Unit Title: Transform the World

Extended Evidence Outcomes

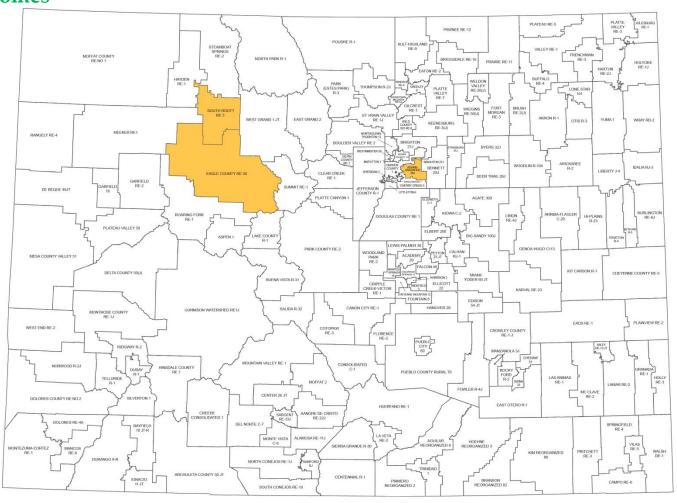
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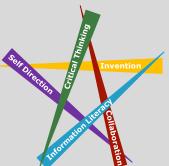


This unit was authored by a team of Colorado educators. The template provided one example of unit design that enabled teacherauthors to organize possible learning experiences, resources, differentiation, and assessments. The unit is intended to support teachers, schools, and districts as they make their own local decisions around the best instructional plans and practices for all students.

DATE POSTED: NOVEMBER 2015

Content Area	Mathematics-Extended Evidence Outcomes			
Course Name/Course Code				
Standard	Grade Level Expectations (GLE)			GLE Code
1. Number Sense, Properties,	1. The complex number system includes real numbers and ima	MA10-GR.HS-S.1-GLE.1		
and Operations	2. Quantitative reasoning is used to make sense of quantities a	MA10-GR.HS-S.1-GLE.2		
Patterns, Functions, and Algebraic Structures	Functions model situations where one quantity determines graphically, and using tables	MA10-GR.HS-S.2-GLE.1		
	2. Quantitative relationships in the real world can be modeled	MA10-GR.HS-S.2-GLE.2		
	3. Expressions can be represented in multiple, equivalent form	MA10-GR.HS-S.2-GLE.3		
	4. Solutions to equations, inequalities and systems of equation	MA10-GR.HS-S.2-GLE.4		
3. Data Analysis, Statistics, and	1. Visual displays and summary statistics condense the information	MA10-GR.HS-S.3-GLE.1		
Probability	2. Statistical methods take variability into account supporting i quantitative studies designed to answer specific questions	MA10-GR.HS-S.3-GLE.2		
	3. Probability models outcomes for situations in which there is	MA10-GR.HS-S.3-GLE.3		
4. Shape, Dimension, and Geometric Relationships	Objects in the plane can be transformed, and those transfor mathematically	MA10-GR.HS-S.4-GLE.1		
	2. Concepts of similarity are foundational to geometry and its a	MA10-GR.HS-S.4-GLE.2		
	3. Objects in the plane can be described and analyzed algebraic	MA10-GR.HS-S.4-GLE.3		
	4. Attributes of two- and three-dimensional objects are measurable and can be quantified			
		MA10-GR.HS-S.4-GLE.5		

Colorado 21st Century Skills



Critical Thinking and Reasoning: *Thinking Deeply, Thinking Differently*

Information Literacy: *Untangling the Web*

Collaboration: Working Together, Learning

Together

Self-Direction: Own Your Learning

Invention: Creating Solutions

Mathematical Practices:

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

Unit Titles	Length of Unit/Contact Hours	Unit Number/Sequence
Transform the World	8 weeks	6

This High School Mathematics unit Transform the World was developed with adaptations for students who have Significant Support Needs. A way to ensure that these students receive high quality instruction when they are in learning environments with same aged typical peers is by using the Extended Evidence Outcomes and Extended Evidence Competencies that were developed to address their learning needs through standards used by typical students their age. The original source for the Extended Evidence Outcomes and Extended Evidence Competencies was the Mathematics with EEOs document that can be accessed via a link on this page: http://www.cde.state.co.us/cdesped/InstructionalStandards. The adaptations suggested in this unit will not automatically meet the needs of every student but differing needs can usually be addressed by collaboration between special and general educators.

Some parameters that were adhered to when developing these adaptations were an attempt to emphasize principals of universal design and to focus on materials and activities that were free or very inexpensive and would be available to all teachers across the state. There was also an attempt to avoid making the unit overly complex and to keep it a reasonable length. For that reason some Assistive Technology items commonly used by SSN students were not mentioned due to possible problems with cost and availability in various settings,

Adaptations to this unit were created that focus specifically on the Extended Evidence Outcomes. The Extended Evidence Outcomes generally tend to focus more on academic skills and the suggestions for materials and activities made in this unit were made to match or parallel the lessons and activities for typical seventh graders. By contrast the Extended Evidence Competencies tend to focus on SSN students whose needs were more in the area of gaining skills in connecting meaning to symbols, the use of symbolic language in communication, participating in mathematical activities and exploring mathematical materials.

The adaptations suggested in this unit do not specifically address the Extended Evidence Competencies (Content Based Access Skills) that are also listed in the Academic Standards with EEO's document. When working with students whose needs fit best with the Extended Evidence Competencies (Content Based Access Skills) collaboration is particularly essential. Some students may need specialized materials and equipment that may vary substantially from one student to another. Listing the substantial number of possibilities was beyond the scope of this adapted unit and could best be addressed with collaboration with members of the student's special ed. team.

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Unit Title	Transform the World		Length of Unit	Length of Unit 8 weeks	
Focusing Lens(es)	Justification Transformation	Standards and Grade Level Expectations Addressed in this Unit	MA10-GR.HS-S.4-GLE.1		
Inquiry Questions (Engaging- Debatable):	 How do architectural engineers use transformations? (MA10-GR.HS-S.4-GLE.1) SSN: How would it helpful for someone planning to build a building to be able to talk about shapes precisely? 				
Unit Strands	Geometry: Congruence				
Concepts	Algebraic representations, model, transformation, coordinate plane, angles, side lengths, congruency, definitions, proofs SSN: transformation or change, angles, line, segment, , rotating, same, similar, reflecting, resizing, parallel, perpendicular, intersection, length, measure				

Generalizations My students will Understand that	Guiding Questions Factual Conceptual		
Algebraic representations model geometric transformations performed on a coordinate plane. (MA10-GR.HS-S.4-GLE.1-EO.a) SSN: Number sentences can explain how to turn, flip or slide a shape using coordinates on a graph paper.	On a coordinate plane, what algebraic description describes a translation? Rotation? Reflection? What is the effect on the x and y coordinates of a point when applying rotations, reflections or translations? SSN: How does sliding, turning, or flipping change a shape, what remains the same?	Why is it useful to describe transformations on a coordinate plane? How is it possible for different compositions of transformations to be equivalent? Why is a rotation of 180 degrees equivalent to a reflection over the x-axis combined with a reflection over the y-axis? SSN: Why does turning, sliding or flipping a shape not change the sides or angle of a shape?	
Sequences of transformations or combinations of angles and side lengths can determine the congruence of shapes. (MA10-GR.HS-S.4-GLE.1-EO.b) SSN: Measuring angles and lengths of sides of shapes help mathematicians know if two shapes are the same even if they look different because of a turn, slide or flip.	What transformations preserve shape and size? How can you determine if a transformation preserves shape and size? What combinations of sides and angles are sufficient to prove congruency of triangles? How can congruence between shapes be shown through indirect comparison? SSN: Which kinds of changes (transformations) in how a shape looks really keep the shape the same, even if it is in a different position?	Why can transformations determine if two figures are congruent? Why do combinations of sides and angles prove congruency of triangles? Why are some combinations of angles and sides sufficient to prove congruency while others are not? SSN: How can shapes be different in the way we measure them? Do we need to use different tools for different attributes of a shape (e.g., ruler for sides, protractor for angles)?	

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Precise definitions of basic geometric concepts facilitate
the development of careful proofs. (MA10-GR.HS-S.4-
GLE.1-EO.c)

SSN: Definitions about attributes of shapes help prove things about the shapes.

What is an angle? What is a triangle? What is a parallelogram?

SSN: What are parallel lines? What does an intersection look like? What are perpendicular lines?

How do definitions contribute to the development of a proof?

SSN: If we have a rule about a shape in geometry or a definition that everyone accepts, why can that help us prove something in geometry?

Key Knowledge and Skills: My students will...

What students will know and be able to do are so closely linked in the concept-based discipline of mathematics. Therefore, in the mathematics samples what students should know and do are combined.

- Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc. (MA10-GR.HS-S.4-GLE.1-EO.a.i)
- SSN: Identify parallel, intersecting and perpendicular lines (MA10-GR.HS-S.4-GLE.1-EEO.I)
- SSN: Identify the midpoint on a line segment. (MA10-GR.HS-S.4-GLE.1-EEO.V)
- Represent transformations in the plane and describe transformations as functions that take points in the plane as inputs and give other points as outputs. (MA10-GR.HS-S.4-GLE.1-EO.a.ii, iii)
- SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II)
- Compare transformations that preserve distance and angle to those that do not. (MA10-GR.HS-S.4-GLE.1-EO.a.iv)
- Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself. (MA10-GR.HS-S.4-GLE.1-EO.a.v)
- Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments. (MA10-GR.HS-S.4-GLE.1-EO.a.vi)
- SSN: Complete an if/then statement related to real life situations. (MA10-GR.HS-S.4-GLE.1-EEO.III)
- Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure. (MA10-GR.HS-S.4-GLE.1-EO.a.vii)
- SSN: Create geometric shapes using construction tools including technology. (MA10-GR.HS-S.4-GLE.1-EEO.IV)
- Specify a sequence of transformations that will carry a given figure onto another. (MA10-GR.HS-S.4-GLE.1-EO.a.viii)
- Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent. (MA10-GR.HS-S.4-GLE.1-EO.b.i, ii)
- Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent. ((MA10-GR.HS-S.4-GLE.1-EO.b.iii)
- Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions. (MA10-GR.HS-S.4-GLE.1-EO.b.iv)
- Prove theorems about lines and angles, triangles, and parallelograms. (MA10-GR.HS-S.4-GLE.1-EO.c)

Critical Language: includes the Academic and Technical vocabulary, semantics, and discourse which are particular to and necessary for accessing a given discipline.

EXAMPLE: A student in Language Arts can demonstrate the ability to apply and comprehend critical language through the following statement: "Mark Twain exposes the hypocrisy of slavery through the use of satire."

A student in _____ can demonstrate the ability to apply and comprehend critical language through the following statement(s):

I can use rigid transformations to show that necessary and sufficient combinations of congruent sides and angles prove triangles congruent.

SSN: I can show whether two triangles are exactly the same size and have exactly the same angles even if they have been turned, flipped, or slide.

Academic Vocabulary:	Classify, identify, compare, analyze, prove, substitution, develop, sufficient, necessary, definition, coordinate plane, angles, side lengths, SSN: Compare, same, different, resize, reflect, side lengths, lines, midpoint, angle, perpendicular, rotate
Technical Vocabulary:	Transformation, definitions, proofs, vertical angles, perpendicular bisector, rotation, translation, reflection, rigid transformation, congruence, theorem, postulate,

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Unit Description:	This unit investigates transformations, congruence, and proof. Students begin with informal explorations of rigid transformations. Students then use precise mathematical definitions of rotations, translations and reflections to determine if each of these rigid transformations is a function. The transformation work of this unit leads students to develop formal proofs about congruency, parallel lines, triangle relationships, and parallelograms.	
Considerations:	SSN: Students will need access to adapted texts listed below and the presentations or writing that they create will reflect Extended Evidence Outcomes p. 3. All EEO's are preceded by the phrase "With appropriate supports students can". They may also need an alternate ways to communicate understanding or write. Consult SWAAAC team member, SPED teacher or related services professional for assistance with augmentative alternative communication (AAC) device and have an alternate pencil if needed. A worthwhile source of ideas for adapted equipment and software is: http://www.swaaac.com/Catalog/default.asp . Another very useful source of adaptation ideas is:	

Performance Assessment: The caps	Performance Assessment: The capstone/summative assessment for this unit.				
Claims: (Key generalization(s) to be mastered and demonstrated through the capstone assessment.)	Precise definitions of basic geometric concepts facilitate the development of careful proofs. SSN: Definitions about attributes of shapes help prove things about the shapes.				
Stimulus Material: (Engaging scenario that includes role, audience, goal/outcome and explicitly connects the key generalization)	You are an artist and the mathematics museum (http://momath.org/) has created a contest for a geometric mural. They want the mural to allow visitors to create geometric proofs about polygons and congruence. Your mural will need to have triangles and other polygons that can be shown to be congruent through transformations and other geometric theorems. The mural design should include symbols for congruence, perpendicularity, and parallelism as appropriate. The mural exhibit will also need to include questions for visitors to answer and information placards with answers and proofs for each question. For example, why are the green and red triangles congruent? SSN: You are creating a quilt to be given away at a local fair.				
Product/Evidence: (Expected product from students)	Students will create a mural, set of questions about the mural, and answers to each question. The design of the mural could include: • At least two pairs of triangles that can be proved congruent through transformations, ASA or SAS. • A visual of at least one other theorem from the unit such as angles formed by parallel lines cut by a transversal. The questions about the mural could include concepts such as: • Transformations				

	 Congruency The answers to each question should include clear explanations, proofs and visuals to help visitors understand each mathematical concept. SSN: https://www.pinterest.com/pin/512073420104812463/ (polygon mural idea) SSN: Students can create a quilt using triangle shapes to demonstrate transformations (flip, turn or slide) and congruency
Differentiation: (Multiple modes for student expression)	Students can write their questions and corresponding answers using their notes from this unit as scaffolding. Student can write their questions and corresponding answers using proofs not discussed in this unit as an extension. Students can use drafting tools including software (http://www.techsupportalert.com/best-free-cad-program.htm) to create their designs and make interactive murals using touch screens. SSN: http://buggyandbuddy.com/geometry-kids-quilt-activity-using-triangles-free-printable/ (resource for creating a quilt) SSN: Students can use the online activities listed in the unit, the quilt activity or coordinate graphs to show transformations and demonstrate that shapes are congruent.

Texts for independent reading or for class read aloud to support the content			
Informational/Non-Fiction	Fiction		
Simon & Schuster's Guide to Gems and Precious Stones by Simon & Schuster and Kennie Lyman (Lexile level 800+) SSN: Shapes book http://tarheelreader.org/2009/03/23/shapes-6/ SSN: Art Forms in a Cat's Face book http://tarheelreader.org/2014/10/13/art-forms-in-a-cats-face/ SSN: Shapes of Your World book http://tarheelreader.org/2009/05/10/quilt-geometry/14/ SSN: Quilt Geometry book http://tarheelreader.org/2009/05/10/quilt-geometry/14/	The Flying Circus of Physics by Jearl Walker (Lexile level 800+) Flatland: A Romance of Many Dimensions by Edwin Abbot (Lexile level 1280)		

Ong	Ongoing Discipline-Specific Learning Experiences				
1.	Description:	Think/work like a mathematician – Expressing mathematical reasoning by constructing viable arguments, critiquing the reasoning of others	Teacher Resources:	http://www.insidemathematics.org/index.php/standard-3 (examples of constructing viable arguments) http://quizlet.com/22134361/cpm-index-cards-of-teaching-strategies-flash-cards/ (teaching strategies to encourage class discussions)	
			Student Resources:	N/A	
	Skills:	Provide justification for arguments through a series of logical steps while using correct mathematical vocabulary. Analyze and critique the arguments of other students	Assessment:	Students provide valid geometric proofs by justifying their reasoning to peers on a consistent basis. Students can also critique a fellow student's proof for validity. Students will need to be precise with language such as definitions, symbols, and algebraic descriptions to demonstrate a high quality proof. SSN: http://www.kidsmathgamesonline.com/facts/geometry/history.html (Explore Geometry	

			1	ier-Authoreu Sampie instructional Ont
				facts)
2.	Description:	Think/work like a mathematician – Engaging in the practice of modeling the solution to real world problems	Teacher Resources:	http://www.corestandards.org/Math/Content/HSM (Common Core State Standards description of the modeling process) http://blog.mrmeyer.com/?p=16301 (Dan Meyer discussion on modeling) http://threeacts.mrmeyer.com (Examples of 3-act problems)
			Student Resources:	http://learni.st/users/S33572/boards/2771-defining-transformations-using-basic-geometry-objects-common-core-standard-9-12-g-co-4 (video 10 is titled "Applications of Transformations" and examines how transformations are used in animations) SSN: https://www.youtube.com/watch?v=NY2cDTpsvBA (video on how transformations are used in animation)
	Skills:	Model real world problems mapping relationships with appropriate models, analyze relationships to draw conclusions, interpret results in relation to context, justify and defend the model, and reflect on whether results make sense	Assessment:	Modeling Problems Students use transformations to model real world contexts in the fields of geology, biology, architecture and animation. Students will be able to draw conclusions and interpret their models in relation to the context to determine if their model makes sense.
3.	Description:	Mathematicians are fluent with geometric transformations	Teacher Resources:	N/A
			Student Resources:	http://www.mathplayground.com/ShapeMods/ShapeMods.html (practice on a coordinate grid with reflections) http://www.kidsmathgamesonline.com/geometry/transformation.html (practice on a coordinate grid with reflections) http://learni.st/users/S33572/boards/2771-defining-transformations-using-basic-geometry-objects-common-core-standard-9-12-g-co-4 (videos and practice problems with transformations)
	Skills:	Visualize geometric relationships between objects using transformations	Assessment:	Fluency Problems Students build fluency with geometric transformations with consistent practice visualizing the result of rotations, reflections and translations.

Prior Knowledge and Experiences

Student familiarity with informally rotating, translating, and reflecting objects will provide a strong foundation for this unit. It is also helpful for students to have a degree of

comfort using a coordinate grid. Knowledge of the basic properties of polygons, parallel and perpendicular lines, angles, slope, midpoints of line segments, and the Pythagorean theorem will also support student learning, many of these ideas are formalized through proof in this unit.

