higher grade level, which is the basis for vertical scaling and measuring student growth

across years on a common scale. Table 252 shows predictive validity coefficients measured as the correlation between test scores for two adjacent years (2010 and 2011) on the basis of a group of students matched on student ID data. Spanish tests are excluded from this table because of the very small number of matched students ($N < 40$).

Factors affecting the measures of predictive validity include the time interval between assessments, reliability of assessments, differential individual and school effects, and so on. The correlation coefficients reported in Table 252 indicate strong predictability of test scores between two adjacent years. The validity coefficients (corrected for attenuation) range from 0.83 to 0.96 for all English content areas and grades indicating a high level of prediction from one year to the next.

Classification Consistency and Accuracy

One of the cornerstones of the No Child Left Behind Act of 2001 (2002) is the measurement of adequate yearly progress (AYP) with respect to the percentage of students at or above performance standards set by states. Because of this heavy emphasis on the classification of student performance, a psychometric property of particular interest is how consistently and accurately assessment instruments can classify students into performance categories.

Classification consistency is defined conceptually as the extent to which the performance classifications of students agree given two independent administrations of the same test or two parallel test forms. That is, if students are tested twice on the same test or on two parallel tests, what is the likelihood of classifying the students into the same performance categories? It is, however, virtually impractical to obtain data from repeated administrations of the same or parallel forms because of cost, testing burden, and effects of student memory or practice. Therefore, a common practice is to estimate classification consistency from a single administration of a test.

When a method to estimate decision consistency is applied, a contingency table of $(H + 1) \times (H + 1)$ is constructed, where H is the number of cut scores. For example, with three cut scores, a 4-by-4 contingency table can be built as follows:

Contingency Table with Three Cut Scores

	Level 1	Level 2	Level 3	Level 4	Sum
Level 1	P_{11}	P_{21}	P_{31}	P_{41}	$P_{.1}$
Level 2	P_{12}	P_{22}	P_{32}	P_{42}	$P_{.2}$
Level 3	P_{13}	P_{23}	P_{33}	P_{43}	$P_{.3}$
Level 4	P_{14}	P_{24}	P_{34}	P_{44}	$P_{.4}$
Sum	$P_{1.}$	$P_{2.}$	$P_{3.}$	$P_{4.}$	1.0

It is common to report two indices of classification consistency: the classification agreement P and coefficient kappa. Hambleton and Novick (1973) proposed P as a measure of classification consistency, where P is defined as the sum of diagonal values of the contingency table:

$$P = P_{11} + P_{22} + P_{33} + P_{44}$$

To reflect statistical chance agreement, Swaminathan, Hambleton, and Algina (1974) suggest using Cohen's kappa (Cohen, 1960):

$$\text{kappa} = \frac{P - P_c}{1 - P_c},$$

where P_c is the chance probability of a consistent classification under two completely random assignments. This probability, P_c , is the sum of the probabilities obtained by multiplying the marginal probability of the first administration and the corresponding marginal probability of the second administration:

$$P_c = (P_{1.} \times P_{.1}) + (P_{2.} \times P_{.2}) + (P_{3.} \times P_{.3}) + (P_{4.} \times P_{.4}).$$

Classification accuracy is defined as the extent to which the actual classifications of test takers agree with those that would be made on the basis of their true scores (Livingston & Lewis, 1995). That is, classification consistency refers to the agreement between two observed scores, while classification accuracy refers to the agreement between observed and true scores. Since true scores are unobservable, a psychometric model is typically used to estimate them on the basis of observed scores and the parameters of the model being used.

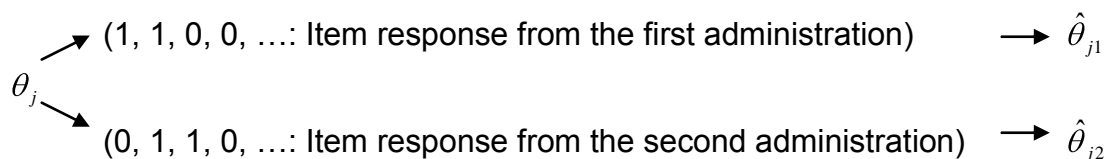
Classification Consistency and Accuracy When Pattern Scoring Is Used

A variety of IRT scoring procedures are available for estimating student proficiency scores. Two of the most popular score estimation techniques are item-pattern (IP) scoring and number-correct (NC) scoring under the IRT framework. NC scoring considers only how many items a student answered correctly (or the sum of item scores) in determining his or her score. In contrast, the IP scoring method takes into account not only a student's total raw score but also which items he or she got right.

Several methods have been proposed to measure classification consistency and accuracy on the basis of number-correct (summed) scores. However, few studies have proposed methods for IP scoring. Kolen and Kim (2004) developed a method to estimate classification consistency and accuracy when IP scoring is used. The following describes the Kolen–Kim method:

Step 1: Obtain ability distribution weight ($\hat{g}(\theta)$) at each quadrature (θ_j) point j .

Step 2: At each quadrature point θ_j , generate two sets of item responses using the item parameters from a test form, assuming that the same test form was administered twice to examinees with the true ability θ_j .



If two parallel (or alternative) forms were used, the two response patterns can be generated on the basis of the item parameters from the two forms. Estimate $\hat{\theta}_{j1}$ and $\hat{\theta}_{j2}$ for the two sets of item responses.

Step 3: Construct a classification matrix (as shown in the example below) at each quadrature point (θ_j). Determine the joint probability for the cells in the example below using the two ability estimates obtained from Step 2.