SSN: Students may have had exposure to shapes and using grids, but likely will need introductory direct instruction for higher level vocabulary and the idea of proofs.

Learning Experience # 1

The teacher may provide straight manipulatives (e.g., toothpicks, straws) so that students can begin to develop and deepen their usage of key terminology (e.g., parallel lines, perpendicular lines, line segments, triangle, parallelogram, angles, circle, circular arc, point, line).

Enactive: Students can represent each geometric concept with the manipulatives.

Iconic: Students can draw representations of each concept and non-examples of each geometric concept.

Symbolic: Students can create directions for drawing each geometric concept and then share the directions with another student to determine if the directions are clear and precise. Students can then use these directions as a starting point for determining clear and precise definitions for each geometric concept.

Teacher Notes:	This is a formative assessment of students' prior understanding of each of these concepts. Students should be encouraged to show each concept in multiple ways (e.g., triangles that are not equilateral) and also non-examples of each concept. Students should also practice verbalizing a description of each concept to their neighbor using precise language.	
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs SSN: Definitions about attributes of shapes help prove things about the shapes.	
Teacher Resources:	http://www.geometrycommoncore.com/content/unit1/gco1/webresources.html (resources for definitions associated with this standard) SSN: https://www.pinterest.com/pin/277041814547556888/ (virtual manipulative activity that could replace this learning experience) SSN: http://1.bp.blogspot.com/-0xye_8t_sGg/UPGSCMXJqVI/AAAAAAAABZ4/JVbAy1ZR6Xs/s1600/Slide1.jpg and https://www.teacherspayteachers.com/Product/Geometry-Is-Magical-Word-Wall-FREEBIE-934215 (two free definition charts for student reference) SSN: https://www.teacherspayteachers.com/Product/Geometry-Activity-Pack-1092174 (inexpensive 78 page geometry activity pack)	
Student Resources:	http://www.mathopenref.com/circle.html (circle definition) http://www.mathopenref.com/tocs/pointstoc.html (point, lines, and planes definitions) SSN: https://www.mathsisfun.com/geometry/line.html (definitions of lines and line segments) SSN: https://www.mathsisfun.com/triangle.html (definition of triangles) SSN: https://tothesquareinch.wordpress.com/2012/04/17/types-of-lines-and-angles-activity/ (types of lines and angles activity) SSN: https://www.ixl.com/math/grade-4/parallel-perpendicular-intersecting (activity on parallel, intersecting and perpendicular lines)	
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: What is the difference between a line and line segment? Will three line segments always make a triangle? Why or why not? What is the connection between parallel and perpendicular lines? Why do we need precise definitions of geometric terms?	

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	How does an angle relate to a circle? Can you have an angle that is more than 180 degrees? Why or why not? SSN: Have students look the following: lines, angles, parallel lines, perpendicular lines, and triangles. http://www.clipartbest.com/cliparts/dc6/74X/dc674Xzc9.gif (Quilt block pattern)	
Differentiation: (Multiple means for students to access content and multiple modes for student to express understanding.)	Access (Resources and/or Process) http://wvde.state.wv.us/strategybank/FrayerModel.html (Frayer model examples of mathematical definitions) http://www.shmoop.com/common-core-standards/ccss-hs-g-co-1.html (definitions and samples questions for G.CO.1) SSN: https://www.mathsisfun.com/geometry/line.html (definitions of Lines and line segments) SSN: https://www.mathsisfun.com/triangle.html (definition of triangles) SSN: https://www.ixl.com/math/grade-4/parallel-perpendicular-intersecting (activity on parallel, intersecting and perpendicular lines)	Expression (Products and/or Performance) Students can match critical language to visual examples, non-examples and definitions Students can answer questions that connect definitions for each concept in the learning experience to real world examples Students can create a quilt block. (http://buggyandbuddy.com/geometry-kids-quilt-activity-using-triangles-free-printable/)
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)
	http://www.illustrativemathematics.org/illustrations/1504 (discussion on the two definitions of a trapezoid) http://www.eisd.net/cms/lib04/TX01001208/Centricity/Domain/599/DoubleBubbleMap.pdf (thinking map for comparing and contrasting)	Students can present to the class the competing definitions for figures such as trapezoids and explain the implications of each definition and explain why precision is necessary in defining geometric terms
Key Knowledge and Skills:	 Know precise definitions of angle, circle, circular arc, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc SSN: Identify parallel, intersecting and perpendicular lines (MA10-GR.HS-S.4-GLE.1-EEO.I) 	
Critical Language:	Circle, angle, parallel lines, perpendicular lines, parallelogram, triangle, line, line segment, point, definition, identify, sort, precision SSN: Line, parallel lines, perpendicular, angle, triangle, circle, line segment	

Learning Experience # 2

The teacher may provide examples of rigid transformation (reflection, rotation, translation) so that students can explore the impact on coordinates of transforming a figure on a coordinate plane.

Enactive: Students can rotate, reflect, and translate a nonsymmetrical object (e.g., tetromino) on a coordinate grid.

Iconic: Students can draw a nonsymmetrical figure on a coordinate grid and then draw the image of the figure after a rotation, reflection, or translation.

Symbolic: Students can record the initial and image coordinates for the vertices of a figure several basic rotations, reflections and translations.

SSN: Students may use transparent concrete shapes such as triangles on a grid to demonstrate concepts of rotation, reflection and translation and may use mirrors in working with reflections. Students may also use letters and numbers they know to demonstrate transformations.

Teacher Notes:	Students may need tracing paper, transparencies, mirrors and technology to help visualize each transformation. A nonsymmetrical
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	Colorado reacher-Admored Sample instruction		
	object can help prevent misconceptions that may naturally occur when trying to transform an object (i.e., rotating a square ninety degrees about the origin may obscure how the vertices have rotated). Rotations are generally the hardest for students to visualize particularly rotations not centered at the origin. Be sure students practice using all four quadrants as a starting point for the transformation. This learning experience is designed to be exploratory to provide comfort with each transformation on the coordinate plane. The next three learning experiences break down each transformation separately to provide students with a deeper exploration.		
Generalization Connection(s):	Algebraic representations model geometric transformations performed on a coordinate plane SSN: Number sentences can explain how to turn, flip or slide a shape using coordinates on a graph paper		
Teacher Resources:	http://mathworld.wolfram.com/Tetromino.html (examples of tetrominoes) https://commoncoregeometry.wikispaces.hcpss.org/Unit+1 (transformation resources, including a unit on transformation with real world examples) SSN: https://www.pinterest.com/pin/524739794052725344/ (simple definition chart)		
Student Resources:	http://www.ixl.com/math/geometry (practice on transformations, L1 through L8) http://www.shmoop.com/common-core-standards/ccss-hs-g-co-2.html (explanation of the standard and real world sample assessment questions) http://www.mybookezzz.org/special-education-lesson-plan-for-coordinate-planes/ (practice with graphing on a coordinate grid) SSN: http://www.mathplayground.com/ShapeMods/ShapeMods.html (transformation game online) SSN: http://www.crickweb.co.uk/ks2numeracy-shape-and-weight.html#triangles (free online grid game to review moving around a grid)		
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: Why do rotations, reflections, and translations preserve the shape and size of a figure? What needs to be included in a precise set of directions for each transformation to allow someone else to perform them? Which transformations create the same images, for example do any rotations and reflections result in the same image? What happens if you combine two transformations? What transformations will carry an object onto itself? SSN: Student can demonstrate rotations (turns) reflections (flips) and translations (slide) using triangles on a grid. SSN: Do rotations (turns) reflections (flips) and translations (slide) change the shape, or just the way it looks at that moment?		
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)	
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://www.mathsisfun.com/geometry/rotation.html (simple explanations of each transformation and practice questions) SSN: http://www.mathsisfun.com/geometry/rotation.html (simple explanations of each transformation and practice questions) SSN: https://www.ixl.com/math/grade-2/flip-turn-and-slide (practice with transformations)	Students can answer questions about rotations, reflections, and translations on a coordinate grid SSN: Student can answer questions about transformations on a coordinate grid using various movable shapes (polygons) demonstrating the terminology flip, turn or slide.	
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)	

	http://www.intmath.com/blog/music-and-transformation-geometry/5074 (music and transformations)	Students can create a short musical piece using the concept of transformations
Key Knowledge and Skills:	 Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) 	
Critical Language:	Coordinate grid, quadrants, symmetry, y-axis, x-axis, rotation, reflection, translation, rigid transformation, image, original, transformation SSN: rotation (turn) reflection (flip) translation (slide) transformation (change), grid, quadrants, up, down, right, left	

Learning Experience # 3

The teacher may provide examples of rotations so that students can begin to create precise geometric and algebraic definitions of a rotation.

Enactive: Students can rotate a point on a coordinate grid using string. Students can anchor one end of the string at center of rotation and stretch the other side of the string out to the original point. By keeping the string taut students can rotate the string a given number of degrees to find the image of the original point.

Iconic: Students can draw with a compass the circle of rotation for a point. The center of the circle will be the center of rotation and the radius is the length from the center of rotation to the original point. By drawing the resulting circle, students can find images for any angle of rotation by finding the point that creates an arc on the circle between the original point and its image with the appropriate measure.

Symbolic: Students can describe a rotation, using angle of rotation, direction (e.g., counterclockwise or clockwise) and center. Students can determine the algebraic generalization on the coordinate plane for angles of rotation about the origin for 90, 180, 270 and 360 degrees rotations (e.g, $T(x, y) \rightarrow T'(y, -x)$) when rotated counterclockwise 270 degrees about the origin on a coordinate grid).

SSN: Students will identify the coordinates before turning, flipping or rotating a shape on a grid and then identify the new coordinates.

Teacher Notes:	Rotations can be viewed geometrically as a movement along the arc of a circle and algebraically as the coordinates of an image for the point (x, y). This learning experience assumes rotations about the origin to provide a consistent look at algebraic representations of rotations. Students can explore rotations with centers beyond the origin and degrees other than 90, 180, 270 and 360 but they should not be expected to generalize the algebraic notation for these other rotations. It is important emphasize the connection between the definitions for a circle and angles as a way of understanding a rotation.
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs Algebraic representations model geometric transformations performed on a coordinate plane
Teacher Resources:	https://www.khanacademy.org/math/geometry/transformations (videos explaining each type of transformation on a coordinate

Student Resources:	grid) http://www.regentsprep.org/Regents/math/geometry/GT5/reviewtranformations.htm (review of transformation notations, formulas and definitions) SSN: https://www.teacherspayteachers.com/Product/I-have-who-has-game-for-measuring-angles-with-a-protractor-89915 (free downloadable game for practice measuring angles with a protractor) SSN: https://www.teacherspayteachers.com/Product/Lines-and-Angles-Posters-467675 (free printouts of definitions of new terms) http://www.mathwarehouse.com/transformations/rotations-in-math.php (interactive demonstration of how to perform a rotation in math) https://www.ixl.com/math/geometry/rotations-find-the-coordinates (practice writing coordinates for rotations around the center)		
	SSN: https://www.ixl.com/math/grade-4 (introduce student to graph coordinate paper, use of a compass to draw circles, and a protractor to measure angles) SSN: https://www.youtube.com/watch?v=2Pfso5qzWFU&feature=iv&src_vid=NKtJd1hkl9k (triangles video)		
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: How can you determine the angle of rotation when provided with two points and the point of rotation? How can you define a rotation using the concept of a circle? What happens if the center of rotation is the same as the point being rotated? What are coordinates of the image of a point (x, y) rotated about the origin 90, 180, 270, 360 degrees? Why does it not matter if the original point is in the 3 rd quadrant? SSN: Assess using activities p. 13-16 https://www.ixl.com/math/grade-4		
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)	
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://enlvm.usu.edu/ma/nav/activity.jsp?sid= shared&cid= emready@transformations&lid=32 (visual images for each transformation) http://learnzillion.com/lessons/2633-measure-full-and-half- rotations (resources for reviewing ideas about angles and circles) http://www.gradeamathhelp.com/transformation- geometry.html (hints about each transformation) SSN:http://www.kidsmathgamesonline.com/geometry/angles. html SSN: http://www.mathplayground.com/measuringangles.html (measure angles game)	Students can develop fluency with the definitions of a rotation scaffolded by visual images of the vocabulary Students can measure angles along the arc of a circle by first reviewing these ideas in a video as prerequisite understanding and skills for this learning experience Students can answer questions on rotations to reinforce their understanding of rotations SSN: Student can demonstrate the use of a protractor to measure angles using either online activity (https://www.ixl.com/math/grade-5/measure-angles-with-a-protractor) or with paper and pencil	
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)	
	N/A	Students can use the distance formula to determine the location of a point after a rotation when the point of rotation is not at the center or for degrees other than 90, 180, 270, and 360 degrees	
Key Knowledge and Skills:	Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments		

	SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II)	
Critical Language:	Circle, arc, origin, direction, clockwise, counterclockwise, degrees, point of rotation, coordinates, original, image, coordinate grid, quadrants, compass, algebraic generalization, transformation SSN: Coordinate grid, x-axis, y-axis, up, down, right, left.	

Learning Experience # 4

The teacher may provide examples of reflections so that students can begin to create precise geometric and algebraic definitions of a reflection.

Enactive: Students can be given two points and asked to find the line of reflection by folding and then a point and line of reflection and asked to find the image of the point.

Iconic: Students can be given two points and asked to draw the line of reflection (i.e., the perpendicular bisector of the two points) using either geometry software, geometric construction tools, or a protractor and ruler.

Symbolic: Students can describe a rotation using the line of reflection. Students can determine the algebraic generalization of a reflection on the coordinate plane (e.g., $T(x, y) \rightarrow T'(x, y)$) when reflected over the x-axis on a coordinate grid).

SSN: Provide examples of reflection on coordinate grid and have students work with mirrors to predict what the shape will look like on the grid as a reflection.

Teacher Notes:	Reflections can be viewed geometrically as the image, which creates a perpendicular bisector between the line of reflection and the original point, and algebraically as the coordinates of an image for the point (x, y). Students can be given opportunities to see that the line of reflection is perpendicular to the segment between the two reflected points. Students might also notice that reflecting a point across a line twice will result in the point carrying onto itself. Students can also connect rotations of 180 degrees to reflections.
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs Algebraic representations model geometric transformations performed on a coordinate plane SSN: Definitions about attributes of shapes help prove things about the shapes. SSN: Number sentences can explain how to turn, flip or slide a shape using coordinates on a graph paper
Teacher Resources:	https://www.khanacademy.org/math/geometry/transformations (videos explaining each type of transformation on a coordinate grid) http://www.youtube.com/watch?v=EDIMOFfc4J0&feature=related (video about reflections) http://www.regentsprep.org/Regents/math/geometry/GT5/reviewtranformations.htm (review of transformation notations, formulas and definitions) SSN: https://www.teacherspayteachers.com/Product/Geometry-Slides-Flips-and-Turns-Translations-Reflections-Rotations-1117529 (inexpensive worksheet/assessment on flips, turns, and slides) SSN: https://www.teacherspayteachers.com/Product/Flip-Slide-Turn-Congruent-Word-Wall224150 (free definitions chart for student notebook) SSN: http://www.mathsisfun.com/geometry/bisect.html (bisecting lines and angles) SSN: http://www.mathsisfun.com/data/cartesian-coordinates.html (intro to graphs and coordinates) SSN: https://www.ixl.com/math/grade-3/coordinate-graphs (coordinates and graphs exercise)
Student Resources:	http://www.mathwarehouse.com/transformations/reflections-in-math.php (activity to examine coordinates) http://www.ixl.com/math/geometry/reflections-find-the-coordinates (applet to practice writing coordinate points after a reflection)

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	SSN: https://www.ixl.com/math/grade-3/reflection-rotation-and-translation (review reflection, rotation, translation with this online activity) SSN: http://www.sheppardsoftware.com/mathgames/geometry/shapeshoot/TranslateShapesShoot.htm (game for reflection, rotation, translation) SSN: http://www.mhschool.com/math/mathconnects/wa/assets/docs/394_397_wa_gr3_adllsn_onln.pdf (review of lines) SSN: https://www.ixl.com/math/grade-3/parallel-perpendicular-intersecting (review of lines exercise online) SSN: https://www.mathsisfun.com/data/cartesian-coordinates-interactive.html (interactive Cartesian Coordinates activity) SSN: https://www.kidsmathgamesonline.com/geometry/grids.html (grid game with coordinates)	
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: What rotation is equivalent to a reflection? What happens when the line of reflection goes through point? How do you find a line of reflection given two points? Why is the perpendicular bisector the same as the line of reflection of two points? How can you define a reflection using the concept of a perpendicular bisector? SSN: Given examples of reflections (flip), translation (move) and rotations (turn) of triangles or letters and students will identify the translation by pointing or showing or stating when comparing the changes to an original. SSN: Given examples the student will identify perpendicular lines, parallel lines and the midpoint (bisection of a line) by pointing, showing or stating.	
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://www.gradeamathhelp.com/transformation- geometry.html (visual images for each transformation) http://enlvm.usu.edu/ma/nav/activity.jsp?sid= shared&cid= emready@transformations&lid=51 (practice on reflections) SSN:https://www.teacherspayteachers.com/Product/Transfor mations-Flips-Slides-and-Turns-407391 (free worksheet activity identifying different types of transformations)	Students can develop fluency with the definitions of a rotation scaffolded by visual images of the vocabulary Students can answer questions on this applet to reinforce their understanding of reflections SSN: Student can demonstrate by using concrete objects on graph paper that translations (moving) reflections (flipping) and (turning) rotations of a shape are the same even if the shape looks different from the original.
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)
	http://www.etymonline.com/index.php?term=reflection (entomology of the word reflection)	Students can create metaphors for reflection and connect its mathematical uses to other content areas
Key Knowledge and Skills:	 Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) 	
Critical Language:	Reflection, line segment, perpendicular, bisect, x-axis, y-axis, y=x, line of reflection, coordinates, original, image, coordinate grid, quadrants, algebraic generalization, transformation SSN: Coordinates, coordinate grid, perpendicular, bisect, X-axis, Y-axis	

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Learning Experience #5

The teacher may provide examples of translations so that students can begin to create precise geometric and algebraic definitions of a translation.

Enactive: Students can move on a life size coordinate grid given directions for a translation such as move -2 units vertically or (x, y-2).