Classification Table for One Cut Point (C_1)¹⁷

	First administration or Form 1		
	$\hat{\theta}_{j1} \geq C_1$	$\hat{\theta}_{j1} < C_1$	
$\hat{\theta}_{j2} \geq C_1$			Second administration, or Form 2
$\hat{\theta}_{j2} < C_1$			

Step 4: Repeat Steps 2 and 3 r times and compute average values over r replications. r should be a large number, for example, 500, to obtain stable results.

Step 5: Multiply the distribution weight ($\hat{g}(\theta)$) by the average values obtained in Step 4 for each quadrature point, and sum the results across all quadrature points. From these results a final contingency table can be constructed and classification consistency indices, such as kappa, can be computed. In addition, because examinees' abilities are estimated at each quadrature point, this quadrature point can be considered the true score. Therefore, classification accuracy may be computed using both

¹⁷ This table is constructed for each quadrature point and replication. One, and only one, cell will have a value of one, with zeros elsewhere.

examinees' estimated abilities (observed scores) and quadrature points (true scores).

Table 253 (composed of two tables) includes the classification consistency and accuracy measures for CSAP grade 3 Reading. The first table is a contingency table with all three cut scores prepared using the Kolen–Kim method. The rows represent the first administration of an assessment, and the columns represent the second administration of the same assessment to the same students. As mentioned above, in the procedure by Kolen and Kim, the score distributions for the first administration and the second administration are estimated using simulation. So, the value in each cell represents the probability of belonging to certain performance levels in two hypothetical administrations. For example, 0.0459 represents the probability of belonging to “Unsatisfactory” in both first and second administrations. The 0.0117 represents the probability of belonging to “Unsatisfactory” in the first administration and “Partially Proficient” in the second administration. “Sum” is obtained simply by adding the four row values or the four column values. The “Observed Score Dist.” row shows the distribution of real data belonging to each performance level. In general, it is expected that the sum values and the distribution of observed scores from real data will be similar to one another. For example, the absolute differences between the sum values and the corresponding observed scores in Table 253 for the Proficient level are 0.0268 (0.6669 vs. 0.6401) and 0.0155 (0.6669 vs. 0.6514). The largest differences were found in the Advanced level, with absolute differences of 0.1335 (0.0607 vs. 0.1942) and 0.1239 (0.0607 vs. 0.1846).

The second table shows indices for classification consistency and classification accuracy. Each index was described above. The values in “All Cuts” were obtained by applying all three cut points simultaneously during analysis. From Table 253, classification agreement (P) for grade 3 Reading is 0.7863, chance probability is 0.4675, kappa is 0.5986, and classification accuracy is 0.8530, when all three cuts were used for computation. Because there are only two levels of classification when only one cut is applied, the values for P , decision accuracy, obtained with all three cuts are smaller than those obtained with only one cut. This explanation is the same for tables for all grade levels and content areas (Tables 253 through 283).

Part 9: Special Study

Part 9 presents results from a special study that investigated the reasons for unstable scale scores in the Extended Writing subcontent area in Writing tests, which were composed of a small number of constructed-response items.

Writing Trend Study

The CSAP incorporates the philosophy of multiple measures of a construct. All CSAP assessments are composed of multiple-choice item types. The CSAP Writing assessments consist of a mixture of multiple-choice (MC) and constructed-response (CR) items measuring the total writing proficiency and skills at various content standards and subcontent areas (e.g., Write Using Conventions, Paragraph Writing, Extended Writing, and Grammar and Usage). CR items in the CSAP take different forms and solicit varying response lengths. Compared to other statewide writing assessments, for example, single-prompt extended writing, the CSAP Writing assessment taps into a variety of writing skills using various item formats.

In addition to providing an overall measure of writing ability, the CSAP provides subscores at various content standards and subcontent areas to provide more diagnostic information on the examinee's writing ability. The subscores are derived on the basis of the examinee's performance on subsets of items, typically composed of a mixture of MC and CR items of various lengths. One exception is the Extended Writing subcontent area, which is measured only by a small number of CR items. It has been observed historically that the score in the Extended Writing subcontent area is unstable across administrations. That is, the historical trends on this subcontent area have fluctuated more radically than the overall construct, the other content standards, and the other subcontent areas. Furthermore, the trends on the subcontent area did not coincide with those on the overall test or other subcontent areas.

At the request of the CSAP Technical Advisory Committee (TAC), a study in English Writing was conducted to explore the unstable trends of the Extended Writing subcontent area in 2011. Grade 3 Writing does not include the Extended Writing subcontent area, so the study was conducted on grades 4 through 10. In this study, the Extended Writing (SA6) was examined as a single subcontent area and also was combined into a new subcontent area that also included the more stable Paragraph Writing (SA 5). That is, a new subcontent area was formed by collapsing the two subcontent areas and the items contributing to them. Scores for this new combined SA 5/SA 6 subcontent area were generated for the past nine years (2002 through 2011). The results in mean and median scale scores are presented in Table 284. Median scores were examined

because subcontent scores tend to be affected unduly by extreme scores. Median scale scores are also presented in Figures 92 through 98. Although the median scale scores on the Extended Writing subcontent area differ markedly from scores in the other areas and show much greater fluctuation across year, the combined score on Extended Writing and Paragraph Writing is much more stable. Because of the increased number of items in the combined subcontent area, the stability of the scores across years is improved considerably, and the fluctuations in difficulty are reduced at every grade level. As shown in Figures 92 through 98, the median scores on the combined Extended Writing/Paragraph Writing are quite stable across years and very similar to the scores on the total test and on the other subcontent areas.

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