Iconic: Students can draw a translated a point on a coordinate grid given directions for a translation.

Symbolic: Students can describe a translation using verbal and algebraic descriptions given two points.

Teacher Notes:	Translations can be viewed geometrically as moving an original point a particular distance and direction (e.g., vector) and algebraically as the coordinates of an image for the point (x, y). Students may struggle to fluently move a point both negatively and positively in vertical and horizontal directions and to coordinate the movement for both the x and y coordinates (e.g. T(x, y) → T'(x+2, y-3) translates a point two units to the right and three units down on a coordinate grid). SSN: Students understand that coordinates on a grid refer to an axis and positive and negative numbers represent units on the grid. It will also be new to most students that numbers can represent movements of shapes on a grid.	
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs Algebraic representations model geometric transformations performed on a coordinate plane SSN: Definitions about attributes of shapes help prove things about the shapes. SSN: Number sentences can explain how to turn, flip or slide a shape using coordinates on a graph paper	
Teacher Resources:	https://www.khanacademy.org/math/geometry/transformations (videos explaining each type of transformation on a coordinate grid) http://www.regentsprep.org/Regents/math/geometry/GT5/reviewtranformations.htm (review of transformation notations, formulas and definitions) SSN: http://www.mathsisfun.com/data/cartesian-coordinates.html (intro to graphs and coordinates) SSN: https://www.ixl.com/math/grade-3/coordinate-graphs (coordinates and graphs exercise)	
Student Resources:	http://www.mathsisfun.com/geometry/translation.html (translate objects while examining changes in coordinates) http://www.ixl.com/math/geometry/translations-write-the-rule (writing the rule for a translation) SSN: http://www.mathsisfun.com/data/cartesian-coordinates-interactive.html (interactive Cartesian Coordinates activity) SSN: http://www.kidsmathgamesonline.com/geometry/grids.html (grid game with coordinates)	
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: How can you describe a translation that will carry a point back to itself? When translating several points how are the lines connecting the points to their images related? How are parallel lines related to translations? How can you find a translation given two points? How can you define a translation geometrically and algebraically? SSN: Using a coordinate graph with isosceles triangle or other shapes, the student will demonstrate or identify with concrete shapes translation (slide) to particular graph points, identify the points on the graph when the triangle is reflected (flipped) and the change in points when the shape is rotated (turned).	

Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://www.gradeamathhelp.com/transformation- geometry.html (visual images for each transformation) http://enlvm.usu.edu/ma/nav/activity.jsp?sid= shared&cid= emready@transformations&lid=29 (practice on translations) SSN:http://resources.oswego.org/games/BillyBug/bugcoord.h tml (interactive graphing of coordinate pairs) SSN:http://nlvm.usu.edu/en/nav/frames asid 297 g 3 t 3.h tml?open=activities&from=topic t 3.html (online activity on reflection) SSN:http://nlvm.usu.edu/en/nav/frames asid 207 g 1 t 3.h tml?open=activities&from=topic t 3.html (using online activity on rotation) SSN:http://nlvm.usu.edu/en/nav/frames asid 167 g 1 t 3.h tml?open=activities&from=topic t 3.html (using online activity on translations)	Students can develop fluency with the definitions of a rotation scaffolded by visual images of the vocabulary Students can answer practice questions to reinforce their understanding of translations SSN: Students can use either online resources or graph paper and shapes to move shapes to given coordinates (translation or sliding), and demonstrate rotation and reflections with the shapes and identify the changed coordinates.
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)
	http://enlvm.usu.edu/ma/nav/activity.jsp?sid= shared&cid= emready@transformations&lid=61&aid=940049925 (relating translations to vectors)	Students can create a presentation for the class on the use of vectors to describe translations and their application to real world situation
Key Knowledge and Skills:	 Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) 	
Critical Language:	Translations, vertically, horizontally, image, original, parallel, contransformation SSN: Up, down, right, left, grid, x-axis, y-axis	ordinates, coordinate grid, quadrants, algebraic generalization,

Learning Experience # 6		
The teacher may provide students with examples of all three types of transformations so that students can gain fluency in describing transformations verbally, algebraically, and graphically.		
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs Algebraic representations model geometric transformations performed on a coordinate plane	
Teacher Resources: <pre>http://map.mathshell.org/materials/lessons.php?taskid=524&subpage=concept</pre> (formative lesson with cards students can come showing transformations graphically, algebraically and graphically) SSN: http://www.virtualnerd.com/middle-math/integers-coordinate-plane/transformations (review lessons on doing)		

	transformations and graphing their movements or changes)	
	SSN: http://www.math-aids.com/Geometry/Transformations/ (create custom worksheets on transformations for student practice)	
Student Resources:	SSN: http://www.bgfl.org/bgfl/custom/resources ftp/client ftp/ks3/maths/coordinate game/game1.htm (game to practice graphing coordinates online) SSN: https://www.teacherspayteachers.com/Product/Battleship-Activity-Common-Core-Graphing-on-a-Coordinate-Plane-887295 (free downloadable game to practice graphing coordinates on paper Graphing Battleships) SSN: http://mste.illinois.edu/users/pavel/java/chameleon/basic/ (use applet to find points on a coordinate grid)	
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: How can you describe a transformation algebraically? What does (x, y) → (y, x) mean? What transformation does it define? How are translations, rotations, and reflections similar and different? Which transformation is the easiest to visualize? Which is the hardest? Why? SSN: Student is able to move shapes to designated coordinates on a grid and is able to demonstrate using triangles rotation (turning) translation (sliding) and reflection (flipping).	
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://www.regentsprep.org/Regents/math/geometry/GT5/reviewtranformations.htm (review of transformation notations, formulas and definitions) http://illuminations.nctm.org/Lesson.aspx?id=3704 (lesson plan for using an online applet that practices all threetransformations) SSN:https://www.teacherspayteachers.com/Product/Reflections-on-a-Coordinate-Plane-for-Interactive-Notebook-586983 (reflections on a coordinate plane notebook)	Students can complete the algebraic and verbal descriptions of a transformation using scaffolding on the notation and definitions for each transformation Students can complete practice questions for all three transformations SSN: Students can use applet to find points on a coordinate grid (http://mste.illinois.edu/users/pavel/java/chameleon/basic/) SSN: Students can move coordinates designated by the teacher to demonstrate the translation (moving) rotation (turning) and reflection (flipping), when given a coordinate graph and a shape.
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)
	http://www.discoveryeducation.com/teachers/free-lesson- plans/discovering-math-exploring-geometry.cfm (unit on creating a three dimensional model of a city)	Students can create a three-dimensional model of a city using transformations
Key Knowledge and Skills:	 Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) 	
Critical Language:	Verbally, algebraically, graphically, translations, vertically, horizontally, reflection, line segment, perpendicular, bisect, x-axis, y-axis, y=x, line of reflection, circle, arc, origin, direction, clockwise, counterclockwise, degrees, point of rotation, image, original, parallel, coordinates, coordinate grid, quadrants, algebraic generalization, transformation	

	SSN: Vertically, horizontally, line segment, perpendicular, bisect, x-axis, y-axis, degrees, parallel, coordinates, coordinate grid,
	quadrants

Learning Experience #7

The teacher may provide examples of transformations (including those that do not preserve distances and angles in addition to examples of reflections, rotations, and translations) so that students can explore which types of transformation preserves distances and angles (i.e., creates congruent figures).

Enactive: Students can explore reflections and rotations on rectangles, parallelograms, trapezoids, and regular polygons to find rotations and reflections that carry each type of figure onto itself.

lonic: Students can draw the image of a figure when provided with algebraic notation of a transformation and identify if the transformation is a reflection, translation, or rotation. Students can justify if the translation created a congruent figure by determining if distances and angles were preserved.

Symbolic: Students can create an argument that each type of rigid transformation is a function based on the precise definition for each rigid transformation (reflections, translations, and rotations) and the definition of a function.

SSN: Student will explore how changing the size of a shape (dilation) makes it not exactly the same but similar, the side lengths change the angle measures stay the same.

Teacher Notes:	This is the first learning experience where students will encounter non-rigid transformations such as T $(x, y) \rightarrow T'(2x, 2y)$ (i.e., a dilation) or T $(x, y) \rightarrow T'(-2x, 3y)$. It may be helpful for students to reason through why dilations are not functions because each point in the original is not mapped to one and only one point in the image before trying to show why reflections, rotations, and translations are functions. Throughout this learning experience students can be introduced to the notation for congruent angles and sides on geometric drawings. Before the end of this unit the teacher may also introduce the notations for perpendicular and parallel lines.
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs Algebraic representations model geometric transformations performed on a coordinate plane Sequences of transformations or combinations of angles and side lengths can determine the congruence of shapes SSN: Definitions about attributes of shapes help prove things about the shapes. SSN: Number sentences can explain how to turn, flip or slide a shape using coordinates on a graph paper SSN: Measuring angles and lengths of sides of shapes help mathematicians know if two shapes are the same even if they look different because of a turn, slide or flip
Teacher Resources:	http://www.whyslopes.com/5080More Algebra/54004 Functions/00505 Function notation for geometric transformations.html (function notation for transformations) https://docs.google.com/a/sjsu.edu/file/d/0ByBN4IxhmiWgMTBjYTZjMjEtNGFkOC00MzUxLWJhZGUtMDM2MmQyOWFIN2M0/edit? hl=en&pli=1 (precise definitions for transformations) http://www.ixl.com/math/geometry (choose L.11, transformations that carry a polygon onto itself, and L.9, classify congruence transformations) http://www.mathematicsvisionproject.org/uploads/1/1/6/3/11636986/sec1_mod5_ccp_tn_112612.pdf (unit exploring congruence and transformations) https://commoncoregeometry.wikispaces.hcpss.org/Unit+1 (congruence as rigid motions) SSN: https://www.mathsisfun.com/geometry/congruent.html (review Congruent or similar lesson) SSN: https://tothesquareinch.wordpress.com/2012/02/21/transformations-foldable/ (activity for teaching rigid vs. non- rigid

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	transformations) SSN: https://www.pinterest.com/pin/358739926544663683/ (activity for transformations using squares and graph paper)	
Student Resources:	http://caccssm.cmpso.org/a/cmpso.org/caccss-resources/geometry-task-force/geometry-resources/isometry-unit (section A8 algebraic transformations: gives a list of transformations written algebraically so students can draw the resulting figure on a coordinate grid and determine what type of transformation was used) SSN: http://www.math-aids.com/Geometry/ (practice worksheet on transformations)	
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: Which transformations create congruent figures and why? Why are reflections, translations, and rotations called rigid transformations? Why are rigid transformations functions? Could transformations be a function and not create a congruent figure? Why or why not? Which rigid transformations can carry a figure onto itself (i.e., the identify transformation)? Does the figure being transformed make a difference? SSN: Student completes online identification of transformations (http://mathcrush.com/geometry/ws_types_of_transformations_pv.gif)	
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://www.worksheetworks.com/miscellanea/graphic- organizers.html (definitions of each transformation and a function using the Frayer model)	Students can provide a written explanation of why each rigid transformation is a function scaffolded by definitions for transformations and a function
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)
	http://en.wikipedia.org/wiki/Inversive geometry (describes the definition of geometric inverse) SSN: https://www.pinterest.com/pin/358739926544663683/ (activity for transformations using squares and graph paper) SSN:https://www.mathsisfun.com/geometry/transformations. html (review transformations on line lesson) SSN:http://www.sheppardsoftware.com/mathgames/geometry/shapeshoot/TranslateShapesShoot.htm (use online game to identify transformations)	Students can write the inverse transformation for each of the transformations in this learning experience SSN: Students can create examples of rigid transformations using paper squares and graph paper, identifying each transformation.
Key Knowledge and Skills:	 Represent transformations in the plane and describe transformations as functions that take points in the plane as inputs and give other points as outputs Compare transformations that preserve distance and angle to those that do not Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) 	

Critical L	.anguage:	Congruence, function, distances, angles, parallelogram, trapezoid, regular polygon, precise, definition, rotation, reflection,
		translation, rigid transformation
		SSN: rotation (turn), reflection (flip), translation (slide), rigid transformation (measurement of the shape stays the same and is the
		same size)

Learning Experience # 8

The teacher may provide students with pairs of figures on a coordinate grid (only some of which are congruent) so that students can use transformations to determine congruency.

Enactive: Students can use tracing paper to show a sequence of transformations to map one figure onto another.

Symbolic: Students can describe algebraically the sequence of transformations necessary to map one figure onto another to show congruence.

SSN: *Enactive*: Using transparent colored triangles cut out from colored plastic (exact same size and shape) and four quadrant graph paper, student identifies where triangles are on graph paper using coordinates as triangles are reflected (flip), rotated (turn), and translated (slide) to another location. *Symbolic*: Students can count and write down graph coordinates for each transformation for above activity.

Teacher Notes:	The enactive stage should support students in the symbolic stage as they describe a sequence of transformations. This is the first time students are composing transformations (i.e., linking transformations). Students should test out whether the order matters when specifying a sequence of transformations.	
Generalization Connection(s):	Sequences of transformations or combinations of angles and side lengths can determine the congruence of shapes SSN: Measuring angles and lengths of sides of shapes help mathematicians know if two shapes are the same even if they look different because of a turn, slide or flip	
Teacher Resources:	http://caccssm.cmpso.org/a/cmpso.org/caccss-resources/geometry-task-force/geometry-resources/isometry-unit (A6 congruence activity: given two figures describe a sequence of transformations to map one figure onto another) https://commoncoregeometry.wikispaces.hcpss.org/Unit+1 (congruence as rigid motions) http://www.showme.com/sh/?h=fPKkK7E (congruency and transformations) SSN:https://www.teacherspayteachers.com/Product/Transformations-Interactive-Notes-Practice-and-Assessments-1256515 (revie activities of transformations) SSN:http://www.math-aids.com/Geometry/Coordinate/ (worksheets on measuring angles with protractors and line segments with rulers) http://www.math-aids.com/Geometry/ (angles worksheets) SSN:http://tle.westone.wa.gov.au/content/file/a4260b21-fb07-4fa0-8f9e- 9579f8d2d6c3/1/COMM1085 angles.zip/angles/html/popups/disc_everyday_examples.html#2 (everyday_examples of angles)	
SSN: https://www.pinterest.com/pin/276760339570563773/ (practice with measuring angles with a protractor of SSN: https://www.pinterest.com/pin/349240146075689993/ (practice measuring line segments with a ruler) SSN: http://www.kidsmathgamesonline.com/geometry/grids.html (game to practice measuring angles)		
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: How can you tell if two figures are congruent by using transformations? Is there more than one sequence of transformations that can be used to map a figure to its image? When does the order of transformations matter when determining the sequence of transformations that map a figure onto its	

	image? SSN: What do you need to measure triangles to make sure they are exactly the same? Do you need to measure more than one thing?	
Differentiation: (Multiple means for students to access content and multiple modes for student to express understanding.)	Access (Resources and/or Process)	Expression (Products and/or Performance)
	Teachers may provide students with the transformations used to create image of a figure	Students can sequence the transformation options provided by the teacher to determine if the two figures are congruent SSN: Students can measure with a protractor and ruler, angle and lines of triangles to determine the congruency of triangles.
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)
	http://www.mcescher.com/ (official McEscher website with examples of his art)	Students can identify the types of transformations used to create art created by McEscher Students can create their own artwork inspired by McEscher Students can create sequences of transformations that are commutative (i.e., a composition of transformations for which order does not matter)
Key Knowledge and Skills:	 Represent transformations in the plane and describe transformations as functions that take points in the plane as inputs and give other points as outputs Compare transformations that preserve distance and angle to those that do not Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent Specify a sequence of transformations that will carry a given figure onto another SSN: Identify parallel, intersecting and perpendicular lines (MA10-GR.HS-S.4-GLE.1-EEO.I) SSN: Identify the midpoint on a line segment. (MA10-GR.HS-S.4-GLE.1-EEO.V) SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) 	
Critical Language:	Sequence, order, congruent, function, distances, angles, rotation, reflection, translation, rigid transformation SSN: Congruent (same), angle, line segment, point, rotation (turn) reflection (flip) and translation (slide), grid, coordinates	

Learning Experience # 9

The teacher may provide students with attributes of triangles (e.g., one angle and one side) so that students can explore which attributes are necessary to ensure congruent triangles.

Enactive: Students can use straight manipulatives (e.g., toothpicks, straws) to determine if there is more than one triangle possible from a list of attributes. *Iconic*: Students can draw triangles with particular attributes to determine if there is more than one triangle possible from a list of attributes.

Symbolic: Students will provide an informal justification of whether the attributes will always result in congruent triangles and critique the reasoning of others.

Teacher Notes:	Students may struggle correctly ordering the sides and angles when doing determining congruent triangles. It is sometimes difficult	
	for them to determine if the side is between the angles or not. This learning experience is designed to provide an informal	

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	experience with these ideas. The next learning experience for SSN: Triangles always have three sides, but can have different learning experience for some sides.	ormalizes these ideas by proving the SSS, SAS, and ASA theorems. engths of sides and different angles.
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs Sequences of transformations or combinations of angles and side lengths can determine the congruence of shapes SSN: Definitions about attributes of shapes help prove things about the shapes. SSN: Measuring angles and lengths of sides of shapes help mathematicians know if two shapes are the same even if they look different because of a turn, slide or flip	
Teacher Resources:	http://map.mathshell.org/materials/lessons.php?taskid=452&subpage=concept (lesson for analyzing which attributes of a triangles are necessary to prove congruence) SSN: Review lesson with student on scalene, isosceles and equilateral triangles: https://www.ixl.com/math/grade-3/triangles-equilateral-isosceles-and-scalene SSN: Worksheet on identifying different types of triangles: http://www.mathworksheets4kids.com/triangles/identify-sides-type1-1.pdf	
Student Resources:	SSN: Book on the pyramids (Subscription site, free trial available): www.readinga-z.com/books/leveled-books/book/?id=317 \ SSN: Interactive triangle activity: https://www.mathwarehouse.com/geometry/triangles/interactive-triangle.php	
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: What attributes do you need to conclude if two triangles are congruent? Why is it not always sufficient to know two angles and a side to determine congruency in triangles? Why is it not always sufficient to know any two sides and an angle to determining congruency in triangles? What are some characteristics of a quality proof? SSN: When you compare triangles, what do you have to measure to make sure they are the exactly the same or congruent?	
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://map.mathshell.org/materials/lessons.php?taskid=452& subpage=concept (lesson for analyzing which attributes of a triangles are necessary to prove congruence) SSN: Work with student on cutting out and taping together triangles of different dimensions and identifying which are possible on this activity: http://illuminations.nctm.org/uploadedFiles/Content/Lessons /Resources/3-5/Triangles-AS-WhatsImportant(1).pdf	Students can verbally explain to a partner only four of the nine examples in the learning experience (SSS, SAS, ASA and a non-example) prior to working as a team to write their informal reasoning SSN: Review with students the different measurements of sides of triangles on the worksheet and identify differences in lengths of side for each problem: Have student cut and compare these triangles to see if any of the three types are congruent based on their measurements or just similar. http://www.mathworksheets4kids.com/triangles/identify-sides-type3-1.pdf
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)
	http://www.geometrycommoncore.com/content/unit1/gco8/gco8.html (resource for examining all the different ways of looking at triangle congruence)	Students can create an informal proof for the more specialized cases of triangle congruence such as for AAS and HL

	 Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) 	
Critical Language:	Triangles, angles, sides, congruence, attributes, necessary, sufficient, critique, corresponding SSN: Triangles, angles sides, isosceles (2 sides the same), scalene (all sides different) and equilateral (all sides the same), similar, congruent, same.	

Learning Experience # 10

The teacher may provide diagrams of congruent triangles so that students can begin to formalize their understanding of triangle congruence developed in the previous learning experience.

SSN: The teacher may provide illustrations (http://www.mathwarehouse.com/geometry/congruent_triangles/) for determining congruence of triangles so the student can understand the concept of proofs related to determining the congruence of triangles.

Teacher Notes:	Students struggle to understand the need for proof in geometry. Drawings accompanying proofs provide visual evidence of what the problem is trying to prove and students sometimes see little need to prove what a drawing shows. Students should be encouraged to understand a drawing is not a proof because it is not generalizable and can be deceiving.		
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs Sequences of transformations or combinations of angles and side lengths can determine the congruence of shapes SSN: Definitions about attributes of shapes help prove things about the shapes. SSN: Measuring angles and lengths of sides of shapes help mathematicians know if two shapes are the same even if they look different because of a turn, slide or flip		
Teacher Resources:	see the resources for free and pay a nominal fee to downlo http://www.illustrativemathematics.org/illustrations/109 (prohttps://commoncoregeometry.wikispaces.hcpss.org/Unit+1 (p	http://www.geometrycommoncore.com/content/unit1/gco8/gco8.html (teaching resources for proving triangle congruence, you can see the resources for free and pay a nominal fee to download everything on the site) http://www.illustrativemathematics.org/illustrations/109 (proof of SAS using reflections) https://commoncoregeometry.wikispaces.hcpss.org/Unit+1 (proving geometric theorems with video) SSN: http://www.mathwarehouse.com/geometry/congruent triangles/ (create "Proof" cards using the illustrations)	
Student Resources:	http://www.shmoop.com/common-core-standards/ccss-hs-g-c	http://www.shmoop.com/common-core-standards/ccss-hs-g-co-8.html (practice questions about congruent triangles)	
Assessment:	How do parallel lines help prove congruent triangles? Why is SAS a congruency theorem but SSA isn't? Why is proof important in geometry?	Why is SAS a congruency theorem but SSA isn't?	
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)	

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(Multiple means for students to access content and multiple modes for student to express understanding.)	http://www.ixl.com/math/geometry (congruent triangle proofs are provided with scaffolding) SSN:http://www.mathworksheets4kids.com/triangles/identify -sides-type3-1.pdf (worksheet of triangles) SSN:http://www.lauracandler.com/filecabinet/math/PDF/Toe 2ToeGeo.pdf (worksheet of triangles)	Students can by provide missing statements and reasons to complete unfinished portion of proofs SSN: Student can identify and cut out triangles where all three sides are the same on worksheet SSN: Students can measure sides and angles to compare and sort triangles into categories (congruent, similar and neither) using worksheet
Extensions for depth and complexity:	Access (Resources and/or Process) Expression (Products and/or Performance)	
	N/A	Students can construct proofs for determining the necessary and sufficient attributes for determining congruency of other shapes (e.g., parallelograms, regular polygons)
Key Knowledge and Skills:	 Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) 	
Critical Language:	Proof, theorem, congruent, triangles, angles, sides, congruence, attributes, necessary, sufficient, corresponding SSN: Proof, congruent (same), angle, side	

Learning Experience #11

The teacher may pose parallel line scenarios so that students can explore angle relationships of parallel lines cut by a transversal and related proofs.

Enactive: Students can investigate relationships between angles by exploring translated parallelograms (i.e., tiled parallelograms) using tracing paper or transparencies. Students can then color all the congruent acute angles in one color and the congruent obtuse angles in another color.

Iconic: Students can identify the key angle relationships (e.g., alternate, corresponding, vertical) on a portion of the tiled parallelograms (e.g., a set of parallel lines cut by a transversal) and determine which relationships are congruent and which are supplementary and explain these to another student by using rotations, reflections and translations.

Symbolic: Students can prove the angle relationships created when a set of parallel lines is cut by a transversal.

SSN: Students compare the angles of parallelograms and rectangles

Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs
Teacher Resources:	http://www.shmoop.com/common-core-standards/ccss-hs-g-co-9.html (detailing the standard, provides assessment questions) http://learni.st/users/S33572/boards/2805-proving-theorems-about-lines-and-angles-common-core-standard-9-12-g-co-9 (examples of the angle relationships, videos about the relationships and example proofs) http://www.brightstorm.com/math/precalculus/equations-of-lines-parabolas-circles/converse-of-parallel-lines-theorem/ (video about angle theorems)

	http://www.cpm.org/teachers/resourcesCCG.htm (select Core Connections Geometry, Chapter 2, Resource page 2.1.2 for a tiling of parallelograms) http://www.cpm.org/technology/CCG/ (select 2.1.2 - video of the translation of a parallelogram into the tiling pattern) SSN: http://www.mathworksheets4kids.com/shapes/chart-quadrilaterals-bw.pdf (compare and discuss differences in angle and side length with quadrilateral chart) SSN: http://www.math-salamanders.com/image-files/4th-grade-math-worksheets-angle-classification-3.gif (naming different types of angles in polygons)		
Student Resources:	http://www.ixl.com/math/geometry (Use D.2, D.4 and D.5. Identifying angle relationships and proving angle relationship theorems) http://www.regentsprep.org/Regents/math/geometry/GP8/Lparallel.htm (easy to read examples of angle theorems) http://quizlet.com/9815961/flashcards (flashcards of definitions and theorems related to parallel lines) SSN: https://www.pinterest.com/pin/277041814547556888/ (create a poster that identifies different types of lines and angles using stickers and toothpicks or straws) SSN: https://www.ixl.com/math/grade-4/parallel-perpendicular-intersecting (parallel and perpendicular lines) SSN: https://www.ixl.com/math/grade-4/parallel-perpendicular-intersecting (measuring angles with a protractor)		
Assessment:	Students mastering the concept and skills of this lesson should be able to answer questions such as: Why are pairs of alternate interior (exterior) angles congruent? Why are pairs of corresponding angles supplementary? Why are all the angles, created by parallel lines cut by transversal, either congruent or supplementary? What is the difference between a proof and just explaining your reasoning? SSN: What is the difference between a proof and just explaining your reasoning?		
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)	
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://img.docstoccdn.com/thumb/orig/122161993.png (handout with angle relationships) http://www.feromax.com/cgi- bin/Provelt.pl?task=getproofslist (proofs of angle relationships with scaffolding) SSN:http://www.lauracandler.com/filecabinet/math/PDF/pondpoly.pdf (activity to identify polygons and explore the differences in sides and angles)	Students can identify the types of angles on the tiled parallelograms using a handout showing the angle relationships Students can complete a two-column proof with scaffolding by correctly ordering a list of statements and their corresponding reasons SSN: Students can identify polygons and measure angles to see which ones have the same and different angles	
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)	
	http://www.illustrativemathematics.org/illustrations/56 (example of a complex parallel line problem)	Students can design unique angle measure problems for parallel lines	
Key Knowledge and Skills:	 Prove theorems about lines and angles, triangles, and parallelograms SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) SSN: Identify parallel, intersecting and perpendicular lines (MA10-GR.HS-S.4-GLE.1-EEO.I) 		
	• SSN: Identify parallel, intersecting and perpendicular lines (N	//A10-GK.П3-3.4-GLE.1-EEU.I)	

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	SSN: Parallel, parallelogram	rectangle nolvgo	nn rìght angle
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Learning Experience # 12

The teacher may provide opportunities to investigate parallelograms so that students can explore precise mathematical proofs for properties of parallelograms.

Enactive: Students can create hypotheses about properties of parallelograms by using transformations (i.e., by folding or tracing) to compare sides, angles and diagonals of parallelograms including those of specials parallelograms such as rectangles, squares, and rhombi.

Iconic: Students can test their hypotheses about properties of parallelograms by using geometric software.

Symbolic: Students can prove theorems about properties of parallelograms.9

SSN: Students can use definition chart (https://www.teacherspayteachers.com/Product/Quadrilateral-Characteristics-Graphic-Organizer-for-Geometry-1669393) to decide if shapes are quadrilaterals and if so what are the attributes that make them that particular shape. Enactive: Students can sort shapes and explain differences in terms of side length and angles. Symbolic: Students can check their sorting using charts and graphic organizers (https://www.teacherspayteachers.com/Product/Geometry-Cut-and-Paste-Math-Common-Core-Standards-3rd-4th-5th-494618).

Teacher Notes:	Proofs about properties of parallelograms should include: opposite sides are congruent; opposite angles are congruent; the diagonals of a parallelogram bisect each other; and conversely, rectangles are parallelograms with congruent diagonals. Students may struggle to make the connection between the special angle relationships formed by parallel lines cut by transversals and the opposite angles in a parallelogram. It may be helpful for students to make connections to the translated parallelograms (e.g., tiled parallelograms) from the previous learning experience.		
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs Algebraic representations model geometric transformations performed on a coordinate plane		
Teacher Resources:	http://mathbits.com/MathBits/GSP/Quadrilaterals.htm (exploration of quadrilaterals using Geometer's Sketch Pad) http://www.wyzant.com/resources/lessons/math/geometry/quadrilaterals/proving_parallelograms (examples of parallelogram proofs) http://www.curtiscenter.math.ucla.edu/downloads/Olson.pdf (PowerPoint examining proofs related to this unit) SSN: https://www.teacherspayteachers.com/Product/Geometry-Cut-and-Paste-Math-Common-Core-Standards-3rd-4th-5th-494618 (geometry definitions chart and activity focused on quadrilaterals) SSN: https://www.teacherspayteachers.com/Product/Quadrilateral-Characteristics-Graphic-Organizer-for-Geometry-1669393 (quadrilaterals graphic organizer)		
Student Resources:	http://www.ixl.com/math/geometry (practice identifying properties of quadrilaterals and proofs – not all proofs are about parallelograms, sections N.2, N.3, N.4, N.9 and N.10) http://www.shmoop.com/common-core-standards/ccss-hs-g-co-11.html (explanations and sample questions for G.CO.11) SSN: https://www.teacherspayteachers.com/Product/Quadrilateral-Classification-Chart-and-Mini-Posters-548696 (quadrilateral classification chart and mini posters) SSN: https://www.mathsisfun.com/quadrilaterals.html (lesson on quadrilaterals)		
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: Why are the diagonals of a rectangle congruent? Why are the diagonals of a rhombus perpendicular bisectors?		

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	How do definitions contribute to the development of a proof? How do the angle relationships of parallel lines and triangle congruence support proofs about parallelograms? SSN: How can you tell if a shape is a quadrilateral? There are different quadrilateral shapes — what are some of the attributes that make them different from each other?	
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://www.regentsprep.org/Regents/math/geometry/GP9/L Parallelogram.htm (completed proofs of parallelogram relationships) SSN:http://illuminations.nctm.org/uploadedFiles/Content/Lessons/Resources/6-8/665-AS-GamePolygons.pdf (printout of shapes) SSN:https://www.teacherspayteachers.com/Product/Quadrilateral-Cut-Sort-238510 (printout of quadrilaterals)	Students can complete proofs with scaffolding such as providing some of the statements and/or reasons and supplying missing information SSN: Student can cut out the shapes from a printout and then sort the shapes into those that are quadrilaterals, triangles, or those with or without right angles. SSN: Students sort quadrilaterals in this activity and explain how different angles and side lengths make them different, measuring when necessary.
Extensions for depth and complexity:	Access (Resources and/or Process)	Expression (Products and/or Performance)
	http://www.mathopenref.com/coordparallelogram.html (examines parallelogram properties using coordinate geometry)	Students can justify the properties of parallelograms using coordinate proofs involving slope and the distance formula
Key Knowledge and Skills:	 Prove theorems about lines and angles, triangles, and parallelograms SSN: Complete an if/then statement related to real life situations. (MA10-GR.HS-S.4-GLE.1-EEO.III) 	
Critical Language:	Parallelogram, rectangle, square, rhombus, opposite, sides, angles, congruent, bisector, parallel, perpendicular, perpendicular bisector, line segment, equidistant, diagonals, converses, reflections, rotations, translations, transformations SSN: Parallelogram, rhombus, square, trapezoid, rectangle, opposites, sides, perpendicular, parallel	

Learning Experience # 13

The teacher may provide opportunities to investigate triangles so that students can explore precise mathematical proofs for properties of triangles.

Enactive: Students can create hypotheses about properties of triangles by using transformations (i.e., by folding or tracing) to compare sides, angles and medians. *Iconic*: Students can test their hypotheses about properties of triangles by using geometric software.

Symbolic: Students can prove theorems about properties of triangles.

SSN: Students can use definition chart (https://www.teacherspayteachers.com/Product/Triangles-775126) to decide if shapes are triangles and if so, what kind of triangle they are and understand the attributes that make them different from each other. *Enactive*: Students can sort shapes and explain differences in terms of side length and angles.

Teacher Notes:	Proofs about properties of triangles should include: measures of interior angles of a triangle sum to 180°; base angles of isosceles
	triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length;
	the medians of a triangle meet at a point.

	Colorado Teacher-Authoreu Sample instruction		
Generalization Connection(s):	Precise definitions of basic geometric concepts facilitate the development of careful proofs Algebraic representations model geometric transformations performed on a coordinate plane		
Teacher Resources:	http://teachinginspecialeducation.blogspot.com/2013/05/angle-sum-theorem.html (example of tearing off the corner of triangle activity) http://www.mathwarehouse.com/geometry/triangles/ (examples of triangle proofs) SSN: http://www.math-salamanders.com/image-files/free-4th-grade-math-worksheets-triangle-classification-1.gif (activity on sorting triangle by obtuse, acute or right angles) SSN: https://www.teacherspayteachers.com/Product/Triangles-775126 (illustrated definition of triangles chart) SSN: https://www.teacherspayteachers.com/Product/Triangles-Math-Foldable-362149 (foldable focusing on different angles in different triangles)		
Student Resources:	http://www.regentsprep.org/Regents/math/geometry/GP6/Lisosceles.htm (isosceles triangle resources) http://www.ixl.com/math/geometry (Use M.1 and M.7. good practice with triangle mid-segment theorems and proofs.) http://www.mathsisfun.com/proof180deg.html (example of proofs for triangle angle sum) SSN: https://www.mathsisfun.com/triangle.html (lesson on triangles) SSN: https://www.ixl.com/math/grade-3/triangles-equilateral-isosceles-and-scalene (guided activity on triangles) SSN: http://nlvm.usu.edu/en/nav/frames asid 165 g 1 t 3.html?open=instructions&from=topic t 3.html (making congruent triangles) SSN: http://www.sheppardsoftware.com/mathgames/geometry/shapeshoot/triangles shoot.htm (triangle shoot game both by type and angle)		
Assessment:	Students mastering the concept and skills of this learning experience should be able to answer questions such as: What is the relationship in all the angles of a triangle? Why must triangle mid-segments be parallel to their bases? SSN: How can you tell if a shape is a triangle? There are different shaped triangles – what are some of the attributes that make them different from each other?		
Differentiation:	Access (Resources and/or Process)	Expression (Products and/or Performance)	
(Multiple means for students to access content and multiple modes for student to express understanding.)	http://www.regentsprep.org/Regents/math/geometry/GP6/Lisosceles.htm (completed proofs of triangle relationships)	Students can complete proofs with scaffolding such as providing some of the statements and/or reasons and supplying missing	
	http://www.mathopenref.com/triangle.html (critical language related to triangles) SSN: http://www.crickweb.co.uk/ks2numeracy-shape-and-weight.html#triangles (game to sort triangles by type) SSN:https://www.teacherspayteachers.com/Product/Geometry-SORTING-CLASSIFYING-TRIANGLES-79806 (sort triangles by type)	information SSN: Students can sort triangles by type and use this chart (https://www.teacherspayteachers.com/Product/Triangles- 775126) to explain why each triangle belongs in it's category by measuring sides and angles if necessary	

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	http://www.mathopenref.com/coordparallelogram.html (examines parallelogram properties using coordinate geometry but the ideas can be applied to triangles and there links at the bottom of the page to support this extension) Students can justify the properties of triangles using coordinate proofs involving slope and the distance formula	
Key Knowledge and Skills:	 Prove theorems about lines and angles, triangles, and parallelograms SSN: Demonstrate congruence of two geometric shapes using translation. (MA10-GR.HS-S.4-GLE.1-EEO.II) SSN: Complete an if/then statement related to real life situations. (MA10-GR.HS-S.4-GLE.1-EEO.III) SSN: Identify parallel, intersecting and perpendicular lines (MA10-GR.HS-S.4-GLE.1-EEO.I) SSN: Identify the midpoint on a line segment. (MA10-GR.HS-S.4-GLE.1-EEO.V) 	
Critical Language:	Triangle, isosceles, opposite, sides, angles, interior, exterior, congruent, midpoint, medians, base angles, parallel, line segment, reflections, rotations, translations, transformations SSN: Opposite, sides, parallel, perpendicular, midpoint, median, rotation	

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